

# Penyelesaian Lengkap

## PENTAKSIRAN SUMATIF

### Kertas 1

- 1 (a) Bukan fungsi. Objek 5 mempunyai dua imej, 2 dan 6.

*Not a function. Object 5 has two images, 2 and 6.*

(b) (i)  $g(x) = 3x + p$   
 $g^2(x) = 3(3x + p) + p$   
 $= 9x + 3p + p$   
 $= 9x + 4p$

Diberi/Given,  $g^2(x) = qx - 20$

Dengan perbandingan,

*By comparison,*

$q = 9,$        $4p = -20$   
 $p = -5$

(ii)  $g(x) = 3x - 5$

$g^{-1}(x) = \frac{x+5}{3}$

$g^{-1}(7) = \frac{7+5}{3}$   
 $= 4$

(iii)  $g^2(x) = 9x - 20$   
 $g^2[g^2(x)] = 9(9x - 20) - 20$   
 $g^4(3) = 9[9(3) - 20] - 20$   
 $= 9(7) - 20$   
 $= 63 - 20$   
 $= 43$

2 (a)  $f(x) = \frac{1}{2}x + n$

Biar/Let  $f(x) = y$

$y = \frac{1}{2}x + n$

$2y = x + 2n$

$x = 2y - 2n$

$\therefore f^{-1}(x) = 2x - 2n$

Diberi/Given  $f^{-1}(x) = px - 12$

Dengan perbandingan/By comparison,

$p = 2,$        $-2n = -12$   
 $n = 6$

(b)  $f(x) = \frac{1}{2}x + 6$

$f[g(x)] = \frac{1}{2}g(x) + 6$

Diberi/Given  $fg(x) = 4x - 7$

$\frac{1}{2}g(x) + 6 = 4x - 7$

$\frac{1}{2}g(x) = 4x - 13$

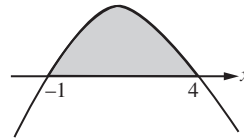
$g(x) = 8x - 26$

3 (a)  $2x + 5 \geq x^2 - x + 1$

$2x + 5 - x^2 + x - 1 \geq 0$

$-x^2 + 3x + 4 \geq 0$

$(-x-1)(x-4) \geq 0$



Daripada graf/From the graph,

$-1 \leq x \leq 4$

(b)  $hx^2 + (h-2)x + 4 = x - h + 7$

$hx^2 + hx - 2x + 4 - x + h - 7 = 0$

$hx^2 + hx - 3x + 4 + h - 7 = 0$

$hx^2 + (h-3)x + h-3 = 0$

$a = h, b = h-3, c = h-3$

$b^2 - 4ac = 0$

$(h-3)^2 - 4(h)(h-3) = 0$

$(h-3)[(h-3) - 4h] = 0$

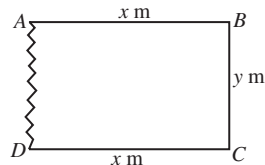
$(h-3)(-3-3h) = 0$

$-3(h-3)(1+h) = 0$

$h-3 = 0, 1+h = 0$

$h = 3, h = -1$

4



(a) Katakan/Let  $BC = y$  m

Panjang pagar/Length of fence,

$x + y + x = 52$

$y + 2x = 52$

$y = 52 - 2x \dots \textcircled{1}$

$A = xy \dots \textcircled{2}$

Gantikan  $\textcircled{1}$  ke dalam  $\textcircled{2}$ ,

Substitute  $\textcircled{1}$  into  $\textcircled{2}$ ,

$A = x(52 - 2x)$

$= 52x - 2x^2$

$= -2[x^2 - 26x]$

$= -2\left[x^2 - 26x + \left(-\frac{26}{2}\right)^2 - \left(-\frac{26}{2}\right)^2\right]$

$= -2[x^2 - 26x + (-13)^2 - (-13)^2]$

$= -2[(x-13)^2 - 169]$

$= -2(x-13)^2 + 338$  [Tertunjuk/Shown]

(b)  $p = -2$

(c) Nilai maksimum  $= q = 338$

Maka, luas maksimum tanah ialah  $338 \text{ m}^2$ .

Maximum value =  $q = 338$   
 Thus, the maximum area of the land is  $338 \text{ m}^2$ .

$$5 \quad 2x + v = x - \frac{4}{x}$$

$$2x^2 + vx = x^2 - 4$$

$$x^2 + vx + 4 = 0$$

$$a = 1, b = v, c = 4$$

$$b^2 - 4ac = 0$$

$$v^2 - 4(1)(4) = 0$$

$$(v + 4)(v - 4) = 0$$

$$v + 4 = 0, v - 4 = 0$$

$$v = -4, v = 4$$

$$6 \text{ (a)} \quad \frac{\sqrt{3} + \sqrt{2}}{\sqrt{3} - \sqrt{2}} = \frac{\sqrt{3} + \sqrt{2}}{\sqrt{3} - \sqrt{2}} \times \frac{\sqrt{3} + \sqrt{2}}{\sqrt{3} + \sqrt{2}}$$

$$= \frac{(\sqrt{3})^2 + \sqrt{6} + \sqrt{6} + (\sqrt{2})^2}{(\sqrt{3})^2 - (\sqrt{2})^2}$$

$$= \frac{3 + 2\sqrt{6} + 2}{3 - 2}$$

$$= 5 + 2\sqrt{6}$$

$$\therefore m = 5, n = 2$$

$$6 \text{ (b)} \quad F = P \times (1 - r)^n$$

$$800 = 1\,200 \times \left(1 - \frac{5}{100}\right)^n$$

$$800 = 1\,200 \times 0.95^n$$

$$0.95^n = 0.6667$$

$$n \log_{10} 0.95 = \log_{10} 0.6667$$

$$n(-0.02228) = -0.1761$$

$$n = 7.904$$

$$n \approx 8$$

Bilangan tikus akan kurang daripada 800 ekor dalam 8 tahun.

