

FORM 4

CHAPTER 2

Self Test 1

1 (Accept any correct answers)

Base	Examples
Three	$12_3, 202_3$
Five	$1234_5, 302_5$
Seven	$65_7, 431_7$

2

(a)	1011101_2	<table border="1"> <tr> <td>Number in base 2</td> <td>1</td> <td>0</td> <td><u>1</u></td> <td>1</td> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>2^6</td> <td>2^5</td> <td>2^4</td> <td>2^3</td> <td>2^2</td> <td>2^1</td> <td>2^0</td> </tr> </table>	Number in base 2	1	0	<u>1</u>	1	1	0	1	Place value	2^6	2^5	2^4	2^3	2^2	2^1	2^0	Place value $= 2^4$ $= 16$
Number in base 2	1	0	<u>1</u>	1	1	0	1												
Place value	2^6	2^5	2^4	2^3	2^2	2^1	2^0												
(b)	22112_3	<table border="1"> <tr> <td>Number in base 3</td> <td>2</td> <td><u>2</u></td> <td>1</td> <td>1</td> <td>2</td> </tr> <tr> <td>Place value</td> <td>3^4</td> <td>3^3</td> <td>3^2</td> <td>3^1</td> <td>3^0</td> </tr> </table>	Number in base 3	2	<u>2</u>	1	1	2	Place value	3^4	3^3	3^2	3^1	3^0	Place value $= 3^3$ $= 27$				
Number in base 3	2	<u>2</u>	1	1	2														
Place value	3^4	3^3	3^2	3^1	3^0														
(c)	3123021_4	<table border="1"> <tr> <td>Number in base 4</td> <td><u>3</u></td> <td>1</td> <td>2</td> <td>3</td> <td>0</td> <td>2</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>4^6</td> <td>4^5</td> <td>4^4</td> <td>4^3</td> <td>4^2</td> <td>4^1</td> <td>4^0</td> </tr> </table>	Number in base 4	<u>3</u>	1	2	3	0	2	1	Place value	4^6	4^5	4^4	4^3	4^2	4^1	4^0	Place value $= 4^6$ $= 4096$
Number in base 4	<u>3</u>	1	2	3	0	2	1												
Place value	4^6	4^5	4^4	4^3	4^2	4^1	4^0												
(d)	42331_5	<table border="1"> <tr> <td>Number in base 5</td> <td>4</td> <td>2</td> <td><u>3</u></td> <td>3</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>5^4</td> <td>5^3</td> <td>5^2</td> <td>5^1</td> <td>5^0</td> </tr> </table>	Number in base 5	4	2	<u>3</u>	3	1	Place value	5^4	5^3	5^2	5^1	5^0	Place value $= 5^2$ $= 25$				
Number in base 5	4	2	<u>3</u>	3	1														
Place value	5^4	5^3	5^2	5^1	5^0														
(e)	54321_6	<table border="1"> <tr> <td>Number in base 6</td> <td>5</td> <td><u>4</u></td> <td>3</td> <td>2</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>6^4</td> <td>6^3</td> <td>6^2</td> <td>6^1</td> <td>6^0</td> </tr> </table>	Number in base 6	5	<u>4</u>	3	2	1	Place value	6^4	6^3	6^2	6^1	6^0	Place value $= 6^3$ $= 216$				
Number in base 6	5	<u>4</u>	3	2	1														
Place value	6^4	6^3	6^2	6^1	6^0														
(f)	43025_7	<table border="1"> <tr> <td>Number in base 7</td> <td>4</td> <td><u>3</u></td> <td>0</td> <td>2</td> <td>5</td> </tr> <tr> <td>Place value</td> <td>7^4</td> <td>7^3</td> <td>7^2</td> <td>7^1</td> <td>7^0</td> </tr> </table>	Number in base 7	4	<u>3</u>	0	2	5	Place value	7^4	7^3	7^2	7^1	7^0	Place value $= 7^3$ $= 343$				
Number in base 7	4	<u>3</u>	0	2	5														
Place value	7^4	7^3	7^2	7^1	7^0														
(g)	14563_8	<table border="1"> <tr> <td>Number in base 8</td> <td>1</td> <td>4</td> <td>5</td> <td><u>6</u></td> <td>3</td> </tr> <tr> <td>Place value</td> <td>8^4</td> <td>8^3</td> <td>8^2</td> <td>8^1</td> <td>8^0</td> </tr> </table>	Number in base 8	1	4	5	<u>6</u>	3	Place value	8^4	8^3	8^2	8^1	8^0	Place value $= 8^1$ $= 8$				
Number in base 8	1	4	5	<u>6</u>	3														
Place value	8^4	8^3	8^2	8^1	8^0														
(h)	5763_9	<table border="1"> <tr> <td>Number in base 9</td> <td><u>5</u></td> <td>7</td> <td>6</td> <td>3</td> </tr> <tr> <td>Place value</td> <td>9^3</td> <td>9^2</td> <td>9^1</td> <td>9^0</td> </tr> </table>	Number in base 9	<u>5</u>	7	6	3	Place value	9^3	9^2	9^1	9^0	Place value $= 9^3$ $= 729$						
Number in base 9	<u>5</u>	7	6	3															
Place value	9^3	9^2	9^1	9^0															

