

**Form 4 Chapter 3**  
**Systems of Equations**  
**Fully-Worked Solutions**

**UPSKILL 3.1a**

1 (a)  $p+q+r=4 \dots (1)$   
 $2p-q+6r=8 \dots (2)$   
 $p+2q-3r=0 \dots (3)$

$$\begin{array}{r} p+q+r=4 \quad \dots (1) \\ (+) 2p-q+6r=8 \quad \dots (2) \\ \hline 3p+7r=12 \quad \dots (4) \end{array}$$

$$\begin{array}{r} 2p+2q+2r=8 \quad \dots (1) \times 2 \\ (-) p+2q-3r=0 \quad \dots (3) \\ \hline p+5r=8 \quad \dots (5) \end{array}$$

$$\begin{array}{r} 3p+7r=12 \quad \dots (4) \\ (-) 3p+15r=24 \quad \dots (5) \times 3 \\ \hline -8r=-12 \\ r=\frac{-12}{-8} \\ r=\frac{3}{2} \end{array}$$

From (4) :

$$\begin{aligned} 3p+7\left(\frac{3}{2}\right) &= 12 \\ 6p+21 &= 24 \\ 6p &= 3 \\ p &= \frac{1}{2} \end{aligned}$$

From (1) :

$$\begin{aligned} \frac{1}{2}+q+\frac{3}{2} &= 4 \\ q+2 &= 4 \\ q &= 2 \end{aligned}$$

(b)  $r+s+t=0 \dots (1)$   
 $5r-3s+5t=12 \dots (2)$   
 $10r+s-5t=6 \dots (3)$

$$\begin{array}{r} r+s+t=0 \quad \dots (1) \\ (-) 10r+s-5t=6 \quad \dots (2) \\ \hline -9r+6t=-6 \\ -3r+2t=-2 \quad \dots (4) \end{array}$$

$$\begin{array}{r} 3r+3s+3t=0 \quad \dots (1) \times 3 \\ (+) 5r-3s+5t=12 \quad \dots (2) \\ \hline 8r+8t=12 \\ 2r+2t=3 \quad \dots (5) \end{array}$$

$$\begin{array}{r} -3r+2t=-2 \quad \dots (4) \\ (-) 2r+2t=3 \quad \dots (5) \\ \hline -5r=-5 \\ r=1 \end{array}$$

From (4) :  $-3(1)+2t=-2$   
 $2t=3-2$   
 $t=\frac{1}{2}$

From (1) :  $1+s+\frac{1}{2}=0$   
 $s=-1.5$

$$\begin{aligned}
 \text{(c) } & 2b + 3d + m = -1 \quad \dots (1) \\
 & b - d - m = -8 \quad \dots (2) \\
 & 3b + d + 4m = 11 \quad \dots (3) \\
 & \quad \quad \quad b - d - m = -8 \quad \dots (2) \\
 (+) & \quad \quad \quad \underline{3b + d + 4m = 11 \quad \dots (3)} \\
 & \quad \quad \quad 4b + 3m = 3 \quad \dots (4) \\
 & \quad \quad \quad 2b + 3d + m = -1 \quad \dots (1) \\
 (+) & \quad \quad \quad \underline{3b - 3d - 3m = -24 \quad \dots (2) \times 3} \\
 & \quad \quad \quad 5b - 2m = -25 \quad \dots (5) \\
 & \quad \quad \quad 8b + 6m = 6 \quad \dots (4) \times 2 \\
 (+) & \quad \quad \quad \underline{15b - 6m = -75 \quad \dots (5) \times 3} \\
 & \quad \quad \quad 23b = -69 \\
 & \quad \quad \quad b = -3 \\
 \text{From (4): } & 4(-3) + 3m = 3 \\
 & \quad \quad \quad 3m = 15 \\
 & \quad \quad \quad m = 5
 \end{aligned}$$

$$\begin{aligned}
 \text{From (1):} \\
 2(-3) + 3d + 5 = -1 \\
 3d = 0 \\
 d = 0
 \end{aligned}$$

$$\begin{aligned}
 \text{2 (a) } & h + k = 2 - m \\
 & h + k + m = 2 \quad \dots (1) \\
 & 2h + 3m = k + 9 \\
 & 2h - k + 3m = 9 \quad \dots (2) \\
 & \quad \quad \quad k + 2 = -3h + 2m \\
 & \quad \quad \quad \underline{3h + k - 2m = -2 \quad \dots (3)} \\
 & \quad \quad \quad h + k + m = 2 \quad \dots (1) \\
 (+) & \quad \quad \quad \underline{2h - k + 3m = 9 \quad \dots (2)} \\
 & \quad \quad \quad 3h + 4m = 11 \quad \dots (4) \\
 & \quad \quad \quad h + k + m = 2 \quad \dots (1) \\
 (-) & \quad \quad \quad \underline{3h + k - 2m = -2 \quad \dots (3)} \\
 & \quad \quad \quad -2h + 3m = 4 \quad \dots (5) \\
 & \quad \quad \quad 6h + 8m = 22 \quad \dots (4) \times 2 \\
 (+) & \quad \quad \quad \underline{-6h + 9m = 12 \quad \dots (5) \times 3} \\
 & \quad \quad \quad 17m = 34 \\
 & \quad \quad \quad m = 2
 \end{aligned}$$

$$\begin{aligned}
 \text{From (4): } & 3h + 4m = 11 \\
 & \quad \quad \quad 3h + 4(2) = 11 \\
 & \quad \quad \quad 3h = 3 \\
 & \quad \quad \quad h = 1
 \end{aligned}$$

$$\begin{aligned}
 \text{From (1):} \\
 1 + k + 2 = 2 \\
 k = -1
 \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad & 2h + k = m - 2 \\ & 2h + k - m = -2 \quad \dots (1) \end{aligned}$$

$$\begin{aligned} & h - m = k - 6 \\ & h - k - m = -6 \quad \dots (2) \end{aligned}$$

$$\begin{aligned} & h - 7 = -2k - 3m \\ & h + 2k + 3m = 7 \quad \dots (3) \end{aligned}$$

$$\begin{aligned} & 2h + k - m = -2 \quad \dots (1) \\ (+) \quad & h - k - m = -6 \quad \dots (2) \end{aligned}$$

$$\hline 3h - 2m = -8 \quad \dots (4)$$

$$\begin{aligned} & 4h + 2k - 2m = -4 \quad \dots (1) \times 2 \\ (-) \quad & h + 2k + 3m = 7 \quad \dots (3) \end{aligned}$$

$$\hline 3h - 5m = -11 \quad \dots (5)$$

$$\begin{aligned} & 3h - 2m = -8 \quad \dots (4) \\ (-) \quad & 3h - 5m = -11 \quad \dots (5) \end{aligned}$$

$$\hline \begin{aligned} 3m &= 3 \\ m &= 1 \end{aligned}$$

From (4) :  $3h - 2(1) = -8$

$$3h = -6$$

$$h = -2$$

From (1) :  $2(-2) + k - 1 = -2$

$$k = -2 + 4 + 1$$

$$k = 3$$

$$\begin{aligned} \text{(c)} \quad & 2h + 3k = 9 - m \\ & 2h + 3k + m = 9 \quad \dots (1) \end{aligned}$$

$$\begin{aligned} & h - 11 = k - 4m \\ & h - k + 4m = 11 \quad \dots (2) \end{aligned}$$