The number of mice will be less than 800 in 8 years.

$$7 \text{ (a)} \quad 3^x = 30 - 3^x$$

$$3^x + 3^x = 30$$

$$2(3^x) = 30$$

$$3^x = 15$$

$$\log_{10} 3^x = \log_{10} 15$$

$$x \log_{10} 3 = \log_{10} 15$$

$$x = \frac{\log_{10} 15}{\log_{10} 3}$$

$$x = 2.465$$

$$7 \text{ (b)} \quad \ln \sqrt[5]{en} + \ln \frac{e}{\sqrt[5]{n}}$$

$$= \frac{1}{5} \ln en + (\ln e - \ln \sqrt[5]{n})$$

$$= \frac{1}{5} (\ln e + \ln n) + \ln e - \frac{1}{5} \ln n$$

$$= \frac{1}{5} \log_e e + \frac{1}{5} \log_e n + \log_e e - \frac{1}{5} \log_e n$$

$$= \frac{1}{5} (1) + \frac{1}{5} (n) + 1 - \frac{1}{5} (n)$$

$$= \frac{1}{5} + 1$$

$$= \frac{6}{5}$$

8 Luas  $\Delta ABC + \text{Luas } \Delta ADC = 59$   
 Area of  $\Delta ABC + \text{Area of } \Delta ADC = 59$

$$\frac{1}{2} \times x \times y + \frac{1}{2} (x + 2)(y - 1) = 59$$

$$xy + (x + 2)(y - 1) = 118$$

$$xy + (xy - x + 2y - 2) = 118$$

$$2xy - x + 2y = 120 \dots \textcircled{1}$$

Dengan menggunakan teorem Pythagoras,

By using Pythagoras' theorem,

bagi for  $\Delta ABC, AC^2 = x^2 + y^2$

bagi for  $\Delta ADC, AC^2 = (x + 2)^2 + (y - 1)^2$

$$(x + 2)^2 + (y - 1)^2 = x^2 + y^2$$

$$x^2 + 4x + 4 + y^2 - 2y + 1 = x^2 + y^2$$

$$2y - 4x = 5$$

$$y = \frac{1}{2}(4x + 5) \dots \textcircled{2}$$

Gantikan  $\textcircled{2}$  ke dalam  $\textcircled{1}$ ,

Substitute  $\textcircled{2}$  into  $\textcircled{1}$ ,

$$2x \left[ \frac{1}{2}(4x + 5) \right] - x + 2 \left[ \frac{1}{2}(4x + 5) \right] = 120$$

$$x(4x + 5) - x + 4x + 5 = 120$$

$$4x^2 + 5x - x + 4x + 5 - 120 = 0$$

$$4x^2 + 8x - 115 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-8 \pm \sqrt{(8)^2 - 4(4)(-115)}}{2(4)}$$

$$= \frac{-8 \pm \sqrt{1\,904}}{8}$$

$$x = -6.454, x = 4.454$$

Oleh sebab/Since  $x > 0, \therefore x = 4.454$

Apabila/When  $x = 4.454,$

$$y = \frac{1}{2}[4(4.454) + 5] = 11.408$$

9  $m + 3n + p = 3 \dots \textcircled{1}$

$3m - n + 2p = 11 \dots \textcircled{2}$

$m - n - p = -1 \dots \textcircled{3}$

$$\textcircled{1} - \textcircled{3}: 4n + 2p = 4$$

$$2n + p = 2 \dots \textcircled{4}$$

$$\textcircled{1} \times 3 - \textcircled{2}: 10n + p = -2 \dots \textcircled{5}$$

Daripada/From  $\textcircled{4},$

$$p = 2 - 2n \dots \textcircled{6}$$

Gantikan  $\textcircled{6}$  ke dalam  $\textcircled{5},$

Substitute  $\textcircled{6}$  into  $\textcircled{5},$

$$10n + (2 - 2n) = -2$$

$$8n = -4$$

$$n = -\frac{1}{2}$$

Daripada/From  $\textcircled{6},$

$$p = 2 - 2\left(-\frac{1}{2}\right)$$

$$p = 3$$

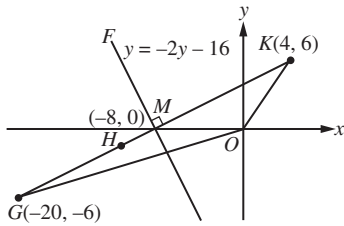
Daripada/From  $\textcircled{1},$

$$m + 3\left(-\frac{1}{2}\right) + 3 = 3$$

$$m = \frac{3}{2}$$

$$\therefore m = \frac{3}{2}, n = -\frac{1}{2}, p = 3$$

10



$$\begin{aligned} \text{(a) } m_{GK} &= \frac{6 - (-6)}{4 - (-20)} \\ &= \frac{12}{24} \\ &= \frac{1}{2} \end{aligned}$$

$$\begin{aligned} m_{GK} \times m_{FM} &= -1 \\ \therefore m_{FM} &= -2 \end{aligned}$$

Titik tengah/Midpoint,  $M$

$$\begin{aligned} &= \left( \frac{-20 + 4}{2}, \frac{-6 + 6}{2} \right) \\ &= (-8, 0) \end{aligned}$$

Persamaan pembahagi dua sama serenjang  $GK$ :  
Equation of the perpendicular bisector of  $GK$ :

$$\begin{aligned} \frac{y-0}{x-(-8)} &= -2 \\ y &= -2(x+8) \\ y &= -2x-16 \end{aligned}$$

(b) Koordinat titik  $H$

Coordinates of point  $H$

$$\begin{aligned} &= \left( \frac{2(-20) + 1(4)}{1+2}, \frac{2(-6) + 1(6)}{1+2} \right) \\ &= (-12, -2) \end{aligned}$$

(c) Katakan  $h$  ialah jarak terdekat dari  $O$  ke  $GK$ .

