

Penyelesaian Lengkap

Kertas Model SPM

Kertas 1

1 C

- A $5\ 876\ \text{kg} = 5.876 \times 10^3\ \text{kg}$
- B $0.00015\ \text{mm} = 1.5 \times 10^{-4}\ \text{mm}$
- C $0.352\ \text{m}\ell = 3.52 \times 10^{-1}\ \text{m}\ell$

2 D

3 C

$$\begin{aligned}\text{Nilai matang/Matured value} &= P \left(1 + \frac{r}{n}\right)^{nt} \\ &= 15\ 000 \left(1 + \frac{0.04}{6}\right)^{(6)(3)} \\ &= \text{RM}16\ 905.72\end{aligned}$$

Jumlah faedah yang terkumpul/Total accumulated interest

$$\begin{aligned}&= \text{RM}16\ 905.72 - \text{RM}15\ 000 \\ &= \text{RM}1\ 905.72\end{aligned}$$

4 D

5 A

6 B

7 D

$$\begin{aligned}0.5\left(\frac{x}{60}\right)(24) + \frac{x}{60}(24) + 0.5\left(\frac{18-2x}{60}\right)(48+24) &= 6 \\ \frac{x}{5} + \frac{2x}{5} + \frac{54-6x}{5} &= 6 \\ -\frac{3x}{5} + \frac{54}{5} &= 6 \\ -3x + 54 &= 30 \\ -3x &= -24 \\ x &= 8\end{aligned}$$

8 C

$$\begin{aligned}f(x) &= (x-1)(x-5) \\ &= x^2 - 6x + 5\end{aligned}$$

9 B

$$x \propto \frac{y}{\sqrt[3]{\frac{1}{z}}}$$

$$k = \frac{x^3 \sqrt[3]{\frac{1}{z}}}{y}$$

$$k = \frac{\sqrt[3]{125}}{2}$$

$$k = \frac{1}{10}$$

$$x = \frac{y}{10 \sqrt[3]{\frac{1}{z}}}$$

10 C

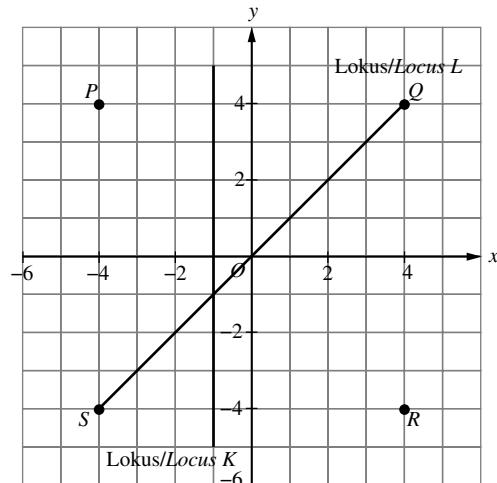
(0, 4) (3, 0), Pintasan- $y = 4$
 y -intercept = 4

$$y = \frac{-4x}{3} + 4$$

11 A

12 A

13 D



14 D

Jejari bulatan terbesar ialah $4r$.

Radius of the largest circle is $4r$.

Luas bulatan terbesar/Area of the largest circle
 $= \pi(4r)^2$
 $= 16\pi r^2$

15 C

16 A

$$\xi = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$

$$A = \{1, 3, 5\}$$

$$B = \{1, 5\}$$

17 D

18 A

20	30	30	30	40	40	50	60	80
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Median = 40

Kuartil pertama/First quartile = 30

Kuartil ketiga/Third quartile

$$= \frac{50 + 60}{2}$$

$$= 55$$

Julat antara kuartil/Interquartile range

$$= 55 - 30$$

$$= 25$$

19 B

Harga/Price (RM)	Kekerapan Frequency, f	x	fx
501 – 1 000	10	750.5	7 505
1 001 – 1 500	9	1 250.5	11 254.5
1 501 – 2 000	8	1 750.5	14 004
2 001 – 2 500	15	2 250.5	33 757.5
	$\sum f = 42$		$\sum fx = 66 521$

$$\begin{aligned} \text{Min/Mean} &= \frac{\sum fx}{\sum f} \\ &= \frac{66 521}{42} \\ &= \text{RM}1 583.83 \end{aligned}$$

20 B

$$\begin{aligned} \text{Kebarangkalian/Probability} &= (0.3 \times 0.6) + (0.7 \times 0.4) \\ &= 0.46 \end{aligned}$$