3

(a)	10101_2	<table border="1"> <tr> <td>Number in base 2</td> <td><u>1</u></td> <td>0</td> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>2^4</td> <td>2^3</td> <td>2^2</td> <td>2^1</td> <td>2^0</td> </tr> </table>	Number in base 2	<u>1</u>	0	1	0	1	Place value	2^4	2^3	2^2	2^1	2^0	Digit value $= 1 \times 2^4$ $= 16$
Number in base 2	<u>1</u>	0	1	0	1										
Place value	2^4	2^3	2^2	2^1	2^0										
(b)	21211_3	<table border="1"> <tr> <td>Number in base 3</td> <td>2</td> <td>1</td> <td><u>2</u></td> <td>1</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>3^4</td> <td>3^3</td> <td>3^2</td> <td>3^1</td> <td>3^0</td> </tr> </table>	Number in base 3	2	1	<u>2</u>	1	1	Place value	3^4	3^3	3^2	3^1	3^0	Digit value $= 2 \times 3^2$ $= 18$
Number in base 3	2	1	<u>2</u>	1	1										
Place value	3^4	3^3	3^2	3^1	3^0										
(c)	33021_4	<table border="1"> <tr> <td>Number in base 4</td> <td>3</td> <td><u>3</u></td> <td>0</td> <td>2</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>4^4</td> <td>4^3</td> <td>4^2</td> <td>4^1</td> <td>4^0</td> </tr> </table>	Number in base 4	3	<u>3</u>	0	2	1	Place value	4^4	4^3	4^2	4^1	4^0	Digit value $= 3 \times 4^3$ $= 192$
Number in base 4	3	<u>3</u>	0	2	1										
Place value	4^4	4^3	4^2	4^1	4^0										
(d)	42431_5	<table border="1"> <tr> <td>Number in base 5</td> <td>4</td> <td>2</td> <td><u>4</u></td> <td>3</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>5^4</td> <td>5^3</td> <td>5^2</td> <td>5^1</td> <td>5^0</td> </tr> </table>	Number in base 5	4	2	<u>4</u>	3	1	Place value	5^4	5^3	5^2	5^1	5^0	Digit value $= 4 \times 5^2$ $= 100$
Number in base 5	4	2	<u>4</u>	3	1										
Place value	5^4	5^3	5^2	5^1	5^0										
(e)	53421_6	<table border="1"> <tr> <td>Number in base 6</td> <td>5</td> <td>3</td> <td><u>4</u></td> <td>2</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>6^4</td> <td>6^3</td> <td>6^2</td> <td>6^1</td> <td>6^0</td> </tr> </table>	Number in base 6	5	3	<u>4</u>	2	1	Place value	6^4	6^3	6^2	6^1	6^0	Digit value $= 4 \times 6^2$ $= 144$
Number in base 6	5	3	<u>4</u>	2	1										
Place value	6^4	6^3	6^2	6^1	6^0										
(f)	5623_7	<table border="1"> <tr> <td>Number in base 7</td> <td>5</td> <td><u>6</u></td> <td>2</td> <td>3</td> </tr> <tr> <td>Place value</td> <td>7^3</td> <td>7^2</td> <td>7^1</td> <td>7^0</td> </tr> </table>	Number in base 7	5	<u>6</u>	2	3	Place value	7^3	7^2	7^1	7^0	Digit value $= 6 \times 7^2$ $= 294$		
Number in base 7	5	<u>6</u>	2	3											
Place value	7^3	7^2	7^1	7^0											

(g)	40753_8	<table border="1"> <tr> <td>Number in base 8</td> <td>4</td> <td>0</td> <td>7</td> <td>5</td> <td>3</td> </tr> <tr> <td>Place value</td> <td>8^4</td> <td>8^3</td> <td>8^2</td> <td>8^1</td> <td>8^0</td> </tr> </table>	Number in base 8	4	0	7	5	3	Place value	8^4	8^3	8^2	8^1	8^0	Digit value = 0×8^3 = 0
Number in base 8	4	0	7	5	3										
Place value	8^4	8^3	8^2	8^1	8^0										
(h)	2473_9	<table border="1"> <tr> <td>Number in base 9</td> <td>2</td> <td>4</td> <td>7</td> <td>3</td> </tr> <tr> <td>Place value</td> <td>9^3</td> <td>9^2</td> <td>9^1</td> <td>9^0</td> </tr> </table>	Number in base 9	2	4	7	3	Place value	9^3	9^2	9^1	9^0	Digit value = 2×9^3 = 1 458		
Number in base 9	2	4	7	3											
Place value	9^3	9^2	9^1	9^0											

