



$\therefore (-2, 4)$  lies on the straight line.

$$(2, 4): \quad x + 2y = 2 + 2(4) \\ = 10 \\ \neq 6$$

$\therefore (2, 4)$  does not lie on the straight line.

$$(12, -3): \quad x + 2y = 12 + 2(-3) \\ = 6$$

$\therefore (12, -3)$  lies on the straight line.

$$(-3, 9): \quad x + 2y = -3 + 2(9) \\ = 15 \\ \neq 6$$

$\therefore (-3, 9)$  does not lie on the straight line.

9

(a)	$(5, -3)$	$x + \frac{1}{2}y = 1$
(b)	$(-3, -2)$	$y = -x + 2$
(c)	$(-1, 4)$	$3x - y = 6$
(d)	$(2, 0)$	$\frac{x}{3} - y = 1$

10

Straight line	Gradient
AB	$\frac{1}{2}$
CD	$\frac{1}{2}$
EF	$\frac{1}{2}$

(b) The gradients of parallel straight lines are equal.

11

(a)	$y = x + 3$	$2x + 3y = 36$
(b)	$5x + y = 10$	$x - y = 4$
(c)	$\frac{x}{3} + \frac{y}{2} = 1$	$\frac{x}{4} - y = 1$
(d)	$4y = x - 4$	$x + \frac{y}{5} = 1$

- 12 (a)  $y = 5$  (c)  $y = -3$   
 (b)  $x = 4$  (d)  $x = -3$

13 (a) The equation of straight line is  $y = 1$ .

(b) The equation of straight line is  $x = 7$ .

(c) The equation of straight line is  $y = 2x + 6$ .

(d)  $y = -3x + c$

Substitute  $x = 1, y = 0$ ,

$$0 = -3(1) + c$$

$$c = 3$$

The equation of straight line is  $y = -3x + 3$ .

14 (a)  $y = 4x + c$

Substitute  $x = 3, y = 4$ ,

$$4 = 4(3) + c$$

$$4 = 12 + c$$

$$c = -8$$

The equation of straight line is  $y = 4x - 8$ .

(b)  $y = -x + c$

Substitute  $x = -1, y = 3$ ,

$$3 = -(-1) + c$$

$$3 = 1 + c$$

$$c = 2$$

The equation of straight line is  $y = -x + 2$ .

15 (a)  $y = \frac{1}{2}x + c$

Substitute  $x = 4, y = 0$ ,

$$0 = \frac{1}{2}(4) + c$$

$$0 = 2 + c$$

$$c = -2$$

The equation of the straight line  $k$  is  $y = \frac{1}{2}x - 2$ .

(b)  $y = -2x + c$

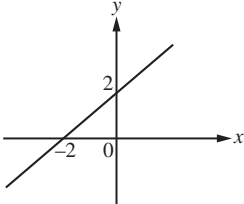
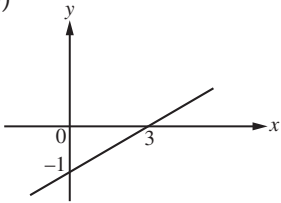
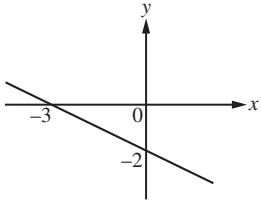
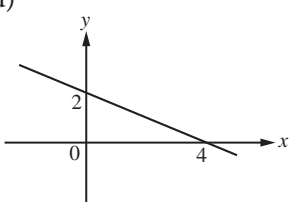
Substitute  $x = -1, y = 7$ ,

$$7 = -2(-1) + c$$

$$7 = 2 + c$$

$$c = 5$$

The equation of the straight line  $k$  is  $y = -2x + 5$ .