$$\begin{aligned} & k - 5m = -3h - 23 \\ & 3h + k - 5m = -23 \quad \dots (3) \end{aligned}$$

$$\begin{aligned} & h - k + 4m = 11 \quad \dots (2) \\ (+) \quad & 3h + k - 5m = -23 \quad \dots (3) \end{aligned}$$

$$\hline 4h - m = -12 \quad \dots (4)$$

$$\begin{aligned} & 2h + 3k + m = 9 \quad \dots (1) \\ (+) \quad & 3h - 3k + 12m = 33 \quad \dots (2) \end{aligned}$$

$$\hline 5h + 13m = 42 \quad \dots (5)$$

$$52h - 13m = -156 \quad \dots (4) \times 13$$

$$(+)\quad 5h + 13m = 42 \quad \dots (5)$$

$$\hline \begin{aligned} 57h &= -114 \\ h &= -2 \end{aligned}$$

From (4) :  $4(-2) - m = -12$

$$m = 4$$

From (1) :  $2h + 3k + m = 9$

$$2(-2) + 3k + 4 = 9$$

$$3k = 9 + 4 - 4$$

$$k = 3$$

### UPSKILL 3.1b

- 1 The total amount invested in ASB, ASW and ASM is RM40 000.

$$x + y + z = 40\,000 \dots (1)$$

The amount invested in ASM is RM10 000 more than that of ASW.

$$z - y = 10\,000 \dots (2)$$

Dividend = RM3 400

$$\frac{7}{100}x + \frac{9}{100}y + \frac{9}{100}z = 3\,400$$

$$7x + 9y + 9z = 340\,000 \dots (3)$$

$$7x + 7y + 7z = 280\,000 \dots (1) \times 7$$

$$(-) \quad 7x + 9y + 9z = 340\,000 \dots (3)$$

$$\hline -2y - 2z = -60\,000$$

$$-y - z = -30\,000 \dots (4)$$

$$z - y = 10\,000 \dots (2)$$

$$(-) \quad -y - z = -30\,000 \dots (4)$$

$$\hline 2z = 40\,000$$

$$z = 20\,000$$

$$\text{From (2) : } 20\,000 - y = 10\,000$$

$$y = 10\,000$$

$$\text{From (1) : } \quad x + y + z = 40\,000$$

$$x + 10\,000 + 20\,000 = 40\,000$$

$$x = 10\,000$$

$$2 \quad 2x + 2y + z = 46\,000 \dots (1)$$

$$3x + 4y + 2z = 82\,000 \dots (2)$$

$$4x + 4y + 3z = 100\,000 \dots (3)$$

$$3x + 4y + 2z = 82\,000 \dots (2)$$

$$(-) \quad 4x + 4y + 3z = 100\,000 \dots (3)$$

$$\hline -x - z = -18\,000 \dots (4)$$

$$4x + 4y + 2z = 92\,000 \dots (1) \times 2$$

$$(-) \quad 3x + 4y + 2z = 82\,000 \dots (2)$$

$$\hline x = 10\,000$$

$$\text{From (4) : } -x - z = -18\,000$$

$$-10\,000 - z = -18\,000$$

$$z = 8\,000$$

From (1) :

$$2x + 2y + z = 46\,000$$

$$2(10\,000) + 2y + 8\,000 = 46\,000$$

$$2y = 18\,000$$

$$y = 9\,000$$

$$\begin{aligned}
3 \quad & 60x + 80y + 70z = 1\,660 \dots (1) \\
& 80x + 30y + 50z = 1\,100 \dots (2) \\
& 30x + 20y + 10z = 430 \dots (3) \\
& \underline{60x + 80y + 70z = 1\,660 \dots (1)} \\
(-) \quad & \underline{60x + 40y + 20z = 860 \dots (3) \times 2} \\
& 40y + 50z = 800 \dots (4) \\
& \underline{480x + 640y + 560z = 13\,280 \dots (1) \times 8} \\
(-) \quad & \underline{480x + 180y + 300z = 6\,600 \dots (2) \times 6} \\
& 460y + 260z = 6\,680 \dots (5) \\
& 4y + 5z = 80 \dots (4) \times \frac{1}{10} \\
& 23y + 13z = 334 \dots (5) \times \frac{1}{20} \\
& \underline{4y + 5z = 80 \dots (6)} \\
& 23y + 13z = 334 \dots (7) \\
& \underline{52y + 65z = 1\,040 \dots (6) \times 13} \\
(-) \quad & \underline{115y + 65z = 1\,670 \dots (7) \times 5} \\
& -63y = -630 \\
& y = 10 \\
& \text{From (6) : } 4(10) + 5z = 80 \\
& \qquad \qquad \qquad z = 8 \\
& \text{From (1) :} \\
& 60x + 80(10) + 70(8) = 1\,660 \\
& \qquad \qquad \qquad x = 5
\end{aligned}$$

**UPSKILL 3.2a**

$$\begin{aligned}
1 \text{ (a) } \quad & x + y = 1 \qquad \dots (1) \\
& 2x^2 + 2y^2 = 17 \qquad \dots (2)
\end{aligned}$$

From (1) :  
 $y = 1 - x \quad (3)$

Substitute (3) into (2) :

$$\begin{aligned}
& 2x^2 + 2(1-x)^2 = 17 \\
& 2x^2 + 2(1 - 2x + x^2) - 17 = 0 \\
& 2x^2 + 2 - 4x + 2x^2 - 17 = 0 \\
& 4x^2 - 4x - 15 = 0 \\
& (2x - 5)(2x + 3) = 0 \\
& x = \frac{5}{2} \text{ or } x = -\frac{3}{2}
\end{aligned}$$

From (3) :

When  $x = \frac{5}{2}$ ,  $y = 1 - \frac{5}{2} = -\frac{3}{2}$

When  $x = -\frac{3}{2}$ ,  $y = 1 - \left(-\frac{3}{2}\right) = \frac{5}{2}$

$$\begin{aligned}
\text{(b) } \quad & x + 1 = 2y \qquad \dots (1) \\
& x^2 + xy - 26 = 0 \qquad \dots (2)
\end{aligned}$$

From (1) :  
 $x = 2y - 1 \quad (3)$

Substitute (3) into (2) :

$$\begin{aligned}
& (2y - 1)^2 + (2y - 1)y - 26 = 0 \\
& 4y^2 - 4y + 1 + 2y^2 - y - 26 = 0 \\
& 6y^2 - 5y - 25 = 0 \\
& (2y - 5)(3y + 5) = 0 \\
& y = \frac{5}{2} \text{ or } y = -\frac{5}{3}
\end{aligned}$$