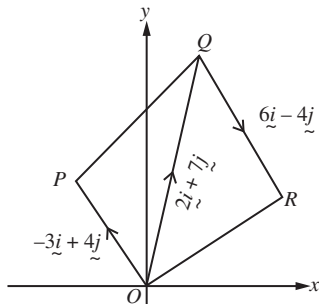
Let  $h$  be shortest distance from  $O$  to  $GK$ .

$$\frac{1}{2} \times 12\sqrt{5} \times h = 48$$

$$h = \frac{48}{6\sqrt{5}}$$

$$h = \frac{8}{\sqrt{5}} \text{ unit/units}$$

11



$$\begin{aligned} \text{(a) (i) } \vec{PQ} &= \vec{OQ} - \vec{OP} \\ &= (2\hat{i} + 7\hat{j}) - (-3\hat{i} + 4\hat{j}) \\ &= 2\hat{i} + 7\hat{j} + 3\hat{i} - 4\hat{j} \\ &= 5\hat{i} + 3\hat{j} \end{aligned}$$

$$\begin{aligned} \text{(ii) } \vec{OR} &= \vec{OQ} + \vec{QR} \\ &= (2\hat{i} + 7\hat{j}) + (6\hat{i} - 4\hat{j}) \\ &= 8\hat{i} + 3\hat{j} \\ \therefore R(8, 3) \end{aligned}$$

(b) Diberi  $\underline{u}$  dan  $\underline{w}$  adalah selari, maka  $\underline{u} = \lambda \underline{w}$  dengan keadaan  $\lambda$  ialah pemalar.

Given  $\underline{u}$  and  $\underline{w}$  are parallel, then  $\underline{u} = \lambda \underline{w}$  where  $\lambda$  is a constant.

$$4\hat{i} + (3h-2)\hat{j} = \lambda(6\hat{i} + 2\hat{j})$$

$$4\hat{i} + (3h-2)\hat{j} = 6\lambda\hat{i} + 2\lambda\hat{j}$$

Bandingkan pekali bagi  $\hat{i}$ .

Compare coefficients of  $\hat{i}$ .

$$6\lambda = 4$$

$$\lambda = \frac{2}{3}$$

Bandingkan pekali bagi  $\hat{j}$ .

Compare coefficients of  $\hat{j}$ .

$$3h-2 = 2\lambda$$

$$3h-2 = 2\left(\frac{2}{3}\right)$$

$$3h-2 = \frac{4}{3}$$

$$3h = \frac{10}{3}$$

$$h = \frac{10}{9}$$

$$12 \quad y = \frac{u^x}{d}$$

$$\log_e y = \log_e \frac{u^x}{d}$$

$$\ln y = \ln u^x - \ln d$$

$$\ln y = (\ln u)x - \ln d \dots \textcircled{1}$$

$$m = \frac{12-4}{2-6} = -\frac{8}{4} = -2$$

$$\ln y = -2x + c$$

Pada/At  $F(2, 12)$ ,

$$12 = -2(2) + c$$

$$c = 16$$

$$\ln y = -2x + 16$$

Daripada/From  $\textcircled{1}$ ,

$$-\ln d = 16$$

$$\ln d = -16$$

$$d = e^{-16}$$

$$\ln u = -2$$

$$u = e^{-2}$$

$$u = \frac{1}{e^2}$$

$$\begin{aligned} \text{13 (a) (i) } d &= T_2 - T_1 = T_3 - T_2 \\ 10 - (p-1) &= 2p - 10 \\ 10 - p + 1 &= 2p - 10 \end{aligned}$$

$$\begin{aligned} -3p &= -21 \\ p &= 7 \end{aligned}$$

(ii) Tiga sebutan yang pertama:

*The first three terms:*

$$7 - 1, 10, 2(7)$$

$$6, 10, 14$$

$$a = 6, d = 10 - 6 = 4$$

Hasil tambah dari sebutan ke-10 hingga  
sebutan ke-20

*Sum of the 10<sup>th</sup> term to the 20<sup>th</sup> term*

$$= S_{20} - S_9$$

$$= \frac{20}{2}[2(6) + (20-1)(4)] - \frac{9}{2}[2(6) + (9-1)(4)]$$

$$= 880 - 198$$

$$= 682$$

(b) (i)  $T_1 + T_2 = 20$

$$a + ar = 20 \dots \textcircled{1}$$

$$T_5 = 9T_3$$

$$ar^4 = 9 \times ar^2$$

$$ar^4 - 9ar^2 = 0$$

$$ar^2(r^2 - 9) = 0$$

$$(r+3)(r-3) = 0$$

$$r = -3, r = 3$$

Oleh sebab  $r > 0$ , maka  $r = 3$

Since  $r > 0$ , thus  $r = 3$

Daripada/From  $\textcircled{1}$ ,

$$a + a(3) = 20$$

$$4a = 20$$

$$a = 5$$

$$(ii) S_n = \frac{a(r^n - 1)}{r - 1}$$

$$S_7 = \frac{5(3^7 - 1)}{3 - 1}$$

$$= 5465$$

14 (a)  $EF : HF = 3 : 1 \Rightarrow EH : HF = 2 : 1$

Koordinat H/Coordinates of H

$$= \left( \frac{1(-4) + 2(14)}{2+1}, \frac{1(2) + 2(8)}{2+1} \right)$$

$$= (8, 6)$$

$$(b) m_{EF} = \frac{8-2}{14-(-4)} = \frac{1}{3}$$

$$m_{EF} \times m_{GH} = -1$$

$$\therefore m_{GH} = -3$$

Persamaan garis GH:

*Equation of GH:*

$$y = mx + c$$

$$6 = (-3)(8) + c$$

$$c = 30$$

$$y = -3x + 30 \dots \textcircled{1}$$

Diberi persamaan EG:

*Given the equation of EG:*

$$y = 2x + 5 \dots \textcircled{2}$$

$$\textcircled{1} = \textcircled{2}:$$

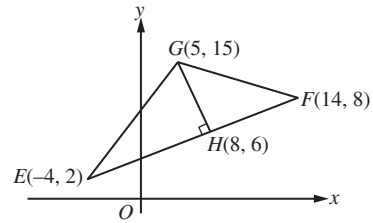
$$2x + 5 = -3x + 30$$

$$5x = 25$$

$$x = 5$$

$$y = 2(5) + 5 = 15$$

$$\therefore G(5, 15)$$



(c) Luas/Area of  $\triangle EHG$

$$= \frac{1}{2} \begin{vmatrix} -4 & 8 & 5 & -4 \\ 2 & 6 & 15 & 2 \end{vmatrix}$$

$$= \frac{1}{2} [( -4)(6) + (8)(15) + (5)(2) ] - [(2)(8) + (6)(5) + (15)(-4)]$$

$$= \frac{1}{2} |106 - (-14)|$$

$$= \frac{1}{2}(120)$$

$$= 60 \text{ unit/units}$$

15 (a)  $T_1 + T_2 + T_3 + T_4 = 60$

$$a + (a+4) + (a+8) + (a+12) = 60$$

$$4a + 24 = 60$$

$$4a = 36$$

$$a = 9$$

(b) (i)  $S_n = 1365$  cm,  $a = 195$  cm,  $n = 13$  cm

$$S_n = \frac{n}{2}[2a + (n-1)d]$$

$$1365 = \frac{13}{2}[2(195) + (13-1)d]$$

$$210 = 390 + 12d$$

$$12d = -180$$

$$d = -15$$

Tiga bahagian tali yang pertama:

*The first three parts of the string:*

195 cm,  $(195 - 15)$  cm,  $(195 - 15 - 15)$  cm

195 cm, 180 cm, 165 cm

(ii)  $T_n = a + (n-1)d$

$$= 195 + (n-1)(-15)$$

$$= 195 - 15n + 15$$

$$= 210 - 15n$$

Panjang bahagian ke- $n$  tali itu ialah

$(210 - 15n)$  cm.

*The length of the  $n^{\text{th}}$  part of the string is*

$(210 - 15n)$  cm.

(iii)  $T_{13} = 210 - 15(13) = 15$

$$T_{12} = 210 - 15(12) = 30$$

$$T_{11} = 210 - 15(11) = 45$$

$$T_{10} = 210 - 15(10) = 60$$

Hasil tambah panjang empat bahagian tali yang terakhir

*Sum of the length of the last four parts of the string*

$$= 15 + 30 + 45 + 60$$

$$= 150 \text{ cm}$$

## Kertas 2

1  $x - y = 2 \dots \textcircled{1}$

$$\frac{4}{x} + \frac{1}{y} = 3 \dots \textcircled{2}$$

Daripada/From  $\textcircled{1}$ ,

$$x = y + 2 \dots \textcircled{3}$$

$$\textcircled{2} \times (xy),$$

$$\frac{4}{x}(xy) + \frac{1}{y}(xy) = 3(xy)$$

$$4y + x = 3xy \dots \textcircled{4}$$

Gantikan  $\textcircled{3}$  ke dalam  $\textcircled{4}$ ,

Substitute  $\textcircled{3}$  into  $\textcircled{4}$ ,

$$4y + (y + 2) = 3y(y + 2)$$

$$4y + y + 2 = 3y^2 + 6y$$

$$3y^2 + 6y - 4y - y - 2 = 0$$

$$3y^2 + y - 2 = 0$$

$$(y + 1)(3y - 2) = 0$$

$$y + 1 = 0, 3y - 2 = 0$$

$$y = -1, \quad y = \frac{2}{3}$$

Apabila/When  $y = -1$ ,

$$x = (-1) + 2 = 1$$

Apabila/When  $y = \frac{2}{3}$ ,

$$x = \left(\frac{2}{3}\right) + 2 = \frac{8}{3}$$

$$\therefore x = -1, y = 1 \text{ dan/and } x = \frac{8}{3}, y = \frac{2}{3}$$

2 Bilangan tiket dewasa yang dijual =  $x$

Number of adult tickets sold =  $x$

Bilangan tiket pelajar yang dijual =  $y$

Number of student tickets sold =  $y$

Bilangan tiket kanak-kanak =  $z$

Number of children tickets sold =  $z$

$$40x + 20y + 10z = 16\,400 \dots \textcircled{1}$$

$$x + y + z = 700 \dots \textcircled{2}$$

$$(x + y) - z = 460 \dots \textcircled{3}$$

$$\textcircled{2} - \textcircled{3}: 2z = 240$$

$$z = 120$$

Daripada/From  $\textcircled{1}$ ,

$$40x + 20y + 10(120) = 16\,400$$

$$40x + 20y = 15\,200 \dots \textcircled{3}$$

Daripada/From  $\textcircled{2}$ ,

$$x + y + 120 = 700$$

$$x + y = 580 \dots \textcircled{4}$$

Daripada/From  $\textcircled{4}$ ,

$$y = 580 - x \dots \textcircled{5}$$

Gantikan  $\textcircled{5}$  ke dalam  $\textcircled{3}$ ,

Substitute  $\textcircled{5}$  into  $\textcircled{3}$ ,

$$40x + 20(580 - x) = 15\,200$$

$$40x + 11\,600 - 20x = 15\,200$$

$$20x = 3\,600$$

$$x = 180$$

Daripada/From  $\textcircled{4}$ ,

$$y = 580 - (180) = 400$$

3 (a)  $r = \frac{1}{2}(4) = 2$

$$T_1 = \pi(2)^2(3.5) = 14\pi$$

$$T_2 = \pi(2)^2(6) = 24\pi$$

$$T_3 = \pi(2)^2(8.5) = 34\pi$$

$$T_2 - T_1 = 24\pi - 14\pi = 10\pi$$

$$T_3 - T_2 = 34\pi - 24\pi = 10\pi$$

Maka, isi padu silinder mengikut satu jangjang aritmetik dengan beza sepunya,  $d = 10\pi \text{ cm}^3$ .

Thus, the volume of the cylinders follows an arithmetic progression with common difference,  $d = 10\pi \text{ cm}^3$ .