21 B

$$\begin{aligned} [(-\sqrt{a}) \div (-\sqrt{b})] \times \sqrt{\frac{a}{b}} \\ &= \sqrt{\frac{a}{b}} \times \sqrt{\frac{a}{b}} \\ &= \frac{a}{b} \end{aligned}$$

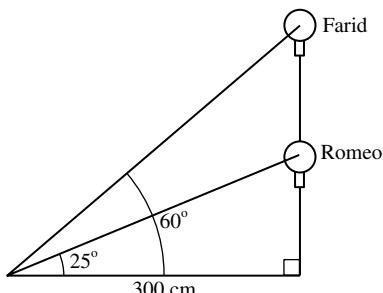
22 C

Luas trapezium

Area of trapezium

$$\begin{aligned} &= 0.5 \times [(12 \times 10^3) + (6 \times 10^2)] \times (5 \times 10^2) \text{ cm}^2 \\ &= 3.15 \times 10^6 \text{ cm}^2 \end{aligned}$$

23 C



Ketinggian Farid dari tanah mengufuk
Height of Farid from the horizontal ground

$$= 300 \tan 60^\circ$$

$$= 519.62 \text{ cm}$$

Ketinggian Romeo dari tanah mengufuk

Height of Romeo from the horizontal ground

$$= 300 \tan 25^\circ$$

$$= 139.89 \text{ cm}$$

$$\begin{aligned} \text{Perbezaan/Difference} &= 519.62 - 139.89 \\ &= 379.73 \text{ cm} \end{aligned}$$

24 A

$$\frac{y-1}{2}(y+1) = 4(y+1)$$

$$y^2 - 1 = 8y + 8$$

$$y^2 - 8y - 9 = 0$$

$$(y+1)(y-9) = 0$$

$$y = -1 \text{ atau/or } y = 9$$

25 C

26 B

$$\begin{aligned} a^2 + b^2 + 2ab &= a^2 - b^2 + a(a+b) \\ (a+b)^2 &= (a-b)(a+b) + a(a+b) \\ a+b &= (a-b+a) \\ a+b &= 2a-b \\ a &= 2b \end{aligned}$$

27 D

$$r \propto \sqrt{A}$$

$$r = k\sqrt{A}$$

$$k = \frac{r}{\sqrt{A}}$$

$$= \frac{3}{\sqrt{28.27}}$$

$$= 0.5642$$

$$r = 0.5642\sqrt{A}$$

Apabila $r = 9 \text{ cm}$,

When $r = 9 \text{ cm}$,

$$9 = 0.5642\sqrt{A}$$

$$\sqrt{A} = 15.95$$

$$A = 254$$

28 B

$$(p-1)\begin{pmatrix} 2 & 3 \\ 4 & q \end{pmatrix} = (14 \quad 13)$$

$$2p+4=14$$

$$2p=10$$

$$p=5$$

$$3p+q=13$$

$$3(5)+q=13$$

$$q=-2$$

$$p+q=5-2$$

$$=3$$

29 A

$$y = 68^\circ \times 2$$

$$= 136^\circ$$

Saiz sudut pada pusat bulatan adalah dua kali ganda saiz sudut pada lilitan bulatan yang dicangkum oleh suatu lengkok yang sama.

The size of angle at the centre of a circle is twice the size of angle at the circumference of the circle subtended by the same arc.

30 B

Diberi bahawa tinggi dan tapak kedua-dua segi tiga itu adalah berkadar.

Given that the heights and the bases of the triangles are in proportion.