4

(a)	1101_2	<table border="1"> <tr> <td>Number in base 2</td> <td>1</td> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>2^3</td> <td>2^2</td> <td>2^1</td> <td>2^0</td> </tr> </table>	Number in base 2	1	1	0	1	Place value	2^3	2^2	2^1	2^0	Number value = $1(2^3) + 1(2^2) + 1(2^0)$ = $8 + 4 + 1$ = 13
Number in base 2	1	1	0	1									
Place value	2^3	2^2	2^1	2^0									
(b)	2012_3	<table border="1"> <tr> <td>Number in base 3</td> <td>2</td> <td>0</td> <td>1</td> <td>2</td> </tr> <tr> <td>Place value</td> <td>3^3</td> <td>3^2</td> <td>3^1</td> <td>3^0</td> </tr> </table>	Number in base 3	2	0	1	2	Place value	3^3	3^2	3^1	3^0	Number value = $2(3^3) + 1(3^1) + 2(3^0)$ = $54 + 3 + 2$ = 59
Number in base 3	2	0	1	2									
Place value	3^3	3^2	3^1	3^0									
(c)	321_4	<table border="1"> <tr> <td>Number in base 4</td> <td>3</td> <td>2</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>4^2</td> <td>4^1</td> <td>4^0</td> </tr> </table>	Number in base 4	3	2	1	Place value	4^2	4^1	4^0	Number value = $3(4^2) + 2(4^1) + 1(4^0)$ = $48 + 8 + 1$ = 57		
Number in base 4	3	2	1										
Place value	4^2	4^1	4^0										
(d)	4221_5	<table border="1"> <tr> <td>Number in base 5</td> <td>4</td> <td>2</td> <td>2</td> <td>1</td> </tr> <tr> <td>Place value</td> <td>5^3</td> <td>5^2</td> <td>5^1</td> <td>5^0</td> </tr> </table>	Number in base 5	4	2	2	1	Place value	5^3	5^2	5^1	5^0	Number value = $4(5^3) + 2(5^2) + 2(5^1) + 1(5^0)$ = $500 + 50 + 10 + 1$ = 561
Number in base 5	4	2	2	1									
Place value	5^3	5^2	5^1	5^0									
(e)	4352_6	<table border="1"> <tr> <td>Number in base 6</td> <td>4</td> <td>3</td> <td>5</td> <td>2</td> </tr> <tr> <td>Place value</td> <td>6^3</td> <td>6^2</td> <td>6^1</td> <td>6^0</td> </tr> </table>	Number in base 6	4	3	5	2	Place value	6^3	6^2	6^1	6^0	Number value = $4(6^3) + 3(6^2) + 5(6^1) + 2(6^0)$ = $864 + 108 + 30 + 2$ = 1 004
Number in base 6	4	3	5	2									
Place value	6^3	6^2	6^1	6^0									
(f)	2563_7	<table border="1"> <tr> <td>Number in base 7</td> <td>2</td> <td>5</td> <td>6</td> <td>3</td> </tr> <tr> <td>Place value</td> <td>7^3</td> <td>7^2</td> <td>7^1</td> <td>7^0</td> </tr> </table>	Number in base 7	2	5	6	3	Place value	7^3	7^2	7^1	7^0	Number value = $2(7^3) + 5(7^2) + 6(7^1) + 3(7^0)$ = $686 + 245 + 42 + 3$ = 976
Number in base 7	2	5	6	3									
Place value	7^3	7^2	7^1	7^0									
(g)	745_8	<table border="1"> <tr> <td>Number in base 8</td> <td>7</td> <td>4</td> <td>5</td> </tr> <tr> <td>Place value</td> <td>8^2</td> <td>8^1</td> <td>8^0</td> </tr> </table>	Number in base 8	7	4	5	Place value	8^2	8^1	8^0	Number value = $7(8^2) + 4(8^1) + 5(8^0)$ = $448 + 32 + 5$ = 485		
Number in base 8	7	4	5										
Place value	8^2	8^1	8^0										
(h)	3845_9	<table border="1"> <tr> <td>Number in base 9</td> <td>3</td> <td>8</td> <td>4</td> <td>5</td> </tr> <tr> <td>Place value</td> <td>9^3</td> <td>9^2</td> <td>9^1</td> <td>9^0</td> </tr> </table>	Number in base 9	3	8	4	5	Place value	9^3	9^2	9^1	9^0	Number value = $3(9^3) + 8(9^2) + 4(9^1) + 5(9^0)$ = $2 187 + 648 + 36 + 5$ = 2 876
Number in base 9	3	8	4	5									
Place value	9^3	9^2	9^1	9^0									