When  $y = \frac{5}{2}$ ,  $x = 2\left(\frac{5}{2}\right) - 1 = 4$

When  $y = -\frac{5}{3}$ ,  $x = 2\left(-\frac{5}{3}\right) - 1 = -\frac{13}{3}$

$$(c) \quad 2x + y + 2 = 0 \quad \dots (1)$$

$$x^2 + y^2 + 2x + 6y + 1 = 0 \quad \dots (2)$$

From (1) :

$$y = -2x - 2 \quad \dots (3)$$

Substitute (3) into (2) :

$$x^2 + (-2x - 2)^2 + 2x + 6(-2x - 2) + 1 = 0$$

$$x^2 + 4x^2 + 8x + 4 + 2x - 12x - 12 + 1 = 0$$

$$5x^2 - 2x - 7 = 0$$

$$(5x - 7)(x + 1) = 0$$

$$x = \frac{7}{5} \text{ or } x = -1$$

$$\text{When } x = \frac{7}{5}, y = -2\left(\frac{7}{5}\right) - 2 = -\frac{24}{5}$$

$$\text{When } x = -1, y = -2(-1) - 2 = 0$$

$$(d) \quad x + y = 2 \quad \dots (1)$$

$$x^2 + xy + y^2 = 12 \quad \dots (2)$$

From (1) :

$$y = 2 - x \quad \dots (3)$$

Substitute (3) into (2) :

$$x^2 + x(2 - x) + (2 - x)^2 = 12$$

$$x^2 + 2x - x^2 + 4 - 4x + x^2 - 12 = 0$$

$$x^2 - 2x - 8 = 0$$

$$(x - 4)(x + 2) = 0$$

$$x = 4 \text{ or } x = -2$$

From (3) :

$$\text{When } x = 4, y = 2 - 4 = -2$$

$$\text{When } x = -2, y = 2 - (-2) = 4$$

$$2 \text{ (a) } 2x + 3y = 2 \quad \dots (1)$$

$$12x^2 + 18y^2 = 5 \quad \dots (2)$$

From (1) :

$$2x + 3y = 2$$

$$y = \frac{2 - 2x}{3} \quad \dots (3)$$

Substitute (3) into (2) :

$$12x^2 + 18\left(\frac{2 - 2x}{3}\right)^2 = 5$$

$$12x^2 + 18\left(\frac{4 - 8x + 4x^2}{9}\right) - 5 = 0$$

$$12x^2 + 2(4 - 8x + 4x^2) - 5 = 0$$

$$12x^2 + 8 - 16x + 8x^2 - 5 = 0$$

$$20x^2 - 16x + 3 = 0$$

$$(2x - 1)(10x - 3) = 0$$

$$x = \frac{1}{2} \text{ or } x = \frac{3}{10}$$

From (3) :

$$\text{When } x = \frac{1}{2}, y = \frac{2 - 2\left(\frac{1}{2}\right)}{3} = \frac{1}{3}$$

$$\text{When } x = \frac{3}{10}, y = \frac{2 - 2\left(\frac{3}{10}\right)}{3} = \frac{7}{15}$$

$$(b) \quad 3x + 2y = 1 \quad \dots (1)$$

$$6xy + 12y^2 = 1 \quad \dots (2)$$

From (1) :

$$x = \frac{1 - 2y}{3} \quad \dots (3)$$

Substitute (3) into (2) :

$$6y\left(\frac{1 - 2y}{3}\right) + 12y^2 = 1$$

$$2y(1 - 2y) + 12y^2 - 1 = 0$$

$$2y - 4y^2 + 12y^2 - 1 = 0$$

$$8y^2 + 2y - 1 = 0$$

$$(4y - 1)(2y + 1) = 0$$

$$y = \frac{1}{4} \text{ or } y = -\frac{1}{2}$$

From (3) :

$$\text{When } y = \frac{1}{4}, x = \frac{1 - 2\left(\frac{1}{4}\right)}{3} = \frac{1}{6}$$

$$\text{When } y = -\frac{1}{2}, x = \frac{1 - 2\left(-\frac{1}{2}\right)}{3} = \frac{2}{3}$$

$$(c) \quad 2x + 3y = 4 \quad \dots (1)$$

$$x^2 + xy + y^2 = 3 \quad \dots (2)$$

From (1) :

$$y = \frac{4 - 2x}{3} \quad \dots (3)$$

Substitute (3) into (2) :

$$x^2 + x\left(\frac{4 - 2x}{3}\right) + \left(\frac{4 - 2x}{3}\right)^2 - 3 = 0$$

$$9x^2 + 3x(4 - 2x) + (4 - 2x)^2 - 27 = 0$$

$$9x^2 + 12x - 6x^2 + 16 - 16x + 4x^2 - 27 = 0$$

$$7x^2 - 4x - 11 = 0$$

$$(7x - 11)(x + 1) = 0$$

$$x = \frac{11}{7} \text{ or } x = -1$$

$$7x^2 + 44x - 96 = 0$$

From (3) :

$$\text{When } x = \frac{11}{7}, y = \frac{4 - 2\left(\frac{11}{7}\right)}{3} = \frac{2}{7}$$

$$\text{When } x = -1, y = \frac{4 - 2(-1)}{3} = 2$$

$$3 \text{ (a) } x - \frac{1}{2}y = \frac{5}{2}$$

$$2x - y = 5$$

$$y = 2x - 5 \dots (1)$$

$$2x + y = -\frac{2}{y}$$

$$2xy + y^2 = -2$$

$$2xy + y^2 + 2 = 0 \dots (2)$$

Substitute (1) into (2) :

$$2x(2x - 5) + (2x - 5)^2 + 2 = 0$$

$$4x^2 - 10x + 4x^2 - 20x + 25 + 2 = 0$$

$$8x^2 - 30x + 27 = 0$$

$$(4x - 9)(2x - 3) = 0$$

$$x = \frac{9}{4} \text{ or } x = \frac{3}{2}$$

From (1) :

$$\text{When } x = \frac{9}{4}, y = 2\left(\frac{9}{4}\right) - 5 = -\frac{1}{2}$$

$$\text{When } x = \frac{3}{2}, y = 2\left(\frac{3}{2}\right) - 5 = -2$$

$$(b) \frac{x}{4} + \frac{y}{3} = 1$$

$$\frac{3x + 4y}{12} = 1$$

$$3x + 4y = 12$$

$$y = \frac{12 - 3x}{4} \dots (1)$$

$$\frac{3}{y} - \frac{2}{x} = \frac{7}{12}$$

$$\frac{3x - 2y}{xy} = \frac{7}{12}$$

$$36x - 24y = 7xy$$

$$36x - 7xy - 24y = 0 \dots (2)$$

Substitute (1) into (2) :

$$36x - 7x\left(\frac{12 - 3x}{4}\right) - 24\left(\frac{12 - 3x}{4}\right) = 0$$

$$144x - 7x(12 - 3x) - 24(12 - 3x) = 0$$

$$144x - 84x + 21x^2 - 288 + 72x = 0$$

$$21x^2 + 132x - 288 = 0$$

$$(7x - 12)(x + 8) = 0$$

$$x = \frac{12}{7} \text{ or } x = -8$$

From (1) :

$$\text{When } x = \frac{12}{7}, y = \frac{12 - 3\left(\frac{12}{7}\right)}{4} = \frac{12}{7}$$

$$\text{When } x = -8, y = \frac{12 - 3(-8)}{4} = 9$$

$$4 \text{ (a) } 12y^2 - 5x^2 = 2y - 5x = 7$$

$$2y - 5x = 7$$

$$y = \frac{7 + 5x}{2} \dots (1)$$

$$12y^2 - 5x^2 = 7 \dots (2)$$

Substitute (1) into (2) :

$$12\left(\frac{5x + 7}{2}\right)^2 - 5x^2 - 7 = 0$$

$$12\left(\frac{25x^2 + 70x + 49}{4}\right) - 5x^2 - 7 = 0$$

$$3(25x^2 + 70x + 49) - 5x^2 - 7 = 0$$

$$75x^2 + 210x + 147 - 5x^2 - 7 = 0$$

$$70x^2 + 210x + 140 = 0$$

$$x^2 + 3x + 2 = 0$$

$$(x + 1)(x + 2) = 0$$

$$x = -1 \text{ or } x = -2$$

From (1) :