$$\frac{r}{9} = \frac{12}{4}$$

$$r = 27 \text{ cm}$$

Luas segi tiga kecil/Area of small triangle

$$= 0.5(4)(9)$$

$$= 18 \text{ cm}^2$$

Luas segi tiga besar/Area of big triangle

$$= 0.5(12)(27)$$

$$= 162 \text{ cm}^2$$

- Nisbah/Ratio
 $= 18 : 162$
 $= 1 : 9$
- 31 D**
A ialah pelan.
A is a top view (plan).
B ialah dongakan depan.
B is a front view.
C ialah dongakan sisi.
C is a side view.
- 32 B**
Nombor perdana yang seterusnya selepas 29 ialah 31.
The next prime number after 29 is 31.
 $7 + 6 + 1 + x + 5 + x + 8 = 31$
 $2x + 27 = 31$
 $2x = 4$
 $x = 2$
- Bilangan murid yang terlibat dalam kajian ini
The number of pupils involved in this survey
 $= 31 + 2x$
 $= 31 + 2(2)$
 $= 35$
- 33 C**
Dalam pusingan kedua, peratusan peserta yang mengambil lebih daripada 80 minit ialah
In the second round, the percentage of participants who took more than 80 minutes is
 $\frac{2}{31} \times 100\% = 6.45\%$
- 34 A**
Nombor genap/Even numbers = {66, 68, 76, 96, 88, 86, 78, 98}
Kebarangkalian/Probability = $\frac{8}{16} = 0.5$
- 35 B**
Katakan x ialah perbelanjaan tidak tetap May.
Let x be May's variable expenses.
 $\text{RM}4\,000 - \text{RM}2\,500 - \text{RM}x = -\text{RM}240$
 $x = \text{RM}1\,740$
- 36 B**

2	444, 432, 420
2	222, 216, 210
	111, 108, 105

Dalam satu kumpulan, terdapat 111, 108 dan 105 orang murid Tingkatan 3, 4 dan 5 masing-masing.
Jumlah murid dalam satu kumpulan ialah
 $111 + 108 + 105 = 324$.
In a group, there are 111, 108 and 105 pupils of Forms 3, 4 and 5 respectively. The total number of pupils in a group is $111 + 108 + 105 = 324$.
 $324 \times \frac{2}{3} = 216$
- 37 C**
 $3x = 6$
 $y = 6$
- Maka/Thus,
 $3x = y$
 $x = \frac{y}{3}$
- 38 D**
 $5 + 10 + 30 + 40 + 15 = 100$
- 39 D**
Diameter = 11_9
 $= 1(9^1) + 1(9^0)$
 $= 9 + 1$
 $= 10 \text{ cm}$
- Tinggi/Height = 31_7
 $= 3(7^1) + 1(7^0)$
 $= 21 + 1$
 $= 22 \text{ cm}$
- Isi padu silinder/Volume of the cylinder
 $= \pi(5^2)(22)$
 $= 550\pi \text{ cm}^3$
- Panjang sisi kubus/Length of side of cube
 $= 12_3$
 $= 1(3^1) + 2(3^0)$
 $= 3 + 2$
 $= 5 \text{ cm}$
- Isi padu kubus/Volume of cube
 $= 5^3$
 $= 125 \text{ cm}^3$
- Isi padu air yang akan mengalir keluar
The volume of water that will flow out
 $= 550\pi - 125$
 $= 550\left(\frac{22}{7}\right) - 125$
 $= 1\,604$
- 40 D**

Kertas 2

Bahagian/Section A

- 1 Luas/Area = $y^2 + 7y + 10$
 $= (y + 5)(y + 2)$
Perimeter = $2(y + 5) + 2(y + 2)$
 $= 2y + 10 + 2y + 4$
 $= 4y + 14 \text{ cm}$
- 2 (a) 3, 0.6, 0.12, 0.024, 0.0048
(b) Mendarab 0.2 kepada nombor sebelumnya.
Multiply 0.2 to the previous number.
- 3 (a) kos/cos $k = \frac{1}{2}$
 $k = \cos^{-1}/\cos^{-1} 0.5$
 $= 60^\circ$
(b) $(0, 0)(\sqrt{3}, 1)$
 $y = \frac{x}{\sqrt{3}}$
- 4 $410_6 = 4(6^2) + 1(6^1)$
 $= 150 \text{ cm}$
- $1020_5 = 1(5^3) + 2(5^1)$
 $= 135 \text{ cm}$

Grace adalah lebih berpotensi sebab dia mencapai ketinggian yang lebih dalam pertandingan.
Grace is more potential as she achieved a higher height in the competition.

$$5 \text{ (a)} P \propto \frac{B}{H}$$

$$P = \frac{kB}{H}$$

$$60 = \frac{3k}{40}$$

$$k = 800$$

$$P = \frac{800B}{H}$$

$$(b) 144 = \frac{800B}{50}$$

$$B = \frac{144 \times 50}{800}$$

$$B = 9$$

6 (a) Jumlah kos yang harus ditanggung oleh Mustafa
Total cost borne by Mustafa
 $= RM1\,000 + \frac{20}{100} \times (RM5\,000 - RM1\,000)$
 $= RM1\,800$

(b) Katakan x mewakili yuran pengajian sendiri.
Let x represents the fee for self education.
 Pendapatan bercukai = Jumlah pendapatan
 - Pengecualian cukai - Pelepasan cukai
 $\text{Chargeable income} = \text{Total annual income} - \text{Tax exemption} - \text{Tax relief}$
 $RM78\,100 = RM93\,600 - RM9\,000 - x$
 $x = RM6\,500$