Straight line	x-intercept	y-intercept	Equation of straight line in the form $\frac{x}{a} + \frac{y}{b} = 1$
(a) 	-2	2	$-\frac{x}{2} + \frac{y}{2} = 1$
(b) 	3	-1	$\frac{x}{3} - y = 1$
(c) 	-3	-2	$-\frac{x}{3} - \frac{y}{2} = 1$
(d) 	4	2	$\frac{x}{4} + \frac{y}{2} = 1$

$$17 \text{ (a) } m = \frac{-6 - 2}{-1 - 3}$$

$$= \frac{-8}{-4}$$

$$= 2$$

$$(b) \text{ (i) } 2 = 2 \times 3 + c$$

$$2 = 6 + c$$

$$c = -4$$

$$(ii) -6 = 2 \times (-1) + c$$

$$-6 = -2 + c$$

$$c = -4$$

$$18 \text{ (a) } m = \frac{1 + 3}{9 - 5}$$

$$= \frac{4}{4}$$

$$= 1$$

$$y = x + c$$

Substitute  $x = 9, y = 1$ ,

$$1 = 9 + c$$

$$c = -8$$

The equation of the straight line is  $y = x - 8$ .

$$(b) m = \frac{8 + 7}{1 + 2}$$

$$= \frac{15}{3}$$

$$= 5$$

$$y = 5x + c$$

Substitute  $x = 1, y = 8$ ,

$$8 = 5(1) + c$$

$$8 = 5 + c$$

$$c = 3$$

The equation of the straight line is  $y = 5x + 3$ .

$$(c) m = \frac{11+4}{-2-3}$$

$$= \frac{15}{-5}$$

$$= -3$$

$$y = -3x + c$$

Substitute  $x = -2, y = 11,$

$$11 = -3(-2) + c$$

$$11 = 6 + c$$

$$c = 5$$

The equation of the straight line is  $y = -3x + 5.$

$$(d) m = \frac{-1+3}{-4-4}$$

$$= \frac{2}{-8}$$

$$= -\frac{1}{4}$$

$$y = -\frac{1}{4}x + c$$

Substitute  $x = -4, y = -1,$

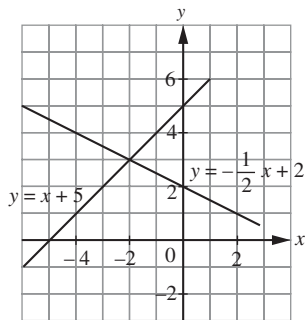
$$-1 = -\frac{1}{4}(-4) + c$$

$$-1 = 1 + c$$

$$c = -2$$

The equation of the straight line is  $y = -\frac{1}{4}x - 2.$

19 (a)