5 (a) $2101_3 = (2 \times 3^p) + (1 \times 3^2) + (1 \times 3^q)$

Number in base 3	2	1	0	1
Place value	3^3	3^2	3^1	3^0

therefore, $p = 3$, $q = 0$

(b) $3241_5 = (3 \times 5^3) + (2 \times 5^p) + (q \times 5) + 1$

Number in base 5	3	2	4	1
Place value	5^3	5^2	5^1	5^0

therefore, $p = 2$, $q = 4$

(c) $5324_7 = (5 \times 7^p) + (3 \times q) + (2 \times 7) + (4 \times 7^0)$

Number in base 7	5	3	2	4
Place value	7^3	7^2	7^1	7^0

therefore, $p = 3$, $q = 49$

6 $6(6^4 + 36 + 3) = 6^5 + 6(6^2) + 3(6^0)$
= $1(6^5) + 0(6^4) + 1(6^3) + 0(6^2) + 3(6^1) + 0(6^0)$
= 101030_6

7 $6(9^1) + 6(7^3) = 54 + 2 058$
= 2 112

8 (a)
$$\begin{array}{r} 3 \overline{)156} \\ 3 \underline{52} \dots 0 \\ 3 \underline{17} \dots 1 \\ 3 \underline{5} \dots 2 \\ 3 \underline{1} \dots 2 \\ 0 \dots 1 \end{array}$$

$156_{10} = 12210_3$

(c)
$$\begin{array}{r} 6 \overline{)156} \\ 6 \underline{26} \dots 0 \\ 6 \underline{4} \dots 2 \\ 0 \dots 4 \end{array}$$

$156_{10} = 420_6$

(e)
$$\begin{array}{r} 8 \overline{)156} \\ 8 \underline{19} \dots 4 \\ 8 \underline{2} \dots 3 \\ 0 \dots 2 \end{array}$$

$156_{10} = 234_8$

9 (a) 113_5 (base three)
= $1(5^2) + 1(5^1) + 3(5^0)$
= 33_{10}
= 1020_3

(b)
$$\begin{array}{r} 4 \overline{)156} \\ 4 \underline{39} \dots 0 \\ 4 \underline{9} \dots 3 \\ 4 \underline{2} \dots 1 \\ 0 \dots 2 \end{array}$$

$156_{10} = 2130_4$

(d)
$$\begin{array}{r} 7 \overline{)156} \\ 7 \underline{22} \dots 2 \\ 7 \underline{3} \dots 1 \\ 0 \dots 3 \end{array}$$

$156_{10} = 312_7$

(f)
$$\begin{array}{r} 9 \overline{)156} \\ 9 \underline{17} \dots 3 \\ 9 \underline{1} \dots 8 \\ 0 \dots 1 \end{array}$$

$156_{10} = 183_9$

$$\begin{array}{r} 3 \overline{)33} \\ 3 \underline{11} \dots 0 \\ 3 \underline{3} \dots 2 \\ 3 \underline{1} \dots 0 \\ 0 \dots 1 \end{array}$$

(b) 3521_6 (base four)
 $= 3(6^3) + 5(6^2) + 2(6^1) + 1(6^0)$
 $= 841_{10}$
 $= 31021_4$

$$\begin{array}{r} 4 \overline{) 841} \\ \underline{4 \ 210} \dots 1 \\ 4 \ \underline{52} \dots 2 \\ 4 \ \underline{13} \dots 0 \\ 4 \ \underline{3} \dots 1 \\ 0 \dots 3 \end{array}$$

(c) 67_8 (base five)
 $= 6(8^1) + 7(8^0)$
 $= 55_{10}$
 $= 210_5$

(d) 1110111_2 (base seven)
 $= 1(2^6) + 1(2^5) + 1(2^4) + 0(2^3) + 1(2^2) + 1(2^1) + 1(2^0)$
 $= 119_{10}$
 $= 230_7$

(e) 21112_3 (base eight)
 $= 2(3^4) + 1(3^3) + 1(3^2) + 1(3^1) + 2(3^0)$
 $= 203_{10}$
 $= 313_8$

$$\begin{array}{r} 8 \overline{) 203} \\ \underline{8 \ 25} \dots 3 \\ 8 \ \underline{3} \dots 1 \\ 0 \dots 3 \end{array}$$

(f) 3212302_4 (base nine)
 $= 3(4^6) + 2(4^5) + 1(4^4) + 2(4^3) + 3(4^2) + 0(4^1) + 2(4^0)$
 $= 14\ 770_{10}$
 $= 22231_9$

10 (a) 1101101_2

Number in base 2	1	1	0	1	1	0	1
Place value	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Digit value	1	4 + 1 = 5		4 + 1 = 5			
Number in base 8	155 ₈						

(b) 1011101_2

Number in base 2	1	0	1	1	1	0	1
Place value	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Digit value	1	2 + 1 = 3		4 + 1 = 5			
Number in base 8	135 ₈						

(c) 10011101_2

Number in base 2	1	0	0	1	1	1	0	1
Place value	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Digit value	2 + 0 = 2	2 + 1 = 3		4 + 1 = 5				
Number in base 8	235 ₈							

(d) 1111111_2

Number in base 2	1	1	1	1	1	1	1
Place value	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Digit value	1	4 + 2 + 1 = 7		4 + 2 + 1 = 7			
Number in base 8	177 ₈						

(e) 11111001_2

Number in base 2	1	1	1	1	1	0	0	1
Place value	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Digit value	2 + 1 = 3	4 + 2 + 1 = 7		1				
Number in base 8	371 ₈							