(b)  $T_n = a + (n - 1)d$

$$T_{13} = (14\pi) + (13 - 1)(10\pi)$$

$$= 14\pi + 120\pi$$

$$= 134\pi \text{ cm}^3$$

(c)  $S_n = \frac{n}{2}[2a + (n - 1)d]$

$$1\,598\pi = \frac{n}{2}[2(14) + (n - 1)(10)]$$

$$1\,598 = n[2(7) + (n - 1)(5)]$$

$$1\,598 = n(14 + 5n - 5)$$

$$1\,598 = n(9 + 5n)$$

$$1\,598 = 5n^2 + 9n$$

$$5n^2 + 9n - 1\,598 = 0$$

$$(5n + 94)(n - 17) = 0$$

$$n = -\frac{94}{5}, \quad n = 17$$

Oleh sebab/Since  $n > 0$ ,  $\therefore n = 17$

4 (a)  $NQ : PQ = 4 : 1 \Rightarrow NP : PQ = 3 : 1$

Katakan/Let  $Q(h, k)$

$$8 = \frac{1(-4) + 3(h)}{3 + 1} \qquad 6 = \frac{1(3) + 3(k)}{3 + 1}$$

$$32 = -4 + 3h \qquad 24 = 3 + 3k$$

$$36 = 3h \qquad 21 = 3k$$

$$h = 12 \qquad k = 7$$

$$\therefore Q(12, 7)$$

(b)  $m_{NQ} = \frac{6 - 3}{8 - (-4)} = \frac{3}{12} = \frac{1}{4}$

$$m_{PT} = -\frac{1}{m_{NQ}} = -4$$

Persamaan garis lurus  $PT$ :

Equation of straight line  $PT$ :

$$y - 6 = -4(x - 8)$$

$$y - 6 = -4x + 32$$

$$y = -4x + 38$$

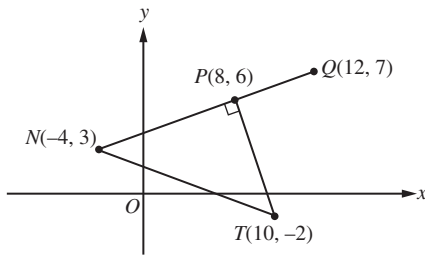
Pada/At  $T(u, -2)$ ,

$$-2 = -4(u) + 38$$

$$4u = 40$$

$$u = 10$$

(c)

Luas/Area of  $\triangle NPT$ 

$$= \frac{1}{2} \begin{vmatrix} -4 & 10 & 8 & -4 \\ 3 & -2 & 6 & 3 \end{vmatrix}$$

$$= \frac{1}{2} [(-4)(-2) + (10)(6) + (8)(3) - [(3)(10) + (-2)(8) + (6)(-4)]]$$

$$= \frac{1}{2} [(92) - (-10)]$$

$$= \frac{1}{2} (102)$$

$$= 51 \text{ unit}^2/\text{units}^2$$

5 (a) Katakan/Let  $y = \log_a b$ 

$$a^y = b$$

$$\log_x a^y = \log_x b$$

$$y \log_x a = \log_x b$$

$$y = \frac{\log_x b}{\log_x a}$$

$$\log_a b = \frac{\log_x b}{\log_x a} \quad [\text{Tertunjuk/Shown}]$$

$$\log_8 32 = \frac{\log_2 32}{\log_2 8}$$

$$= \frac{\log_2 2^5}{\log_2 2^3}$$

$$= \frac{5}{3}$$

$$(b) \quad 2^x - 3 = 4 - \frac{12}{2^x}$$

$$2^x - 7 + \frac{12}{2^x} = 0$$

$$(2^x)2^x - 7(2^x) + 12 = 0$$

$$2^{2x} - 7(2^x) + 12 = 0$$

$$(2^x - 3)(2^x - 4) = 0$$

$$2^x = 3, 2^x = 4$$

Apabila/When  $2^x = 3$ ,

$$\log_{10} 2^x = \log_{10} 3$$

$$x = \frac{\log_{10} 3}{\log_{10} 2} = 1.585$$

Apabila/When  $2^x = 4$ ,

$$2x = 2^2$$

$$x = 2$$

$$\begin{aligned} 6 \text{ (a) } f(x) &= 6 + 5x - 2x^2 \\ &= -2x^2 + 5x + 6 \\ &= -2 \left[ x^2 - \frac{5}{2}x - \frac{6}{2} \right] \\ &= -2 \left[ x^2 - \frac{5}{2}x - 3 \right] \end{aligned}$$

$$= -2 \left[ x^2 - \frac{5}{2}x + \left( -\frac{5}{4} \right)^2 - \left( -\frac{5}{4} \right)^2 - 3 \right]$$

$$= -2 \left[ \left( x - \frac{5}{4} \right)^2 - \frac{25}{16} - 3 \right]$$

$$= -2 \left[ \left( x - \frac{5}{4} \right)^2 - \frac{73}{16} \right]$$

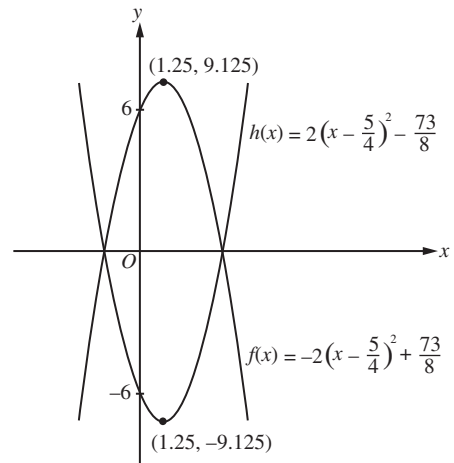
$$= -2 \left( x - \frac{5}{4} \right)^2 + \frac{73}{8}$$

$$\text{Nilai maksimum} = \frac{73}{8}$$

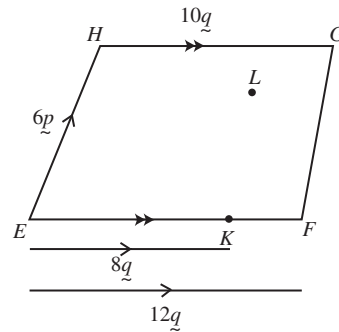
$$\text{Maximum value} = \frac{73}{8}$$

$$(b) \quad h(x) = 2 \left( x - \frac{5}{4} \right)^2 - \frac{73}{8}$$

(c)