$$\text{When } x = -1, y = \frac{7 + 5(-1)}{2} = 1$$

$$\text{When } x = -2, y = \frac{7 + 5(-2)}{2} = -\frac{3}{2}$$

$$(b) x^2 - xy + y^2 = 2x + 2y = 12$$

$$2x + 2y = 12$$

$$x + y = 6$$

$$y = -x + 6 \dots (1)$$

$$x^2 - xy + y^2 = 12 \dots (2)$$

Substitute (1) into (2) :

$$x^2 - x(-x + 6) + (-x + 6)^2 = 12$$

$$x^2 + x^2 - 6x + x^2 - 12x + 36 - 12 = 0$$

$$3x^2 - 18x + 24 = 0$$

$$x^2 - 6x + 8 = 0$$

$$(x - 4)(x - 2) = 0$$

$$x = 4 \text{ or } x = 2$$

From (1) :

$$\text{When } x=4, y=-4+6=2$$

$$\text{When } x=2, y=-2+6=4$$

$$\begin{aligned} 5 \quad x+3y+1 &= 0 \\ x &= -3y-1 \dots (1) \end{aligned}$$

$$x^2+xy+y^2=4 \dots (2)$$

Substitute (1) into (2) :

$$(-3y-1)^2+y(-3y-1)+y^2-4=0$$

$$9y^2+6y+1-3y^2-y+y^2-4=0$$

$$7y^2+5y-3=0$$

$$y = \frac{-5 \pm \sqrt{5^2 - 4(7)(-3)}}{2(7)}$$

$$y = \frac{-5 \pm \sqrt{109}}{14}$$

$$y = 0.3886 \text{ or } y = -1.103$$

From (1) :

$$\text{When } y = 0.3886,$$

$$x = -3(0.3886) - 1 = -2.166$$

$$\text{When } y = -1.103,$$

$$x = -3(-1.103) - 1 = 2.309$$

$$\begin{aligned} 6 \quad 3x+y+6 &= x^2+x-y=2 \\ 3x+y+6 &= 2 \\ 3x+y &= -4 \\ y &= -3x-4 \dots (1) \end{aligned}$$

$$x^2+x-y=2$$

$$y = x^2+x-2 \dots (2)$$

Substitute (2) into (1) :

$$3x + (x^2+x-2) = -4$$

$$x^2+4x+2=0$$

$$x = \frac{-4 \pm \sqrt{4^2 - 4(1)(2)}}{2}$$

$$x = \frac{-4 \pm \sqrt{8}}{2}$$

$$x = -0.586 \text{ or } x = -3.414$$

From (1) :

$$\text{When } x = -0.586, y = -3(-0.586) - 4 = -2.242$$

$$\text{When } x = -3.414, y = -3(-3.414) - 4 = 6.242$$

$$\begin{aligned} 7 \quad my+kx &= 8 \\ 2m+3k &= 8 \\ m &= \frac{8-3k}{2} \dots (1) \end{aligned}$$

$$m^2y-k^2x+10=0$$

$$2m^2-3k^2+10=0 \dots (2)$$

Substitute (1) into (2) :

$$2\left(\frac{8-3k}{2}\right)^2 - 3k^2 + 10 = 0$$

$$2\left(\frac{64-48k+9k^2}{4}\right) - 3k^2 + 10 = 0$$

$$64-48k+9k^2-6k^2+20=0$$

$$3k^2-48k+84=0$$

$$k^2-16k+28=0$$

$$(k-2)(k-14)=0$$

$$k=2 \text{ or } k=14$$

From (1) :

$$\text{When } k=2, m = \frac{8-3(2)}{2} = 1$$

$$\text{When } k=14, m = \frac{8-3(14)}{2} = -17$$

### UPSKILL 3.2b

1 Let the two numbers be  $x$  and  $y$ .

$$y-x=2$$

$$y=x+2 \dots (1)$$

$$x^2+y^2=20 \dots (2)$$

From (1) :  $y=x+2 \dots (3)$

Substitute (3) into (2) :

$$x^2+(x+2)^2=20$$

$$x^2+x^2+4x+4-20=0$$

$$2x^2+4x-16=0$$

$$x^2+2x-8=0$$

$$(x-2)(x+4)=0$$

$$x=2 \text{ or } x=-4$$

$x=-4$  is not accepted.

Hence,  $x=2$ .

When  $x=2$ , from (3),

$$y=2+2=4$$

Hence, the two required numbers are 2 and 4.

2 Perimeter = 48

$$4(10x)+2y=48$$

$$20x+y=24$$

$$y=24-20x \dots (1)$$



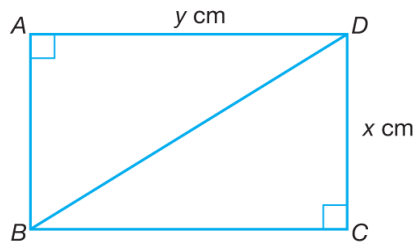
$$\begin{aligned} \text{Area} &= 144 \text{ cm}^2 \\ 2\left(\frac{1}{2} \times 12x \times 8x\right) + 12xy &= 144 \\ 96x^2 + 12xy &= 144 \\ 8x^2 + xy - 12 &= 0 \dots (2) \end{aligned}$$

Substitute (1) into (2) :

$$\begin{aligned} 8x^2 + x(24 - 20x) &= 12 \\ 8x^2 + 24x - 20x^2 &= 12 \\ -12x^2 + 24x - 12 &= 0 \\ x^2 - 2x + 1 &= 0 \\ (x-1)^2 &= 0 \\ x &= 1 \end{aligned}$$

$$\text{From (1) : } y = 24 - 20x = 24 - 20(1) = 4$$

3



$$\text{Perimeter} = 18$$

$$2x + 2y = 18$$

$$x + y = 9$$

$$y = 9 - x \dots (1)$$

$$BD^2 = x^2 + y^2 = 45 \dots (2)$$

Substitute (1) into (2) :

$$x^2 + (9-x)^2 = 45 \dots (2)$$

$$x^2 + 81 - 18x + x^2 - 45 = 0$$

$$2x^2 - 18x + 36 = 0$$

$$x^2 - 9x + 18 = 0$$

$$x = 6 \text{ or } x = 3$$

$x = 6$  is not accepted.

Hence,  $x = 3$

$$\text{From (1), when } x = 3, y = 9 - 3 = 6$$

Hence, length = 6 cm and width = 3 cm

4

$$\text{Perimeter} = 56 \text{ cm}$$

$$4(x+1) + 4(y-2) + 4(x+2) = 56$$

$$(x+1) + (y-2) + (x+2) = 14$$

$$2x + y = 13$$

$$y = 13 - 2x$$

$$\text{Base area} = 15$$

$$(x+1)(y-2) = 15$$

$$xy - 2x + y - 2 = 15 = 0$$

$$x(13 - 2x) - 2x + (13 - 2x) - 17 = 0$$

$$-2x^2 + 13x - 2x - 2x + 13 - 17 = 0$$

$$-2x^2 + 9x - 4 = 0$$

$$2x^2 - 9x + 4 = 0$$

$$(x-4)(2x-1) = 0$$

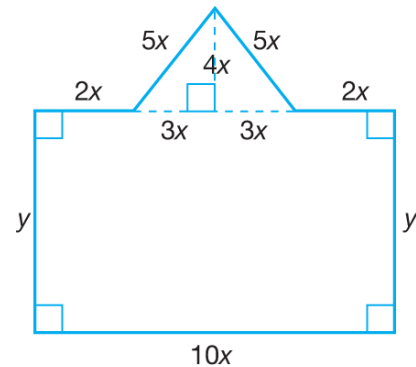
$$x = 4 \text{ or } x = \frac{1}{2}$$

$x = \frac{1}{2}$  is not accepted.