(f) 101011_2

Number in base 2	1	0	1	0	1	1
Place value	2^2	2^1	2^0	2^2	2^1	2^0
Digit value	4 + 1 = 5		2 + 1 = 3			
Number in base 8	53 ₈					

11 (a) 175_8

Base 8	1			7			5		
	0 + 0 + 1			4 + 2 + 1			4 + 0 + 1		
Place value	2^2	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Base 2	0	0	1	1	1	1	1	0	1
	1111101 ₂								

(b) 31_8

Base 8	3			1		
	0 + 2 + 1			0 + 0 + 1		
Place value	2^2	2^1	2^0	2^2	2^1	2^0
Base 2	0	1	1	0	0	1
	11001 ₂					

(c) 462_8

Base 8	4			6			2		
	4 + 0 + 0			4 + 2 + 0			0 + 2 + 0		
Place value	2^2	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Base 2	1	0	0	1	1	0	0	1	0
	100110010 ₂								

(d) 564_8

Base 8	5			6			4		
	4 + 0 + 1			4 + 2 + 0			4 + 0 + 0		
Place value	2^2	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Base 2	1	0	1	1	1	0	1	0	0
	101110100 ₂								

(e) 2734_8

Base 8	2			7			3			4		
	0 + 2 + 0			4 + 2 + 1			0 + 2 + 1			4 + 0 + 0		
Place value	2^2	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Base 2	0	1	0	1	1	1	0	1	1	1	0	0
	10111011100 ₂											

(f) 125_8

Base 8	1			2			5		
	0 + 0 + 1			0 + 2 + 0			4 + 0 + 1		
Place value	2^2	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Base 2	0	0	1	0	1	0	1	0	1
	1010101 ₂								

12 (a) $10101_2 + 11101_2 = 110010_2$ (b) $211_3 + 102_3 = 1020_3$

$$\begin{array}{r} \\ 1 \ 0 \ 1 \ 0 \ 1_2 \\ + 1 \ 1 \ 1 \ 0 \ 1_2 \\ \hline 1 \ 1 \ 0 \ 0 \ 1 \ 0_2 \end{array}$$

$$\begin{array}{r} \\ 2 \ 1 \ 1_3 \\ + 1 \ 0 \ 2_3 \\ \hline 1 \ 0 \ 2 \ 0_3 \end{array}$$

(c) $1302_4 + 2113_4 = 10021_4$ (d) $2341_5 + 304_5 = 3200_5$

$$\begin{array}{r} \\ 1 \ 3 \ 0 \ 2_4 \\ + 2 \ 1 \ 1 \ 3_4 \\ \hline 1 \ 0 \ 0 \ 2 \ 1_4 \end{array}$$

$$\begin{array}{r} \\ 2 \ 3 \ 4 \ 1_5 \\ + 3 \ 0 \ 4_5 \\ \hline 3 \ 2 \ 0 \ 0_5 \end{array}$$

(e) $5134_6 + 245_6 = 5423_6$ (f) $454_7 + 365_7 = 1152_7$

$$\begin{array}{r} 5 \overset{1}{1} 3 \overset{1}{4}_6 \\ + 2 \overset{1}{4} 5_6 \\ \hline 5 \overset{1}{4} 2 \overset{1}{3}_6 \end{array}$$

$$\begin{array}{r} 4 \overset{1}{5} 4_7 \\ + 3 \overset{1}{6} 5_7 \\ \hline 1 \overset{1}{1} 5 \overset{1}{2}_7 \end{array}$$

(g) $6125_8 + 357_8 = 6504_8$ (h) $286_9 + 254_9 = 551_9$

$$\begin{array}{r} 6 \overset{1}{1} 2 \overset{1}{5}_8 \\ + 3 \overset{1}{5} 7_8 \\ \hline 6 \overset{1}{5} 0 \overset{1}{4}_8 \end{array}$$

$$\begin{array}{r} 2 \overset{1}{8} 6_9 \\ + 2 \overset{1}{5} 4_9 \\ \hline 5 \overset{1}{5} 1_9 \end{array}$$

13 (a) $110101_2 - 11101_2 = 11000_2$ (b) $1221_3 - 112_3 = 1102_3$

$$\begin{array}{r} \overset{2}{0} \overset{2}{1} \overset{2}{1} 0 \overset{2}{1} 0 \overset{2}{1} 2 \\ - \overset{2}{1} \overset{2}{1} \overset{2}{1} 0 \overset{2}{1} 2 \\ \hline 1 \overset{2}{1} 0 \overset{2}{0} 0 \overset{2}{0} 2 \end{array}$$

$$\begin{array}{r} 1 \overset{4}{2} \overset{4}{2} \overset{4}{1} 3 \\ - 1 \overset{4}{1} 2_3 \\ \hline 1 \overset{4}{1} 0 \overset{4}{2} 3 \end{array}$$