7 (a) Diberi persamaan garis lurus yang menghubungkan pasar dengan kedai runcit ialah
 $y = \frac{3}{4}x - \frac{1}{4}$.
Given the equation of straight line that connects the market with the grocery store is $y = \frac{3}{4}x - \frac{1}{4}$.
 Gantikan $(-1, -1)$ dan $m = -\frac{4}{3}$ ke dalam $y = mx + c$.
Substitute $(-1, -1)$ and $m = -\frac{4}{3}$ into $y = mx + c$.
 $y = -\frac{4}{3}x + c$
 $-1 = -\frac{4}{3} + c$
 $c = -\frac{7}{3}$

Maka, persamaan garis lurus ialah $y = -\frac{4}{3}x - \frac{7}{3}$.

Hence, the equation of the straight line is
 $y = -\frac{4}{3}x - \frac{7}{3}$.

(b) Koordinat bagi padang ialah $(n, 3)$.
The coordinate of the field is $(n, 3)$
 $\sqrt{[3 - (-1)]^2 + [n - (-1)]^2} = 5$
 $16 + (n + 1)^2 = 25$
 $(n + 1)^2 = 9$

$$n + 1 = 3 \quad \text{atau /or} \quad n + 1 = -3$$

$$n = 2 \quad \quad \quad n = -4$$

$$\therefore n = -4$$

$$8 \text{ (a)} \frac{30}{100 + p + 70} = \frac{1}{10}$$

$$300 = 170 + p$$

$$p = 300 - 170$$

$$= 130$$

$$(b) \frac{10 + 6}{20 + 3 + 0.02q} = \frac{4}{11}$$

$$176 = 92 + 0.08q$$

$$q = 1\,050$$

9 (a) Wang pendahuluan/*Down payment*
 $= \frac{20}{100} \times RM90\,000 = RM18\,000$

Dia perlu menyimpan $\frac{RM18\,000}{24} = RM750$

sebulan untuk mencapai matlamat kewangannya.
 Eric dapat mencapai matlamat kewangannya sebab dia dapat menyimpan RM4 500 - RM2 000 = RM2 500 sebulan.

He needs to save $\frac{RM18\,000}{24} = RM750$ a month

in order to achieve his financial goal. Eric is able to achieve his financial goal as he managed to save RM4 500 - RM2 000 = RM2 500 per month.

(b) Aliran tunai = Jumlah pendapatan - Jumlah perbelanjaan

Cash flow = Total income - Total expenses
 $RM4\,150 = RM6\,000 + RM1\,000 - \text{Jumlah perbelanjaan}/\text{Total expenses}$

Jumlah perbelanjaan/Total expenses = RM2\,850
 $\text{Perbelanjaan tidak tetap}/\text{Variable expenses} = RM2\,850 - RM2\,000 = RM850$

10 (a)

Gaji harian <i>Daily wages</i> (RM)	Bilangan pekerja <i>Number of workers, f</i>	x	x^2	fx
5 - 9	3	7	49	21
10 - 14	9	12	144	108
15 - 19	18	17	289	306
20 - 24	25	22	484	550
25 - 29	m	27	729	$27m$
30 - 34	10	32	1 024	320
35 - 39	6	37	1 369	222
	$\sum f = 71 + m$			$\sum fx = 1\,527 + 27m$

$$\text{Min/Mean} = \frac{\sum fx}{\sum f}$$

$$\frac{\sum fx}{\sum f} = 23.1$$

$$\frac{1\,527 + 27m}{71 + m} = 23.1$$

$$1\,640.1 + 23.1m = 1\,527 + 27m$$

$$27m - 23.1m = 113.1$$

$$3.9m = 113.1$$

$$m = 29$$

(b)

Bilangan pekerja Number of workers, f	x	x^2	fx	fx^2
3	7	49	21	147
9	12	144	108	1 296
18	17	289	306	5 202
25	22	484	550	12 100
29	27	729	783	21 141
10	32	1 024	320	10 240
6	37	1 369	222	8 214
$\sum f = 100$			$\sum fx = 2 310$	$\sum fx^2 = 58 340$