Hence,  $x = 4$ .

$$y = 13 - 2x = 13 - 2(4) = 5$$

5



$$\text{Perimeter} = 36 \text{ m}$$

$$10x + 4x + 10x + 2y = 36$$

$$24x + 2y = 36$$

$$12x + y = 18$$

$$y = 18 - 12x \dots (1)$$

Area of the enclosed region = 72

$$10xy + \frac{1}{2}(6x)(4x) = 72$$

$$10x(18 - 12x) + \frac{1}{2}(6x)(4x) = 72$$

$$10x(18 - 12x) + (3x)(4x) = 72$$

$$10x(2)(9 - 6x) + 12x^2 - 72 = 0$$

$$5x(9 - 6x) + 3x^2 - 18 = 0$$

$$45x - 30x^2 + 3x^2 - 18 = 0$$

$$-27x^2 + 45x - 18 = 0$$

$$9x^2 - 15x + 6 = 0$$

$$3x^2 - 5x + 2 = 0$$

$$(x-1)(3x-2) = 0$$

$$x = 1 \text{ or } x = \frac{2}{3}$$

From (1) :

$$\text{When } x = 1, y = 18 - 12(1) = 6$$

$$\text{When } x = \frac{2}{3}, y = 18 - 12\left(\frac{2}{3}\right) = 10$$

6

$$\text{Perimeter} = 22 \text{ cm}$$

$$3x + 4x + 5x + 2x + 2y = 22$$

$$14x + 2y = 22$$

$$7x + y = 11$$

$$y = 11 - 7x \dots (1)$$

$$\text{Area} = 10 \text{ cm}^2$$

$$\frac{1}{2}(4x)(3x) + xy = 10$$

$$6x^2 + xy = 10$$

$$6x^2 + x(11 - 7x) = 10$$

$$6x^2 + 11x - 7x^2 - 10 = 0$$

$$-x^2 + 11x - 10 = 0$$

$$x^2 - 11x + 10 = 0$$

$$(x - 10)(x - 1) = 0$$

$$x = 10 \text{ or } x = 1$$

$x = 10$  is not accepted.

$$x = 1$$

$$\text{From (1): } y = 11 - 7(1) = 4$$

### Summative Practice 3

$$1 \quad 2(x + y) - 3z = 9$$

$$2x + 2y - 3z = 9 \dots (1)$$

$$3x - 5(y + z) = -10$$

$$3x - 5y - 5z = -10 \dots (2)$$

$$x + 2y + 3z = 3 \dots (3)$$

$$(1) + (3): 3x + 4y = 12 \dots (4)$$

$$(1) \times 5: 10x + 10y - 15z = 45 \dots (5)$$

$$(2) \times 3: 9x - 15y - 15z = -30 \dots (6)$$

$$(5) - (6): x + 25y = 75 \dots (7)$$

$$(7) \times 3: 3x + 75y = 225 \dots (8)$$

$$(8) - (4): 71y = 213$$

$$y = 3$$

Substitute  $y = 3$  into (8):

$$3x + 75(3) = 225$$

$$x = 0$$

Substitute  $x = 0$  and  $y = 3$  into (1):

$$2(0) + 2(3) - 3z = 9$$

$$z = -1$$

$$2 \quad 2x + 6y + 5z + 1 = 0$$

$$2x + 6y + 5z = -1 \dots (1)$$

$$30(x - y - z) + 11 = 0$$

$$30x - 30y - 30z = -11 \dots (2)$$

$$6(x + y) - 10z - 9 = 0$$

$$6x + 6y - 10z = 9 \dots (3)$$

$$(1) \times 2: 4x + 12y + 10z = -2 \dots (4)$$

$$(1) \times 6: 12x + 36y + 30z = -6 \dots (5)$$

$$(3) + (4): 10x + 18y = 7 \dots (6)$$

$$(2) + (5): 42x + 6y = -17 \dots (7)$$

$$(7) \times 3: 126x + 18y = -51 \dots (8)$$

$$(8) - (6): 116x = -58$$

$$x = -\frac{1}{2}$$

Substitute  $x = -\frac{1}{2}$  into (6):

$$10\left(-\frac{1}{2}\right) + 18y = 7$$

$$18y = 12$$

$$y = \frac{2}{3}$$

Substitute  $x = -\frac{1}{2}$  and  $y = \frac{2}{3}$  into (1):

$$2\left(-\frac{1}{2}\right) + 6\left(\frac{2}{3}\right) + 5z = -1$$

$$-1 + 4 + 5z = -1$$

$$5z = -4$$

$$z = -\frac{4}{5}$$

$$3 \quad \frac{1}{2}y + \frac{1}{3}z = 26$$

$$3y + 2z = 156 \dots (1)$$

$$\frac{1}{3}x + \frac{1}{4}z = 23$$

$$4x + 3z = 276 \dots (2)$$

$$\frac{1}{2}x + \frac{1}{4}y = 28$$

$$2x + y = 112 \dots (3)$$

$$y = -2x + 112 \dots (4)$$

Substitute (4) into (1) :

$$3(-2x + 112) + 2z = 156$$

$$-6x + 336 + 2z = 156$$

$$-6x + 2z = -180$$

$$-3x + z = -90 \dots (5)$$

$$(5) \times 3 : -9x + 3z = -270 \dots (6)$$

$$(2) - (6) : \quad 13x = 546$$

$$x = 42$$

Substitute  $x = 42$  into (2) :

$$4(42) + 3z = 276$$

$$3z = 108$$

$$z = 36$$

Substitute  $x = 42$  into (4) :

$$y = -2(42) + 112 = 28$$

$$4 \quad 5x + 2y + 3z = 23.60 \dots (1)$$

$$3x + y + 2z = 14.20 \dots (2)$$

$$x + 3z = 4y \Rightarrow x - 4y + 3z = 0 \dots (3)$$

$$(2) \times 2 : 6x + 2y + 4z = 28.4 \dots (4)$$

$$(2) \times 4 : 12x + 4y + 8z = 56.8 \dots (5)$$

$$(4) - (1) : x + z = 4.8 \dots (6)$$

$$(3) + (5) : 13x + 11z = 56.8 \dots (7)$$

$$(6) \times 11 : 11x + 11z = 52.8 \dots (8)$$

$$(7) - (8) : 2x = 4$$

$$x = 2$$

Substitute  $x = 2$  into (7) :

$$13(2) + 11z = 56.8$$

$$11z = 30.8$$

$$z = 2.80$$

Substitute  $x = 2$  and  $z = 2.80$  into (1) :

$$5(2) + 2y + 3(2.8) = 23.60$$

$$2y = 5.2$$

$$y = 2.6$$

Hence, the prices of a cup of coffee, a cup of Milo and a glass of orange juice are RM2.00, RM2.60 and RM2.80 respectively.