(c) $2312_4 - 213_4 = 2033_4$ (d) $4321_5 - 1324_5 = 2442_5$

$$\begin{array}{r} 2 \overset{4}{2} \overset{4}{3} \overset{4}{1} 2_4 \\ - 2 \overset{4}{1} 3_4 \\ \hline 2 \overset{4}{0} 3 \overset{4}{3} 4 \end{array}$$

$$\begin{array}{r} 4 \overset{6}{3} \overset{6}{2} \overset{6}{1} 3_5 \\ - 1 \overset{6}{3} 2 \overset{6}{4} 5 \\ \hline 2 \overset{6}{4} 4 \overset{6}{2} 5 \end{array}$$

(e) $5341_6 - 3254_6 = 2043_6$ (f) $654_7 - 266_7 = 355_7$

$$\begin{array}{r} 5 \overset{7}{3} \overset{7}{4} \overset{7}{1} 6 \\ - 3 \overset{7}{2} 5 \overset{7}{4}_6 \\ \hline 2 \overset{7}{0} 4 \overset{7}{3} 6 \end{array}$$

$$\begin{array}{r} 6 \overset{11}{5} \overset{11}{4} 7 \\ - 2 \overset{11}{6} 6_7 \\ \hline 3 \overset{11}{5} 5_7 \end{array}$$

(g) $654_8 - 367_8 = 265_8$ (h) $758_9 - 364_9 = 384_9$

$$\begin{array}{r} 6 \overset{12}{5} \overset{12}{4} 8 \\ - 3 \overset{12}{6} 7_8 \\ \hline 2 \overset{12}{6} 5_8 \end{array}$$

$$\begin{array}{r} 7 \overset{14}{6} \overset{14}{5} 8_9 \\ - 3 \overset{14}{6} 4_9 \\ \hline 3 \overset{14}{8} 4_9 \end{array}$$

14 Let $z =$ Zakiah's age this year

Kim's age this year $= 2(5^1) + 1(5^0)$
 $= 11_{10}$

$$\left. \begin{array}{l} 11_2 = 1(2^1) + 1(2^0) \\ = 3_{10} \\ 22_3 = 2(3^1) + 2(3^0) \\ = 8_{10} \end{array} \right\} \begin{array}{l} \text{Zakiah's age is 3 times Kim's} \\ \text{age 8 years ago} \end{array}$$

Therefore, $z - 8 = 3(11 - 8)$
 $z = 3(3) + 8$
 $= 17$

Zakiah's age 50₆ years later
 $= 17 + [5(6^1) + 0(6^0)]$
 $= 17 + 30$
 $= 47$

15 $483_9 = 4(9^2) + 8(9^1) + 3(9^0)$

$= 399_{10}$
 $543_7 = 5(7^2) + 4(7^1) + 3(7^0)$
 $= 276_{10}$

$1211_3 = 1(3^3) + 2(3^2) + 1(3^1) + 1(3^0)$
 $= 49_{10}$

Remaining stamps $= 483_9 - 543_7 - 1211_3$
 $= 399 - 276 - 49$
 $= 74_{10}$
 $= 244_5$

$$\begin{array}{r} 5 \overline{) 74} \\ 5 \overline{) 14} \dots 4 \uparrow \\ 5 \overline{) 2} \dots 4 \uparrow \\ 0 \dots 2 \uparrow \end{array}$$

16 Price of television $= \text{RM}20140_8$
 $= \text{RM}2(8^4) + 1(8^2) + 4(8^1)$
 $= \text{RM}8288$
 Total discount $= \text{RM}(8288 - 5801.60)$
 $= \text{RM}2486.40$

Percentage of discount $= \frac{\text{RM}2486.40}{\text{RM}8288} \times 100\%$
 $= 30\%$
 $= 11110_2\%$

$$\begin{array}{r} 2 \overline{) 30} \\ 2 \overline{) 15} \dots 0 \uparrow \\ 2 \overline{) 7} \dots 1 \uparrow \\ 2 \overline{) 3} \dots 1 \uparrow \\ 2 \overline{) 1} \dots 1 \uparrow \\ 0 \dots 1 \uparrow \end{array}$$

SPM PRACTICE

Paper 1

1 D

Place value	7^4	7^3	7^2	7^1	7^0
Number in base 7	1	0	0	3	0

2 B $10110_2 + 111_2 = 11101_2$

$$\begin{array}{r} 1 \overset{1}{0} \overset{1}{1} 1 \overset{1}{0} 2 \\ + 1 \overset{1}{1} 1_2 \\ \hline 1 \overset{1}{1} 1 \overset{1}{0} 1_2 \end{array}$$

3 C $1001110011_2 = 2363_8$

Number in base 2	1	0	0	1	1	1	1	0	0	1	1
Place value	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0	2^2	2^1	2^0
Digit value	$2 + 0$ $= 2$	$2 + 1$ $= 3$	$4 + 2 + 0$ $= 6$	$2 + 1$ $= 3$							
Number in base 8	2363_8										