(b) The coordinates of the point of intersection are  $(-2, 3).$

20 (a)  $y = 4x - 5 \dots \textcircled{1}$

$$y = 3 \dots \textcircled{2}$$

Substitute  $\textcircled{2}$  into  $\textcircled{1},$

$$3 = 4x - 5$$

$$4x = 8$$

$$x = 2$$

$\therefore$  Point of intersection:  $(2, 3)$

(b)  $3x - 2y = 1 \dots \textcircled{1}$

$$y = -5x - 7 \dots \textcircled{2}$$

Substitute  $\textcircled{2}$  into  $\textcircled{1},$

$$3x - 2(-5x - 7) = 1$$

$$3x + 10x + 14 = 1$$

$$13x = -13$$

$$x = -1$$

$$\text{From } \textcircled{2}, y = -5(-1) - 7$$

$$= 5 - 7$$

$$= -2$$

$\therefore$  Point of intersection:  $(-1, -2)$

(c)  $y = x - 7 \dots \textcircled{1}$

$$x - \frac{y}{4} = 4 \dots \textcircled{2}$$

$$\textcircled{2} \times 4, 4x - y = 16 \dots \textcircled{3}$$

$$\textcircled{1} + \textcircled{3}, 4x = x + 9$$

$$3x = 9$$

$$x = 3$$

From  $\textcircled{1}, y = 3 - 7$

$$= -4$$

$\therefore$  Point of intersection:  $(3, -4)$

(d)  $2x + y = 1 \dots \textcircled{1}$

$$-\frac{x}{12} + \frac{y}{6} = 1 \dots \textcircled{2}$$

$$\textcircled{2} \times 24, -2x + 4y = 24 \dots \textcircled{3}$$

$$\textcircled{1} + \textcircled{3}, y + 4y = 1 + 24$$

$$5y = 25$$

$$y = 5$$

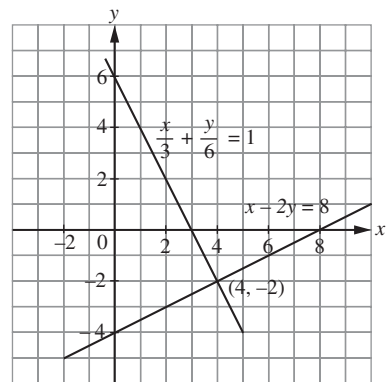
From  $\textcircled{1}, 2x + 5 = 1$

$$2x = -4$$

$$x = -2$$

$\therefore$  Point of intersection:  $(-2, 5)$

21 (a)



Point of intersection:  $(4, -2)$

(b)  $x - 2y = 8 \dots \textcircled{1}$

$$\frac{x}{3} + \frac{y}{6} = 1 \dots \textcircled{2}$$

$$\textcircled{2} \times 6, 2x + y = 6$$

$$y = 6 - 2x \dots \textcircled{3}$$

Substitute  $\textcircled{3}$  into  $\textcircled{1},$

$$x - 2(6 - 2x) = 8$$

$$x - 12 + 4x = 8$$

$$5x = 20$$

$$x = 4$$

From  $\textcircled{3}, y = 6 - 2(4)$

$$= -2$$

Point of intersection:  $(4, -2)$

(c)  $x - 2y = 8 \dots \textcircled{1}$

$$\frac{x}{3} + \frac{y}{6} = 1 \dots \textcircled{2}$$

$$\textcircled{2} \times 12, 4x + 2y = 12 \dots \textcircled{3}$$

$$\textcircled{1} + \textcircled{3}, x + 4x = 8 + 12$$

$$5x = 20$$

$$x = 4$$

From  $\textcircled{1}$ ,  $4 - 2y = 8$

$$-2y = 4$$

$$y = -2$$

Point of intersection:  $(4, -2)$

22 (a) The  $y$ -intercept of the straight line  $BC$  is 4.

$$\therefore B(0, 4)$$

$$4x + y = k$$

Substitute  $x = 0, y = 4$ ,

$$4(0) + 4 = k$$

$$k = 4$$

(b) The straight line  $AD$  is parallel to the  $x$ -axis.

$\therefore$  The equation of the straight line  $AD$  is  $y = -2$ .

(c) Gradient  $CD =$  Gradient  $AB$

$$= -4$$

$$y = -4x + c$$

Substitute  $x = 6, y = -2$ ,

$$-2 = -4(6) + c$$

$$-2 = -24 + c$$

$$c = 22$$

The equation of the straight line  $CD$  is  $y = -4x + 22$ .

(d)  $4x + y = 4 \dots \textcircled{1}$

$$y = -2 \dots \textcircled{2}$$

Substitute  $\textcircled{2}$  into  $\textcircled{1}$ ,

$$4x - 2 = 4$$

$$4x = 6$$

$$x = \frac{3}{2}$$

The coordinates of point  $A$  are  $\left(\frac{3}{2}, -2\right)$ .

### Summative Practice

1 A  $3y = x + 12$

When  $x = 0$ ,

$$3y = 12$$

$$y = 4$$

The  $y$ -intercept = 4

B  $\frac{1}{2}y = 2x - 3$

When  $x = 0$ ,

$$\frac{1}{2}y = -3$$

$$y = -6$$

The  $y$ -intercept = -6

C  $-\frac{x}{6} + \frac{y}{3} = 1$

When  $x = 0$ ,

$$\frac{y}{3} = 1$$

$$y = 3$$

The  $y$ -intercept = 3

D  $5x - 3y = 9$

When  $x = 0$ ,

$$-3y = 9$$

$$y = -3$$

The  $y$ -intercept = -3

Answer: C

2  $3y = kx + 5$

$$y = \frac{k}{3}x + \frac{5}{3}$$

$$\text{Gradient} = \frac{k}{3}$$

$$x + y = 10$$

$$y = -x + 10$$

$$\text{Gradient} = -1$$

$$\frac{k}{3} = \frac{1}{2} \times (-1)$$

$$k = -\frac{3}{2}$$

Answer: B

3 Gradient,

$$m = -\frac{8}{(-4)}$$

$$= 2$$

$y$ -intercept,

$$c = 8$$

The equation of the straight line is  $y = 2x + 8$ .