7



$$(a) \quad \vec{EG} = \vec{EH} + \vec{HG}$$

$$\vec{EG} = \vec{EH} + \frac{5}{6}\vec{EF}$$

$$\vec{EG} = 6\vec{p} + \frac{5}{6}(12\vec{q})$$

$$= 6\vec{p} + 10\vec{q}$$

$$(b) \text{ (i) } 2\vec{KL} = \beta\vec{EH}$$

$$2\vec{KL} = \beta(6\vec{p})$$

$$\vec{KL} = 3\beta\vec{p}$$

$$\vec{EL} = \vec{EK} + \vec{KL}$$

$$= \frac{2}{3}\vec{EF} + \vec{KL}$$

$$= \frac{2}{3}(12\underline{q}) + 3\underline{\beta p}$$

$$= 3\underline{\beta p} + 8\underline{q}$$

(ii)  $\vec{EL} = \lambda \vec{EG}$

$$3\underline{\beta p} + 8\underline{q} = \lambda(6\underline{p} + 10\underline{q})$$

$$3\underline{\beta p} + 8\underline{q} = 6\lambda\underline{p} + 10\lambda\underline{q}$$

Bandungkan pekali bagi  $\underline{q}$ ,  
Compare coefficients of  $\underline{q}$ ,

$$10\lambda = 8$$

$$\lambda = \frac{4}{5}$$

Bandungkan pekali bagi  $\underline{p}$ ,  
Compare coefficients of  $\underline{p}$ ,