4 C $p = x^2$ $q = x^1$ $r = x^0$

$2x^2 + x + 2(x^0) = 23$
 $2x^2 + x + 2 - 23 = 0$
 $2x^2 + x - 21 = 0$
 $(2x + 7)(x - 3) = 0$
 $x = 3$ (negative value is rejected)

Therefore, $p + q - r = 3^2 + 3^1 - 3^0$
 $= 11$

5 C Digit value of 2 $= 2 \times 6^2$

$= 72$

6 B $(3 \times 4^3) + (2 \times 4^2) + 4x = 3220_4$

Place value	4^3	4^2	4^1	4^0
Number in base 7	3	2	x	0

$x = 2$

7 B Digits in the number base 5 are 0, 1, 2, 3 and 4.

8 C $4(6^2) - 4(8) = 112$

9 D $463_8 + 57_8 = 542_8$

$$\begin{array}{r} 4 \overset{1}{6} 3_8 \\ + 5 \overset{1}{7}_8 \\ \hline 5 \overset{1}{4} 2_8 \end{array}$$

10 A Encik Alif's savings in Bank A $= \text{RM}43562_9$

$= \text{RM}[4(9^4) + 3(9^3) + 5(9^2) + 6(9^1) + 2(9^0)]$
 $= \text{RM}(26\,244 + 2\,187 + 405 + 54 + 2)$
 $= \text{RM}28\,892$

Encik Alif's savings in Bank B $= \text{RM}25413_6$

$= \text{RM}[2(6^4) + 5(6^3) + 4(6^2) + 1(6^1) + 3(6^0)]$
 $= \text{RM}(2\,592 + 1\,080 + 144 + 6 + 3)$
 $= \text{RM}3\,825$

Total savings
 $= \text{RM}(28\,892 + 3\,825)$
 $= \text{RM}32\,717$

Total down payment
 $= 10\% \times \text{RM}485\,600$
 $= \text{RM}48\,560$

Amount of money still needed

$$= \text{RM}(48\,560 - 32\,717)$$

$$= \text{RM}15\,843$$

11 A $3412_5 - 34_5 = 3323_5$

$$\begin{array}{r} 3412_5 \\ - 34_5 \\ \hline 3323_5 \end{array}$$

12 C

$$\begin{aligned} 4k5_6 &= 326_7 \\ 4(6^2) + k(6^1) + 5(6^0) &= 3(7^2) + 2(7^1) + 6(7^0) \\ 144 + 6k + 5 &= 147 + 14 + 6 \\ 6k &= 18 \\ k &= 3 \end{aligned}$$

13 D

$$\begin{aligned} 70_9 &= 7(9^1) + 0(9^0) \\ &= 63 \\ 230_5 &= 2(5^2) + 3(5^1) + 0(5^0) \\ &= 65 \end{aligned}$$

14 C

$$\begin{aligned} 52024_8 &= 5(8^4) + 2(8^3) + 0(8^2) + 2(8^1) + 4(8^0) \\ &= 20\,480 + 1\,024 + 16 + 4 \\ &= 21\,524 \\ 2240453_6 &= 2(6^6) + 2(6^5) + 4(6^4) + 0(6^3) + 4(6^2) + 5(6^1) + 3(6^0) \\ &= 93\,312 + 15\,552 + 5\,184 + 144 + 30 + 3 \\ &= 114\,225 \\ 52024_8 + 2240453_6 &= 21\,524 + 114\,225 \\ &= 135\,749 \end{aligned}$$

15 B

$$1513_6 = 1(6^3) + 5(6^2) + 1(6^1) + 3(6^0) = 405$$

$$p\% = \frac{450 - 405}{450} \times 100\% = 10\% = 22_4$$

Paper 2

Section A

1 $4400_5 - 3041_5 = 1304_5$

$$\begin{aligned} &= 1(5^3) + 3(5^2) + 0(5^1) + 4(5^0) \\ &= 125 + 75 + 4 \\ &= 204 \\ &= 411_7 \end{aligned}$$

$$M = 411$$

$$\begin{array}{r} 4400_5 \\ - 3041_5 \\ \hline 1304_5 \end{array}$$

2 $123_4 = 1(4^2) + 2(4^1) + 3(4^0)$

$$= 16 + 8 + 3 = 27$$

$$26_7 = 2(7^1) + 6(7^0)$$

$$= 14 + 6 = 20$$

$$34_5 = 3(5^1) + 4(5^0)$$

$$= 15 + 4 = 19$$

$$47_8 = 4(8^1) + 7(8^0)$$

$$= 32 + 7 = 39$$

Arrangement in descending: $47_8, 123_4, 26_7, 34_5$

3 Total digit value of '2' = $2(3^2) + 2(8^2) + 2(6^3)$

$$= 18 + 128 + 432 = 578$$

4 Given that $431_p = 102010_3 - 312_5$

$$4p^2 + 3p + 1p^0 = 1(3^5) + 2(3^4) + 1(3^3) - [3(5^2) + 1(5^1) + 2(5^0)]$$

$$4p^2 + 3p + 1 = 243 + 54 + 3 - [75 + 5 + 2]$$

$$4p^2 + 3p - 217 = 0$$

$$(4p + 31)(p - 7) = 0$$

$$p = 7 \text{ (negative value of } p \text{ is rejected)}$$

5 (a) $\frac{228^\circ}{360^\circ} \times 90 = 57 = 212_5$

$$\begin{array}{r} 5 \overline{) 57} \\ \underline{50} \\ 7 \\ \underline{5} \\ 2 \\ \underline{0} \\ 2 \end{array}$$