Varians/Variance

$$= \frac{\sum fx^2}{\sum f} - \bar{x}^2$$

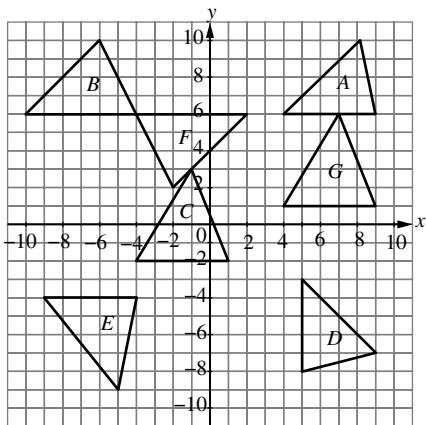
$$= \frac{58 340}{100} - 23.1^2$$

$$= \text{RM}49.79$$

Bahagian/Section B

- 11 (a) A dan/and D
B dan/and F

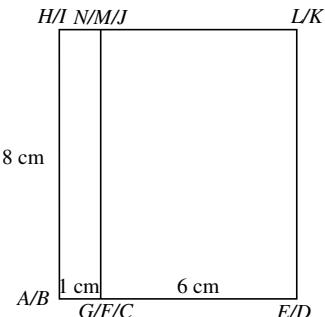
(b)



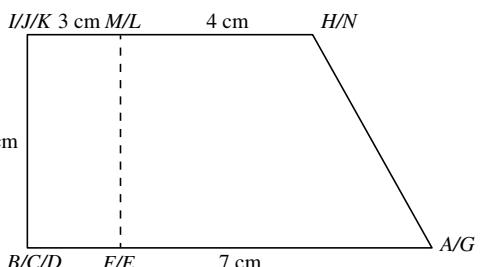
- (c) Pantulan pada garis $y = x + 10$ /Reflection in the line $y = x + 10$

Putaran 180° pada pusat $(-4, 6)$.
180° rotation at centre $(-4, 6)$.

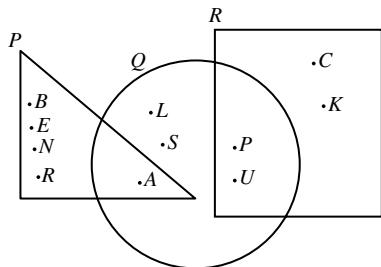
12 (a)



(b)



13 (a)



$$(b) Q' = \{B, E, N, R, C, K\}$$

$$n(Q') = 6$$

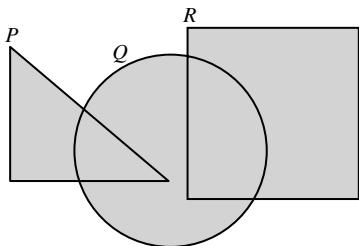
$$P' = \{L, S, P, U, C, K\}$$

$$n(P') = 6$$

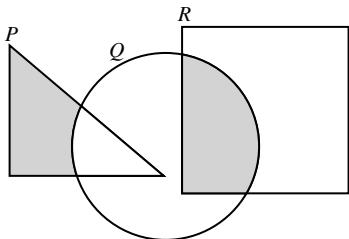
Maka, $n(Q') = n(P')$ adalah benar.

Hence, $n(Q') = n(P')$ is true.

(c) (i)



(ii)



$$14 \text{ (a)} \quad 0.5 \begin{pmatrix} 92 & 80 \\ 156 & 140 \\ 88 & 70 \end{pmatrix} \begin{pmatrix} 1.1 \\ 0.8 \end{pmatrix} = \begin{pmatrix} 82.6 \\ 141.8 \\ 76.4 \end{pmatrix}$$

Min IPU bagi ketiga-tiga negeri tersebut bagi dua hari tersebut masing-masing ialah 82.6, 141.8 dan 76.4.

The mean API for the three states for the two days is 82.6, 141.8 and 76.4 respectively.

$$\text{(b)} \quad 0.5 \begin{pmatrix} 92 & 80 \\ 156 & 140 \\ 88 & 70 \end{pmatrix} = \begin{pmatrix} 46 & 40 \\ 78 & 70 \\ 44 & 35 \end{pmatrix}$$

IPU bagi Perak dan Sarawak adalah dalam lingkungan yang sihat tetapi IPU di Selangor masih belum mencapai lingkungan yang sihat.