$$3\underline{\beta} = 6\lambda$$

$$3\underline{\beta} = 6\left(\frac{4}{5}\right)$$

$$3\underline{\beta} = \frac{24}{5}$$

$$\underline{\beta} = \frac{8}{5}$$

8 (a)  $5^m \times \frac{25^n}{5} = 1$

$$5^m \times \frac{(5^2)^n}{5} = 5^0$$

$$5^m \times 5^{2n-1} = 5^0$$

$$m + 2n - 1 = 0$$

$$m = 1 - 2n \dots \textcircled{1}$$

$$\log_3 6 - \log_3 (m - n) = 1$$

$$\log_3 6 - \frac{\log_3 (m - n)}{\log_3 3^2} = 1$$

$$\log_3 6 - \frac{\log_3 (m - n)}{2} = 1$$

$$2 \log_3 6 - \log_3 (m - n) = 2$$

$$\log_3 6^2 - \log_3 (m - n) = 2$$

$$\log_3 36 - \log_3 (m - n) = 2$$

$$\log_3 \frac{36}{(m - n)} = 2$$

$$\frac{36}{(m - n)} = 3^2$$

$$9(m - n) = 36$$

$$m - n = 4 \dots \textcircled{2}$$

Gantikan  $\textcircled{1}$  ke dalam  $\textcircled{2}$ ,

Substitute  $\textcircled{1}$  into  $\textcircled{2}$ ,

$$(1 - 2n) - n = 4$$

$$3n = -3$$

$$n = -1$$

Daripada/From  $\textcircled{1}$ ,

$$m = 1 - 2(-1)$$

$$= 3$$

(b)  $\frac{3^x}{3^{2y}} = 9 \Rightarrow 3^{x-2y} = 3^2$

$$\therefore x - 2y = 2 \dots \textcircled{1}$$

$$\log_y (x - 3) = 2$$

$$\therefore x - 3 = y^2 \dots \textcircled{2}$$

Daripada/From  $\textcircled{1}$ ,  $x = 2y + 2 \dots \textcircled{3}$

Gantikan  $\textcircled{3}$  ke dalam  $\textcircled{2}$ ,

Substitute  $\textcircled{3}$  into  $\textcircled{2}$ ,

$$(2y + 2) - 3 = y^2$$

$$2y - 1 = y^2$$

$$y^2 - 2y + 1 = 0$$

$$(y - 1)^2 = 0$$

$$y = 1$$

Daripada/From  $\textcircled{3}$ ,

$$x = 2(1) + 2$$

$$= 4$$

$$\therefore x = 4, y = 1$$

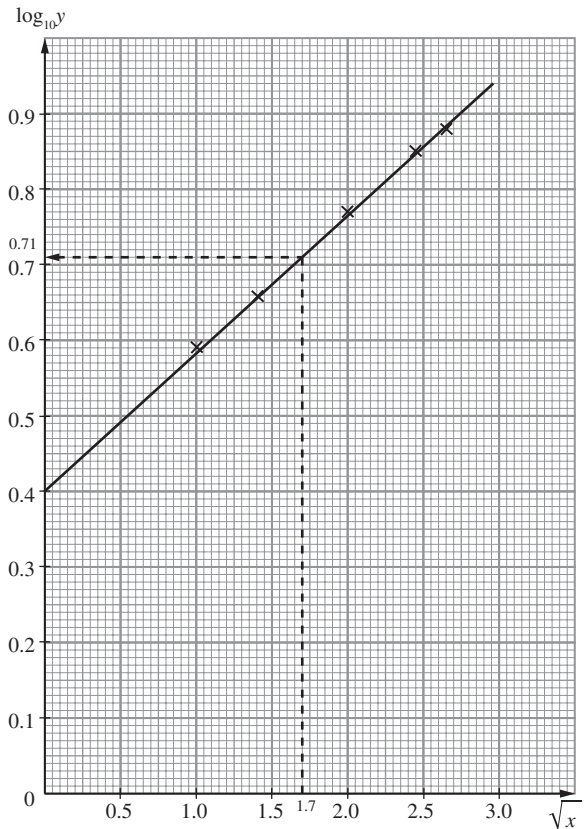
9 (a)  $y = pq^{\sqrt{x}}$

$$\log_{10} y = \log_{10} pq^{\sqrt{x}}$$

$$\log_{10} y = \log_{10} p + \sqrt{x} \log_{10} q$$

$$\log_{10} y = (\log_{10} q) \sqrt{x} + \log_{10} p$$

$\sqrt{x}$	1	1.41	2	2.45	2.65
$\log_{10} y$	0.59	0.66	0.77	0.85	0.88



(b) (i) Daripada graf,

From the graph,

$$\log_{10} p = 0.4$$

$$p = 2.512$$

(ii) Kecerunan/Gradient

$$= \frac{0.88 - 0.4}{2.65 - 0}$$

$$\log_{10} q = 0.1811$$

$$q = 1.517$$

(iii) Apabila/When  $x = 3$ ,

$$\sqrt{x} = 1.732$$

$$\log_{10} y = 0.71$$

$$y = 5.129$$

10 (a)  $m_{EF} = \frac{6-0}{9-(-3)} = \frac{1}{2}$

$$m_{EF} \times m_{FG} = -1, \therefore m_{FG} = -2$$

Persamaan FG:

Equation of FG:

$$y - 6 = -2(x - 9)$$

$$y - 6 = -2x + 18$$

$$y = -2x + 24$$

(b)  $y = -2x + 24 \dots \textcircled{1}$

$$4x - 3y + 12 = 0 \dots \textcircled{2}$$

Gantikan  $\textcircled{1}$  ke dalam  $\textcircled{2}$ ,

Substitute  $\textcircled{1}$  into  $\textcircled{2}$ ,

$$4x - 3(-2x + 24) + 12 = 0$$

$$4x + 6x - 72 + 12 = 0$$

$$10x - 60 = 0$$

$$x = 6$$

Daripada/From  $\textcircled{1}$ ,

$$y = -2(6) + 24 = 12$$

Koordinat kedudukan bank ialah (6, 12).

The coordinates of the location of the bank is (6, 12).

(c) Katakan nisbah jarak antara rumah Qistina dan gym =  $m : n$

Let the ratio of distance between Qistina's house and gym =  $m : n$

$$\frac{n(-3) + m(9)}{m + n} = 5$$

$$-3n + 9m = 5(m + n)$$

$$-3n + 9m = 5m + 5n$$

$$4m = 8n$$

$$\frac{m}{n} = \frac{2}{1}$$

$$\therefore m : n = 2 : 1$$

$$p = \frac{1(0) + 2(6)}{1 + 2}$$

$$= \frac{12}{3}$$

$$= 4$$

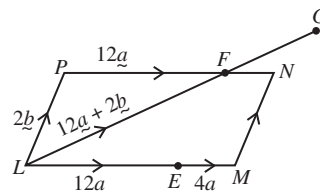
(d)  $(x-9)^2 + (y-6)^2 = 1^2$

$$x^2 - 18x + 81 + y^2 - 12y + 36 = 1$$

$$x^2 + y^2 - 18x - 12y + 116 = 0$$

11 (a) (i)  $\vec{LF} = \vec{LP} + \vec{PF}$   
 $= 12\vec{a} + 2\vec{b}$

(ii)  $\vec{EN} = \vec{EM} + \vec{MN}$   
 $= \frac{1}{3}\vec{LE} + \vec{LP}$   
 $= 4\vec{a} + 2\vec{b}$   
 $= 2(2\vec{a} + \vec{b})$



Daripada/From (ii),

$$2\vec{a} + \vec{b} = \frac{1}{2}\vec{EN}$$

$$\vec{EG} = \vec{EL} + \vec{LG}$$

$$= -12\vec{a} + \vec{LF} + \vec{FG}$$

$$= -12\vec{a} + 12\vec{a} + 2\vec{b} + 6\vec{a} + \vec{b}$$

$$= 6\vec{a} + 3\vec{b}$$

$$= 3(2\vec{a} + \vec{b})$$

$$= \frac{3}{2}\vec{EN}$$

Maka, titik E, N dan G adalah segaris.

Thus, points E, N and G are collinear.

(b) (i)  $\vec{EN} = 4\vec{a} + 2\vec{b}$   
 $= 4(6\vec{j}) + 2(4\vec{i} + 10\vec{j})$   
 $= 24\vec{i} + 8\vec{i} + 20\vec{j}$   
 $= 32\vec{i} + 20\vec{j}$

(ii)  $|\vec{EN}| = \sqrt{32^2 + 20^2}$   
 $= \sqrt{1424}$   
 $= 4\sqrt{89}$

Vektor unit dalam arah  $\vec{EN}$

Unit vector in the direction of  $\vec{EN}$

$$= \frac{1}{|\vec{EN}|}(\vec{EN})$$

$$= \frac{1}{4\sqrt{89}}(32\vec{i} + 20\vec{j})$$

$$= \frac{1}{\sqrt{89}}(8\vec{i} + 5\vec{j})$$

12 (a) (i)  $\frac{\sin EFH}{12} = \frac{\sin 96}{15.73}$

$$\sin \angle EFH = \frac{12 \times \sin 96}{15.73}$$

$$= 0.7587$$

$$\angle EFH = 49.35^\circ$$

(ii)  $\angle FEG = 180^\circ - 2(49.35^\circ)$   
 $= 81.3^\circ$

$$FG^2 = 9^2 + 9^2 - 2(9)(9) \cos 81.3^\circ$$

$$FG^2 = 9^2 + 9^2 - 2(9)(9) \cos 81.3^\circ$$

$$= 137.496$$

$$FG = 11.726 \text{ cm}$$

**Kaedah alternatif**  
**Alternative method**

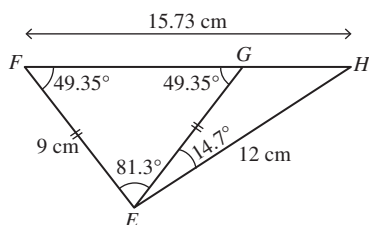
$$\frac{\sin 81.3}{FG} = \frac{\sin 49.35^\circ}{9}$$