$$5 \quad x + y + 2z = 260 \dots (1)$$

$$x + y + 4z = 340 \dots (2)$$

$$8x + 10y + 15z = 2\,200 \dots (3)$$

$$(2) - (1) : 2z = 80$$

$$z = 40$$

Substitute  $z = 40$  into (1) :

$$x + y + 2(40) = 260$$

$$x + y = 180 \dots (4)$$

Substitute  $z = 40$  into (3) :

$$8x + 10y + 15(40) = 2\,200$$

$$8x + 10y = 1\,600$$

$$4x + 5y = 800 \dots (5)$$

$$(4) \times 4 : 4x + 4y = 720 \dots (6)$$

$$(5) - (6) : y = 80$$

Substitute  $y = 80$  into (5) :

$$4x + 5(80) = 800$$

$$4x = 400$$

$$x = 100$$

Hence, the numbers of voice recorded model  $P$ ,  $Q$  and  $R$  are 100, 80 and 40 units respectively.

$$6 \quad 5x + 3y + 4z = 360 \dots (1)$$

$$x + y + 2z = 120 \dots (2)$$

$$6x + 4y + 5z = 450 \dots (3)$$

$$(2) \times 5 : 5x + 5y + 10z = 600 \dots (4)$$

$$(2) \times 6 : 6x + 6y + 12z = 720 \dots (5)$$

$$(4) - (1) : 2y + 6z = 240 \dots (6)$$

$$(5) - (3) : 2y + 7z = 270 \dots (7)$$

$$(7) - (6) : z = 30$$

Substitute  $z = 30$  into (7) :

$$2y + 7(30) = 270$$

$$2y = 60$$

$$y = 30$$

Substitute  $y = 30$  and  $z = 30$  into (1) :

$$5x + 3(30) + 4(30) = 360$$

$$5x = 150$$

$$x = 30$$

Hence, the number of nitrile, vinyl and surgical gloves produced are 30, 30 and 30 respectively.

7  $x + y + z = 240 \dots (1)$   
 $x + y = 3z \Rightarrow x + y - 3z = 0 \dots (2)$   
 $3x + 2y + 4z = 700 \dots (3)$

(1) - (2) :  
 $4z = 240$   
 $z = 60$

Substitute  $z = 60$  into (1) :  
 $x + y + 60 = 240$   
 $x + y = 180 \dots (4)$

Substitute  $z = 60$  into (3) :  
 $3x + 2y + 4(60) = 700$   
 $3x + 2y = 460 \dots (5)$

(4)  $\times 2$  :  $2x + 2y = 360 \dots (6)$

(5) - (6) :  $x = 100$

Substitute  $x = 100$  into (4) :  
 $100 + y = 180$   
 $y = 80$

Hence, the number of oranges, apples and pineapples sold are 100, 80 and 60 respectively.

8 (a)  $y - 2x = 7 \dots (1)$   
 $4x^2 + y^2 = 37 \dots (2)$   
 From (1) :  
 $y = 2x + 7 \dots (3)$

Substitute (3) into (2) :  
 $4x^2 + (2x + 7)^2 = 37$   
 $4x^2 + 4x^2 + 28x + 49 - 37 = 0$   
 $8x^2 + 28x + 12 = 0$   
 $4x^2 + 14x + 6 = 0$   
 $2x^2 + 7x + 3 = 0$   
 $(2x + 1)(x + 3) = 0$   
 $x = -\frac{1}{2}$  or  $x = -3$

From (3) :

When  $x = -\frac{1}{2}$ ,  $y = 2\left(-\frac{1}{2}\right) + 7 = 6$

When  $x = -3$ ,  $y = 2(-3) + 7 = 1$

(b)  $2x + y = 5 \dots (1)$   
 $x^2 - xy = 12 \dots (2)$

From (1) :

$y = 5 - 2x \dots (3)$

Substitute (3) into (2) :

$x^2 - x(5 - 2x) - 12 = 0$

$x^2 - 5x + 2x^2 - 12 = 0$

$3x^2 - 5x - 12 = 0$

$(x - 3)(3x + 4) = 0$

$x = 3$  or  $x = -\frac{4}{3}$

From (3) :

When  $x = 3$ ,  $y = 5 - 2(3) = -1$

When  $x = -\frac{4}{3}$ ,  $y = 5 - 2\left(-\frac{4}{3}\right) = \frac{23}{3}$

(c)  $3x - y = 7 \dots (1)$   
 $x^2 - xy + y^2 = 7 \dots (2)$

From (1) :

$y = 3x - 7 \dots (3)$

Substitute (3) into (2) :

$x^2 - x(3x - 7) + (3x - 7)^2 - 7 = 0$

$x^2 - 3x^2 + 7x + 9x^2 - 42x + 49 - 7 = 0$

$7x^2 - 35x + 42 = 0$

$x^2 - 5x + 6 = 0$

$(x - 3)(x - 2) = 0$

$x = 3$  or  $x = 2$

From (3) :

When  $x = 3$ ,  $y = 3(3) - 7 = 2$

When  $x = 2$ ,  $y = 3(2) - 7 = -1$

9 (a)  $2x + 3y = 7 \dots (1)$   
 $x^2 + y^2 = 7 - xy \dots (2)$

From (1) :

$y = \frac{7 - 2x}{3} \dots (3)$

Substitute (3) into (2) :

$x^2 + \left(\frac{7 - 2x}{3}\right)^2 - 7 + x\left(\frac{7 - 2x}{3}\right) = 0$

$x^2 + \left(\frac{49 - 28x + 4x^2}{9}\right) - 7 + x\left(\frac{7 - 2x}{3}\right) = 0$

$$9x^2 + 49 - 28x + 4x^2 - 63 + 3x(7 - 2x) = 0$$

$$9x^2 + 49 - 28x + 4x^2 - 63 + 21x - 6x^2 = 0$$

$$7x^2 - 7x - 14 = 0$$

$$x^2 - x - 2 = 0$$

$$(x - 2)(x + 1) = 0$$

$$x = 2 \text{ or } x = -1$$

From (3) :

$$\text{When } x = 2, y = \frac{7 - 2(2)}{3} = 1$$

$$\text{When } x = -1, y = \frac{7 - 2(-1)}{3} = 3$$

$$(b) \quad 2x + 3y = 1 \quad \dots (1)$$

$$3x^2 + 4xy - y^2 - 6 = 0 \quad \dots (2)$$

$$\text{From (1) : } y = \frac{1 - 2x}{3} \quad \dots (3)$$

Substitute (3) into (2) :

$$3x^2 + 4x\left(\frac{1 - 2x}{3}\right) - \left(\frac{1 - 2x}{3}\right)^2 - 6 = 0$$

$$3x^2 + 4x\left(\frac{1 - 2x}{3}\right) - \frac{1 - 4x + 4x^2}{9} - 6 = 0$$

$$27x^2 + 12x(1 - 2x) - (1 - 4x + 4x^2) - 54 = 0$$

$$27x^2 + 12x - 24x^2 - 1 + 4x - 4x^2 - 54 = 0$$

$$-x^2 + 16x - 55 = 0$$

$$x^2 - 16x + 55 = 0$$

$$(x - 5)(x - 11) = 0$$

$$x = 5 \text{ or } x = 11$$

From (3) :