(b) Number of students who prefer rambutans = $\frac{56^\circ}{360^\circ} \times 90 = 14$

Number of students who prefer bananas = $\frac{40^\circ}{360^\circ} \times 90 = 10$

Number of students who prefer mangoes = $90 - 57 - 14 - 10 = 9$

Difference in the number of students who prefer rambutans and mangoes = $14 - 9 = 5_{10} = 12_3$

Section B

6 (a) Banana flavour: $100000_2 = 2^5 = 32$

Orange flavour: $110_4 = 1(4^2) + 1(4^1) = 20$

Chocolate flavour: $143_5 = 1(5^2) + 4(5^1) + 3(5^0) = 48$

Banana : Orange : Chocolate = $32 : 20 : 48 = 8 : 5 : 12$

(b) New total of banana cupcakes = $32 + 8 = 40$

Banana : Orange : Chocolate = $8 : 5 : 12$
 $\times 5 \times 5 \times 5$
 $= 40 : 25 : 60$

Additional number of orange cupcakes needed

$$= 25 - 20 = 5 = 12_3$$

Additional number of chocolate cupcakes needed

$$= 60 - 48 = 12 = 110_3$$

7 (a) Area of trapezium = 4301_5

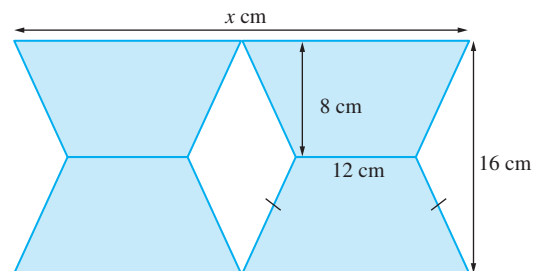
$$4 \times \frac{1}{2} \times \left(12 + \frac{x}{2}\right)(8) = 4(5^3) + 3(5^2) + 0(5^1) + 1(5^0)$$

$$16\left(12 + \frac{x}{2}\right) = 500 + 75 + 1$$

$$192 + 8x = 576$$

$$8x = 384$$

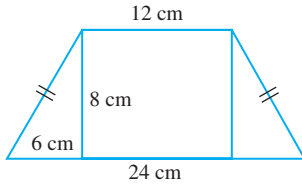
$$x = 48$$



(b) Length of hypotenuse of triangle formed in the trapezium

$$= \sqrt{8^2 + 6^2}$$

$$= 10 \text{ cm}$$



Perimeter of the shaded region

$$= 2(48) + 8(10)$$

$$= 176 \text{ cm}$$

$$= 260_8 \text{ cm}$$

$$\begin{array}{r} 8 \overline{) 176} \\ 8 \overline{) 22} \dots 0 \\ 8 \overline{) 2} \dots 6 \\ \underline{0} \dots 2 \end{array}$$

Section C

8 Radius = $1(2^2) + 1(2^1) + 1(2^0)$

$$= 4 + 2 + 1$$

$$= 7 \text{ cm}$$

(a) Slanting height = $\sqrt{7^2 + 10^2}$

$$= 12.21 \text{ cm}$$

(b) Volume = Volume of cone + volume of hemisphere

$$= \frac{1}{3} \left(\frac{22}{7} \right) (7^2) (10) + \left(\frac{2}{3} \right) \left(\frac{22}{7} \right) (7^3)$$

$$= 513 \frac{1}{3} + 718 \frac{2}{3}$$

$$= 1\,232 \text{ cm}^3$$

$$= 1618_9 \text{ cm}^3$$

$$\begin{array}{r} 9 \overline{) 1232} \\ 9 \overline{) 136} \dots 8 \\ 9 \overline{) 15} \dots 1 \\ 9 \overline{) 1} \dots 6 \\ \underline{0} \dots 1 \end{array}$$

(c) Total surface area of hemisphere = $2 \left(\frac{22}{7} \right) (7^2)$

$$= 308 \text{ cm}^2$$

$$= 464_8 \text{ cm}^2$$

$$\begin{array}{r} 8 \overline{) 308} \\ 8 \overline{) 38} \dots 4 \\ 8 \overline{) 4} \dots 6 \\ \underline{0} \dots 4 \end{array}$$

(d) Price of a can of paint = RM1(2²)

$$= \text{RM}4$$

$$308 \div 100 = 3.08$$

Number of cans = 4

Amount of money needed = $4 \times \text{RM}4$

$$= \text{RM}16$$