Form 5 Chapter 7 Linear Programming Fully-Worked Solutions

UPSKILL 7.1

- 1 (a) $1500x + 900y \le 45\,000 \Rightarrow 5x + 3y \le 150$ (b) $y - x \le 10$ (c) $y \ge \frac{1}{10}x$ 2 (a) $x \ge 10$ (b) $y \ge 2x$ (c) $8x + 12y \le 12 \times 60 \Rightarrow 2x + 3y \le 180$ 3 (a) $x + y \le 90$
 - (b) $x \le 2y$
 - (c) $y x \le 10$

UPSKILL 7.2

1 (a) $x \ge 100, y \ge 200, x + y \le 400$

(b)



(c) Commission = 4x + 3yDraw the straight line 4x + 3y = 120

> The optimal point (minimum) is (100, 200). Minimum commission= 4(100) + 3(200) = RM1000

The optimal point (maximum) is (200, 200). Maximum commission = 4(200) + 3(200) = RM1400



(c) Monthly fees = 30x + 40yDraw the straight line 30x + 40y = 120The optimal point is (3, 6).

Maximum fee = 30(3) + 40(6) = RM330



(c) Wage = 24x + 30y

Draw the straight line 24x + 30y = 72The optimal point is (4, 4).

Maximum wage = 24(4) + 30(4) = RM216



- (c) (i) When y = 4, x (minimum) = 2 cars x (maximum) = 8 cars
 - (ii) Profits = 220x + 300yDraw the straight line 220x + 300y = 660The optimal point is (8, 4).

Maximum profit = 220(8) + 300(4) = RM2 960



- (c) (i) When y = 30, $40 \le x \le 50$.
 - (ii) Cost = 10x+12yDraw the straight line 10x+12y=120The optimal point (minimum) is (15, 5).

Minimum cost = 10(15) + 12(5) = RM210



(c) (i) Wage = 10x + 5yDraw the straight line 5x + 4y = 24The optimal point (minimum) is (3, 3).

Minimum wage = 10x + 5y = 10(3) + 5(3) = RM45

(ii) When x = 4, y (minimum) = 1 Minimum wage = 10(4) + 5(1) = RM45

> When x = 4, y (maximum) = 4 Maximum wage = 10(4) + 5(4) = RM60



(c) (i) Profits = 80x + 70yDraw the straight line 80x + 70y = 560The optimal point is (38, 34).

Maximum profit = 80(38) + 70(34) = 5420 sen = RM54.20

- (ii) Draw the straight line y x = 20
 - x (maximum) = 24 cakes
 - y (maximum) = 44 buns

8 (a) $180x + 250y \le 6750 \Longrightarrow 18x + 25y \le 675$, $60\,000x + 150\,000 \le 2\,250\,000 \Longrightarrow 2x + 5y \le 75$, $x \ge 15$



(c) (i) Profits = $20\ 000x + 40\ 000y$ Draw the straight line $20\ 000x + 40\ 000y = 80\ 000$ 2x + 4y = 8

The optimal point is (15, 16).

Maximum profit = 20 000(15)+ 40 000(16) = RM940 000

- (ii) Draw the straight line x = 2y.
 - x (maximum) = 22 houses,
 - y (maximum) = 11 houses



(c) (i) Profits = 8x + 7yDraw the straight line 8x + 7y = 56The optimal point is (4, 9).

Maximum profit = 8(4) + 7(9) = RM95

- (ii) x (maximum) = 4 baskets
- (iii) When x = 2, y (minimum) = 4 floor mats

Summative Practice 7

1 (a) $6x + 4y \le 108 \Longrightarrow 3x + 2y \le 54$, $x + y \le 24, y \ge x$

(b)



(c) (i) Profits = 40x + 30yDraw the straight line 40x + 30y = 120The optimal point is (6, 18).

Maximum profit = 40(6) + 30(18) = RM780

- (ii) Draw the straight line y = 2x
 - x (maximum) = 7 type P racquets y (maximum) = 14 type Q racquets



(c) (i) Cost = 40x + 24y

Draw the straight line 40x + 24y = 960The optimal point (minimum) is (21, 14) Minimum cost = 40(21) + 24(14) = RM1 176

(ii) When x = 30, $20 \le y \le 30$

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(c) (i) When x = 25, $35 \le y \le 55$

(ii) Allocation = 60x + 80yDraw the straight line 60x + 80y = 4800The optimal point is (16, 64).

Maximum allocation = $60x + 80y = 60(16) + 80(64) = RM6\ 080$

- 4 (a) $60x + 20y \le 12 \times 60 \Longrightarrow 3x + y \le 36$, $30x + 40y \ge 8 \times 60 \Longrightarrow 3x + 4y \ge 48$, $y \le 3x$
 - (b)



(c) (i) When y = 12, x (maximum) = 8 trophies

(ii) Profits = 100x + 140yDraw the straight line 100x + 140y = 1400The optimal point is (6, 18).

Maximum profit = 100(6) + 140(18) = RM3 120



(c) (i) If x = 150, y (minimum) = 250 boxes of pocket files

(ii) Profits = 5x + 3y

Draw the straight line 5x+3y=1500The optimal point is (375, 125) Maximum profit = 5(375) + 3(125) = RM2250

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6 (a) x + y \le 90, x \le 2y, y - x \le 40
(b)
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(c) (i) x (maximum) = 60 ballpoint pens

(ii) Cost = 1.5x + 5yDraw the straight line 1.5x + 5y = 75The optimal point is (25, 65).

Maximum cost = 1.5(25) + 5(65) = RM362.50

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7 (a) x + y \le 84, y \ge 14, y \le \frac{5}{2}x
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(b)



(c) (i) x (minimum) = 6 course P participants

(ii) Fees = 300x + 450yDraw the straight line 300x + 450y = 13500The optimal point is (24, 60).

Maximum fee = $300(24) + 450(60) = RM34\ 200$



(c) (i) If x = 24, y (minimum) = 8 tins of *satin-glo* paints (ii) Expenditure = 100x + 140yDraw the straight line 100x + 140y = 1400The optimal point is (15, 30).

Maximum expenditure = 100(15) + 140(30) = RM5700



(c) (i) If x = 200, y (maximum) = 450 chairs (ii) Profits = 7x + 5yDraw the straight line 7x + 5y = 3500The optimal point is (320, 360).

Maximum profit = $7(320) + 5(360) = RM4\ 040$

10 (a) $x + y \ge 40$, $96x + 80y \le 240 \times 60 \Longrightarrow 6x + 5y \le 900$, $\frac{x}{y} \le \frac{3}{5} \Longrightarrow 3y \ge 5x$

(b)



(c) Sales = 25x + 30yDraw the straight line 25x + 30y = 750

The optimal point (minimum) is (15, 25). Minimum sale = $25(15) + 30(25) = RM1 \ 150$

The optimal point (maximum) is (62, 105). Maximum sale = 25(62) + 30(105) = RM4700

RM1 125 \leq Total sales \leq RM4 700

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