The API for Perak and Sarawak is in the healthy range but the API for Selangor has not reached the healthy level.

$$15 \text{ (a)} \quad 0.1x + 0.2y \leq 3 \\ x \geq 5y$$

$$\text{(b)} \quad 0.2y = -0.1x + 3 \\ y = -0.5x + 15 \dots\dots \textcircled{1}$$

Apabila $x = 0$, $y = 15$ dan $x = 20$, $y = 5$

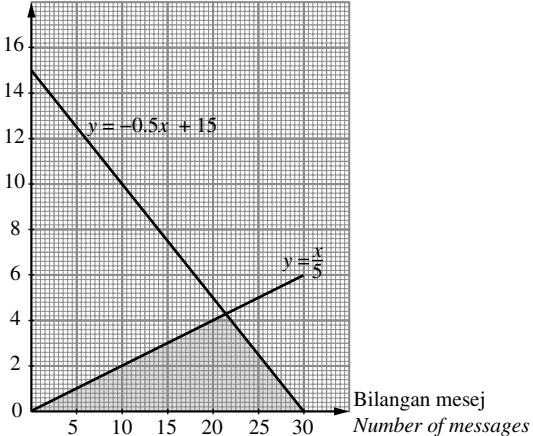
When $x = 0$, $y = 15$ *and* $x = 20$, $y = 5$

$$y = \frac{x}{5} \dots\dots \textcircled{2}$$

Apabila $x = 0$, $y = 0$ dan $x = 5$, $y = 1$

When $x = 0$, $y = 0$ *and* $x = 5$, $y = 1$

Bilangan panggilan/Number of phone calls



(c) $(20, 4)$ berada dalam kawasan berlorek. Maka, 4 minit panggilan dan 20 mesej adalah dalam budget Rodi.

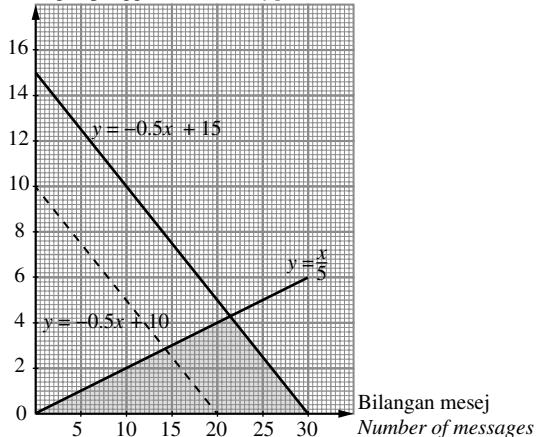
$(20, 4)$ is within the shaded region. Hence, 4 minutes of phone calls and 20 messages is within Rodi's budget.

$$\text{(d) (i)} \quad 0.1x + 0.2y < 2$$

$$\text{(ii)} \quad 0.2y = -0.1x + 2$$

$$y = -0.5x + 10$$

Bilangan panggilan/Number of phone calls



Bahagian/Section C

$$16 \text{ (a) (i)} \quad \text{Saat ke-6 hingga saat ke-28, iaitu, } 28 - 6 = 22 \text{ saat}$$

6th – 28th seconds, that is, $28 - 6 = 22$ seconds

(ii) Jarak yang dilalui/Distance travelled

$$= 0.5(6)(30)$$

$$= 90 \text{ m}$$

(b) Katakan a , b dan c masing-masing mewakili bilangan kucing betina dengan 3, 6 dan 8 ekor anak kucing.

Let a, b and c represents the number of female cats with 3, 6 and 8 kittens respectively.

$$a + b + c = 8 \dots\dots \textcircled{1}$$

$$a = c \dots\dots \textcircled{2}$$

Gantikan $\textcircled{2}$ ke dalam $\textcircled{1}$.

Substitute $\textcircled{2}$ into $\textcircled{1}$.

$$2c + b = 8 \dots\dots \textcircled{3}$$

$$\frac{5+c}{21} = \frac{1}{3}$$

$$c = a = 2 \dots\dots \textcircled{4}$$

Gantikan $\textcircled{4}$ ke dalam $\textcircled{3}$.

Substitute $\textcircled{4}$ into $\textcircled{3}$.

$$2(2) + b = 8$$

$$b = 4$$

Maka, nisbah bilangan kucing betina dengan 3, 6 dan 8 ekor anak kucing ialah $2 : 4 : 2 = 1 : 2 : 1$.

Hence, the ratio of female cats with 3, 6 and 8 kittens is $2 : 4 : 2 = 1 : 2 : 1$.

(c) Beza antara sudut tunduk ikan palsu/Difference in the angle of depression of fake fish

$$= \left(\tan^{-1} \frac{103}{50} \right) - \left(\tan^{-1} \frac{18}{50} \right)$$

$$= 64.11^\circ - 19.8^\circ$$

$$= 44.31^\circ$$