$$FG = \frac{9 \times \sin 81.3^\circ}{\sin 49.35^\circ}$$

$$= 11.726 \text{ cm}$$



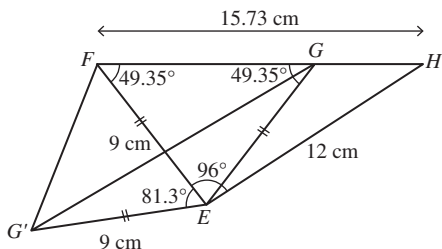
(iii)



$$\angle GEH = 96^\circ - 81.3^\circ = 14.7^\circ$$

$$\begin{aligned} \text{Luas/Area of } \triangle EGH &= \frac{1}{2} \times 9 \times 12 \times \sin 14.7^\circ \\ &= 13.703 \text{ cm}^2 \end{aligned}$$

(b)



$$\angle G'EG = 2 \times 81.3^\circ = 162.6^\circ$$

$$(G'G)^2 = 9^2 + 9^2 - 2(9)(9) \cos 162.6^\circ$$

$$\begin{aligned} (G'G)^2 &= 9^2 + 9^2 - 2(9)(9) \cos 162.6^\circ \\ &= 316.587 \end{aligned}$$

$$G'G = 17.793 \text{ cm}$$

13 (a) (i)  $QS^2 = 12^2 + 7^2 - 2(12)(7) \cos 65^\circ$

$$QS^2 = 12^2 + 7^2 - 2(12)(7) \cos 65^\circ = 122$$

$$QS = \sqrt{122} = 11.045 \text{ cm}$$

(ii)  $\angle QRS = 180^\circ - 65^\circ = 115^\circ$

$$\frac{\sin QSR}{4.6} = \frac{\sin 115^\circ}{11.045}$$

$$\sin \angle QSR = \frac{4.6 \sin 115^\circ}{11.045}$$

$$= 0.3775$$

$$\angle QSR = 22.18^\circ$$

$$\begin{aligned} \angle SQR &= 180^\circ - 115^\circ - 22.18^\circ \\ &= 42.82^\circ \end{aligned}$$

(b) (i) Luas PQRS = Luas  $\triangle QPS$  + Luas  $\triangle SQR$

$$\text{Area of PQRS} = \text{Area of } \triangle PQS + \text{Area of } \triangle SQR$$

$$= \frac{1}{2} \times 12 \times 7 \times \sin 65^\circ$$

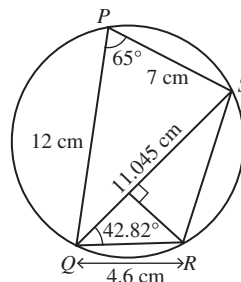
$$+ \frac{1}{2} \times 11.045 \times 4.6 \times \sin 42.82^\circ$$

$$= 38.065 \text{ cm}^2 + 17.267 \text{ cm}^2$$

$$= 55.332 \text{ cm}^2$$

(ii) Katakan  $h$  ialah jarak terpendek dari  $R$  ke  $QS$

Let  $h$  be the shortest distance from  $R$  to  $QS$



$$\text{Luas/Area of } \triangle QRS = \frac{1}{2} \times h \times QS$$

$$17.267 = \frac{1}{2} \times h \times 11.045$$

$$\begin{aligned} h &= \frac{2 \times 17.267}{11.045} \\ &= 3.127 \text{ cm} \end{aligned}$$

14 (a)  $x = \frac{5.40}{4.00} \times 100 = 135$

$$\frac{y}{3.50} \times 100 = 140$$

$$\begin{aligned} y &= \frac{140 \times 3.50}{100} \\ &= 4.90 \end{aligned}$$

$$\frac{6.25}{z} \times 100 = 125$$

$$z = \frac{6.25 \times 100}{125}$$

$$z = 5.00$$

(b)  $I = \frac{P_{2020}}{P_{2016}} \times 100$

$$= \frac{2.40}{1.60} \times 100$$

$$= 150$$

(c)  $360^\circ - 140^\circ - 110^\circ - 30^\circ = 80^\circ$

$$\bar{I} = \frac{\sum I_i w_i}{\sum w_i}$$

$$= \frac{135(30) + 140(110) + 125(80) + 200(140)}{360}$$

$$= \frac{57450}{360}$$

$$= 159.58$$

(d)  $\frac{120}{P_{2020}} \times 100 = 159.583$

$$P_{2020} = 75.196$$

Harga pai strawberi pada tahun 2020 ialah RM75.20.

The price of the strawberry pie in the year 2020 was RM75.20.

15 (a)  $u = \frac{62.5}{50} \times 100$

$$= 125$$

$$\frac{105.00}{v} \times 100 = 140$$

$$v = \frac{105.00}{140} \times 100$$

$$= 75$$

$$\frac{w}{55} \times 100 = 130$$

$$w = \frac{55 \times 130}{100}$$

$$= 71.50$$

(b) (i)  $\frac{120(3) + 125(n) + 140(6) + 130(4)}{3 + n + 6 + 4} = 129.75$

$$\frac{125n + 1\,720}{n + 13} = 129.75$$

$$125n + 1\,720 = 129.75(n + 13)$$

$$125n + 1\,720 = 129.75n + 1\,686.75$$

$$33.25 = 4.75n$$

$$n = 7$$

- (ii) Katakan  $h$  = hasil jualan pada tahun 2018  
 Let  $h$  = total sales in the year 2018

$$\frac{h}{24\,000} \times 100 = 129.75$$

$$h = \text{RM}31\,140$$

(c)  $I_{2024/2023} = 129.75 \times \frac{100 + 4}{100}$

$$= 129.75 \times 1.04$$

$$= 134.94$$