$$\text{When } x = 5, y = \frac{1 - 2(5)}{3} = -3$$

$$\text{When } x = 11, y = \frac{1 - 2(11)}{3} = -7$$

$$10 \text{ (a)} \quad \frac{x}{3} + \frac{y}{4} = \frac{9}{2}$$

$$4x + 3y = 54$$

$$y = \frac{54 - 4x}{3} \quad \dots (1)$$

$$\frac{3}{x} + \frac{4}{y} = 1$$

$$3y + 4x = xy \quad \dots (2)$$

Substitute (1) into (2) :

$$3\left(\frac{54 - 4x}{3}\right) + 4x - x\left(\frac{54 - 4x}{3}\right) = 0$$

$$54 - 4x + 4x - x\left(\frac{54 - 4x}{3}\right) = 0$$

$$162 - x(54 - 4x) = 0$$

$$162 - 54x + 4x^2 = 0$$

$$2x^2 - 27x + 81 = 0$$

$$(x - 9)(2x - 9) = 0$$

$$x = 9 \text{ or } x = \frac{9}{2}$$

From (1) :

$$\text{When } x = 9, y = \frac{54 - 4(9)}{3} = 6$$

$$\text{When } x = \frac{9}{2}, y = \frac{54 - 4\left(\frac{9}{2}\right)}{3} = 12$$

$$(b) \quad \frac{2y}{3} - \frac{x}{2} = \frac{2}{3}$$

$$4y - 3x = 4$$

$$y = \frac{4 + 3x}{4} \quad \dots (1)$$

$$\frac{2}{x} + \frac{3}{y} = 3$$

$$2y + 3x = 3xy$$

$$2y + 3x - 3xy = 0 \quad \dots (2)$$

Substitute (1) into (2) :

$$2\left(\frac{4 + 3x}{4}\right) + 3x - 3x\left(\frac{4 + 3x}{4}\right) = 0$$

$$2(4 + 3x) + 12x - 3x(4 + 3x) = 0$$

$$8 + 6x + 12x - 12x - 9x^2 = 0$$

$$-9x^2 + 6x + 8 = 0$$

$$9x^2 - 6x - 8 = 0$$

$$(3x - 4)(3x + 2) = 0$$

$$x = \frac{4}{3} \text{ or } x = -\frac{2}{3}$$

From (1) :

$$\text{When } x = \frac{4}{3}, y = \frac{4 + 3\left(\frac{4}{3}\right)}{4} = 2$$

$$\text{When } x = -\frac{2}{3}, y = \frac{4 + 3\left(-\frac{2}{3}\right)}{4} = \frac{1}{2}$$

$$11 \text{ (a)} \quad 4y - 4x = 24$$

$$y - x = 6$$

$$y = x + 6 \quad \dots (1)$$

$$3x^2 + y^2 - 4y = 24 \quad \dots (2)$$

Substitute (1) into (2) :

$$3x^2 + (x + 6)^2 - 4(x + 6) - 24 = 0$$

$$3x^2 + x^2 + 12x + 36 - 4x - 24 - 24 = 0$$

$$4x^2 + 8x - 12 = 0$$

$$x^2 + 2x - 3 = 0$$

$$(x - 1)(x + 3) = 0$$

$$x=1 \text{ or } x=-3$$

From (1) :

When  $x=1$ ,  $y=1+6=7$

When  $x=-3$ ,  $y=-3+6=3$

(b)  $3(4x-3y)=45$

$$4x-3y=15$$

$$x = \frac{15+3y}{4} \dots (1)$$

$$8x^2 - 27y^2 = 45 \dots (2)$$

Substitute (1) into (2) :

$$8\left(\frac{15+3y}{4}\right)^2 - 27y^2 = 45$$

$$8\left(\frac{225+90y+9y^2}{16}\right) - 27y^2 - 45 = 0$$

$$\left(\frac{225+90y+9y^2}{2}\right) - 27y^2 - 45 = 0$$

$$225+90y+9y^2 - 54y^2 - 90 = 0$$

$$-45y^2 + 90y + 135 = 0$$

$$45y^2 - 90y - 135 = 0$$

$$9y^2 - 18y - 27 = 0$$

$$3y^2 - 6y - 9 = 0$$

$$y^2 - 2y - 3 = 0$$

$$(y-3)(y+1) = 0$$

$$y=3 \text{ or } y=-1$$

From (1) :

When  $y=3$ ,  $x = \frac{15+3(3)}{4} = 6$

When  $y=-1$ ,  $x = \frac{15+3(-1)}{4} = 3$

12  $Q=P$

$$-2y=3-x$$

$$x=3+2y \dots (1)$$

$$Q=R$$

$$-2y=x(5+9y)$$

$$-2y=5x+9xy$$

$$-2y-5x-9xy=0 \dots (2)$$

Substitute (1) into (2) :

$$-2y-5(2y+3)-9y(2y+3)=0$$

$$-2y-10y-15-18y^2-27y=0$$

$$-18y^2-39y-15=0$$

$$18y^2+39y+15=0$$

$$6y^2+13y+5=0$$

$$(3y+5)(2y+1)=0$$

$$y = -\frac{5}{3} \text{ or } -\frac{1}{2}$$

From (1) :

When  $y = -\frac{5}{3}$ ,  $x = 3 + 2\left(-\frac{5}{3}\right) = -\frac{1}{3}$

When  $y = -\frac{1}{2}$ ,  $x = 3 + 2\left(-\frac{1}{2}\right) = 2$

13  $y+2x=4$

$$3k+2(2h)=4$$

$$3k+4h=4$$

$$k = \frac{4-4h}{3} \dots (1)$$

$$\frac{2}{y} - \frac{3}{2x} = 1$$

$$\frac{2}{3k} - \frac{3}{2(2h)} = 1$$

$$\frac{8h-9k}{12hk} = 1$$

$$8h-9k=12hk \dots (2)$$

Substitute (1) into (2) :

$$9h-9\left(\frac{4-4h}{3}\right)=12h\left(\frac{4-4h}{3}\right)$$

$$8h-3(4-4h)=4h(4-4h)$$

$$8h-12+12h=16h-16h^2$$

$$16h^2+4h-12=0$$

$$4h^2+h-3=0$$

$$(4h-3)(h+1)=0$$

$$h = \frac{3}{4} \text{ or } -1$$

From (1) :

When  $h = \frac{3}{4}$ ,  $k = \frac{4-4\left(\frac{3}{4}\right)}{3} = \frac{1}{3}$

When  $h = -1$ ,  $k = \frac{4-4(-1)}{3} = \frac{8}{3}$

14  $x - \frac{1}{2}y = \frac{5}{2}$

$$2x - y = 5$$

$$y = 2x - 5 \dots (1)$$

$$2x + y = -\frac{2}{y}$$

$$2xy + y^2 = -2$$

$$2x(2x-5) + (2x-5)^2 + 2 = 0$$

$$4x^2 - 10x + 4x^2 - 20x + 25 + 2 = 0$$

$$8x^2 - 30x + 27 = 0$$

$$(4x-9)(2x-3) = 0$$

$$x = \frac{9}{4} \text{ or } x = \frac{3}{2}$$

From (1) :

$$\text{When } x = \frac{9}{4}, y = 2\left(\frac{9}{4}\right) - 5 = -\frac{1}{2}$$

$$\text{When } x = \frac{3}{2}, y = 2\left(\frac{3}{2}\right) - 5 = -2$$

**15**  $x - y = 1$

$$x = 1 + y \dots (1)$$

$$x^2 + 3y = 6 \dots (2)$$

Substitute (1) into (2) :

$$(1+y)^2 + 3y = 6$$

$$1 + 2y + y^2 + 3y - 6 = 0$$

$$y^2 + 5y - 5 = 0$$

$$y = \frac{-5 \pm \sqrt{5^2 - 4(1)(-5)}}{2(1)}$$

$$y = \frac{-5 \pm \sqrt{45}}{2(1)}$$

$$y = 0.854 \text{ or } -5.854$$

$$\text{When } y = 0.854, x = 1.854$$

$$\text{When } y = -5.854, x = -4.851$$

**16**  $3x + y + 4 = 0$

$$y = -3x - 4 \dots (1)$$

$$xy + 40 = y^2$$

$$x(-3x-4) + 40 - (-3x-4)^2 = 0$$

$$-3x^2 - 4x + 40 - (9x^2 + 24x + 16) = 0$$

$$-3x^2 - 4x + 40 - 9x^2 - 24x - 16 = 0$$

$$-12x^2 - 28x + 24 = 0$$

$$(x+3)(3x-2) = 0$$

$$x = -3 \text{ or } x = \frac{2}{3}$$

From (1) :

$$\text{When } x = -3, y = -3(-3) - 4 = 5$$

$$\text{When } x = \frac{2}{3}, y = -3\left(\frac{2}{3}\right) - 4 = -6$$

**17**  $m - 2n = -1$

$$m = 2n - 1 \dots (1)$$

$$mn + n - 3m = 0$$

$$n(2n-1) + n - 3(2n-1) = 0$$

$$2n^2 - n + n - 6n + 3 = 0$$

$$2n^2 - 6n + 3 = 0$$

$$n = \frac{6 \pm \sqrt{(-6)^2 - 4(2)(3)}}{2(2)}$$

$$n = \frac{6 \pm \sqrt{12}}{4}$$

$$n = 2.366 \text{ or } n = 0.634$$

From (1) :

$$\text{When } n = 2.366, m = 2(2.366) - 1 = 3.732$$

$$\text{When } n = 0.634, m = 2(0.634) - 1 = 0.268$$

**18** Perimeter = 42

$$10 + x + y + 30 - 3y + x = 42$$

$$2x - 2y - 2 = 0$$

$$x - y - 1 = 0$$

$$x = y + 1 \dots (1)$$

$$\text{Area} = 86 \text{ cm}^2$$

$$10x + (10 - y)^2 = 86$$

$$10x + 100 - 20y + y^2 - 86 = 0$$

$$10x + 14 - 20y + y^2 = 0$$

$$\text{Substitute } x = y + 1,$$

$$10(y+1) + 14 - 20y + y^2 = 0$$

$$10y + 10 + 14 - 20y + y^2 = 0$$

$$y^2 - 10y + 24 = 0$$

$$(y-6)(y-4) = 0$$

$$y = 6 \text{ or } y = 4$$

From (1) :

$$y = 6, x = 6 + 1 = 7$$

$$y = 4, x = 4 + 1 = 5$$

**19** Perimeter = 70 cm

$$5x + y + 12x + y + 13x = 70$$

$$30x + 2y = 70$$

$$15x + y = 35$$

$$y = 35 - 15x \dots (1)$$

$$\text{Area} = 240 \text{ cm}^2$$

$$\frac{1}{2} \times 12x \times 5x + 12xy = 240$$

$$30x^2 + 12xy = 240$$

$$10x^2 + 4xy = 80$$

$$5x^2 + 2xy = 40 \dots (2)$$

Substitute (1) into (2) :

$$5x^2 + 2x(35 - 15x) = 40$$

$$5x^2 + 70x - 30x^2 - 40 = 0$$

$$-25x^2 + 70x - 40 = 0$$

$$5x^2 - 14x + 8 = 0$$

$$(x-2)(5x-4) = 0$$

$$x = 2 \text{ or } x = \frac{4}{5}$$

From (1) :

When  $x = 2$ ,  $y = 35 - 15(2) = 5$

When  $x = \frac{4}{5}$ ,  $y = 35 - 15\left(\frac{4}{5}\right) = 23$

**20** Area = 28 cm<sup>2</sup>

$$7xy = 28$$

$$xy = 4 \dots (1)$$

$$\text{Perimeter} = 26 \text{ cm}$$

$$7x + y + y + \left(\frac{22}{7} \times \frac{7}{2}x\right) = 26$$

$$7x + 2y + 11x = 26$$

$$18x + 2y = 26$$

$$9x + y = 13$$

$$y = 13 - 9x \dots (2)$$

Substitute (2) into (1) :

$$x(13 - 9x) = 4$$

$$13x - 9x^2 = 4$$

$$9x^2 - 13x + 4 = 0$$

$$(x - 1)(9x - 4) = 0$$

$$x = 1 \text{ or } x = \frac{4}{9}$$

$$x = \frac{4}{9} \text{ is not accepted.}$$

$$\therefore x = 1$$

$$\text{From (2) : } y = 13 - 9(1) = 4$$

**21** Perimeter of fish pond = 48 m

$$2(x - 10) + 2(30 - y) = 48$$

$$x - 10 + 30 - y = 24$$

$$x - y = 4$$

$$y = x - 4 \dots (1)$$

Area of the region planted with papayas =

$$460 \text{ m}^2$$

$$(30 \times 10) + y(x - 10) = 460$$

$$-160 + xy - 10y = 0 \dots (2)$$

Substitute (1) into (2) :

$$-160 + x(x - 4) - 10(x - 4) = 0$$

$$-160 + x^2 - 4x - 10x + 40 = 0$$

$$x^2 - 14x - 120 = 0$$

$$(x - 20)(x + 6) = 0$$

$$x = 20 \text{ or } x = -6$$

$$x = -6 \text{ is not accepted.}$$

$$\text{Hence, } x = 20$$

$$\text{When } x = 20, y = 20 - 4 = 16$$

**22** Perimeter = 30

$$x + (x + y) + (2x + 3) = 30$$

$$4x + y = 27$$

$$y = 27 - 4x \dots (1)$$

Using the Pythagoras' Theorem,

$$x^2 + (x + y)^2 = (2x + 3)^2$$

$$x^2 + x^2 + 2xy + y^2 = 4x^2 + 12x + 9$$

$$2x^2 - 2xy - y^2 + 12x + 9 = 0 \dots (2)$$

$$2x^2 - 2x(27 - 4x) - (27 - 4x)^2 + 12x + 9 = 0$$

$$2x^2 - 54x + 8x^2 - (729 - 216x + 16x^2) + 12x + 9 = 0$$

$$-6x^2 + 174x - 720 = 0$$

$$6x^2 - 174x + 720 = 0$$

$$x^2 - 29x + 120 = 0$$

$$(x - 5)(x - 24) = 0$$

$$x = 5 \text{ or } x = 24$$

$x = 24$  is not accepted because it will make the value of  $y$  to be negative.

Hence,  $x = 5$ .

$$\text{From (1) : } y = 27 - 4(5) = 7$$

The lengths of the sides are  $x = 5$  m,  $(x + y) = 12$  m and  $(2x + 3) = 13$  m respectively.