Answer: A

4  $\frac{k-5}{-8-2} = \frac{4}{5}$

$$\frac{k-5}{-10} = \frac{4}{5}$$

$$k - 5 = -8$$

$$k = -3$$

Answer: B

5  $px + qy = 6$

Substitute  $x = 1, y = -3$ ,

$$p(1) + q(-3) = 6$$

$$p - 3q = 6 \dots \textcircled{1}$$

Substitute  $x = -2, y = -12$ ,

$$p(-2) + q(-12) = 6$$

$$-2p - 12q = 6$$

$$-p - 6q = 3 \dots \textcircled{2}$$

$$\textcircled{1} + \textcircled{2}, -3q - 6q = 9$$

$$-9q = 9$$

$$q = -1$$

$$\begin{aligned} \text{From } \textcircled{1}, p - 3(-1) &= 6 \\ p + 3 &= 6 \\ p &= 3 \end{aligned}$$

**Alternative method**

$$\begin{aligned} \text{Gradient, } m &= \frac{-12 + 3}{-2 - 1} \\ &= \frac{-9}{-3} \\ &= 3 \end{aligned}$$

$$y = 3x + c$$

Substitute  $x = 1, y = -3,$

$$-3 = 3(1) + c$$

$$-3 = 3 + c$$

$$c = -6$$

The equation of the straight line is  $y = 3x - 6$  or

$$3x - y = 6.$$

$$\therefore p = 3, q = -1$$

Answer: D

6  $qy = (2p + 5)x + 9$

(a) Straight line that is parallel to the  $x$ -axis has equation of the form  $y = k.$

$$2p + 5 = 0 \text{ and } q \neq 0$$

$$2p = -5$$

$$p = -\frac{5}{2}$$

$$\therefore q \neq 0, p = -\frac{5}{2}$$

(b) Straight line that is parallel to the  $y$ -axis has equation of the form  $x = h.$

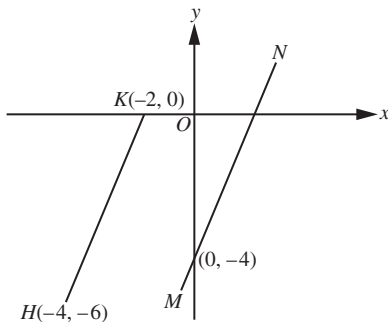
$$q = 0 \text{ and } 2p + 5 \neq 0$$

$$2p \neq -5$$

$$p \neq -\frac{5}{2}$$

$$\therefore p \neq -\frac{5}{2}, q = 0$$

7



$$\text{Gradient } MN = \text{Gradient } HK$$

$$= \frac{0 + 6}{-2 + 4}$$

$$\begin{aligned} &= \frac{6}{2} \\ &= 3 \\ m &= 3 \end{aligned}$$

$y$ -intercept,  $c = -4$

The equation of the straight line  $MN$  is  $y = 3x - 4.$

8 (a) (i)  $\frac{x}{2} + \frac{y}{(-4)} = 1$

$$\frac{x}{2} - \frac{y}{4} = 1$$

(ii) Gradient of the straight line  $l$

$$m = -\frac{-4}{2}$$

$$= 2$$

$$y = 2x + c$$

Substitute  $x = -3, y = 0,$

$$0 = 2(-3) + c$$

$$0 = -6 + c$$

$$c = 6$$

The equation of the straight line  $l$  is  $y = 2x + 6$  or

$$2x - y = -6.$$

(b) Straight line  $k:$

$$\frac{x}{2} - \frac{y}{4} = \frac{4}{2} - \frac{14}{4}$$

$$= 2 - \frac{7}{2}$$

$$= -\frac{3}{2}$$

$$\neq 1$$

$\therefore$  Straight line  $k$  does not pass through point  $(4, 14).$

Straight line  $l:$

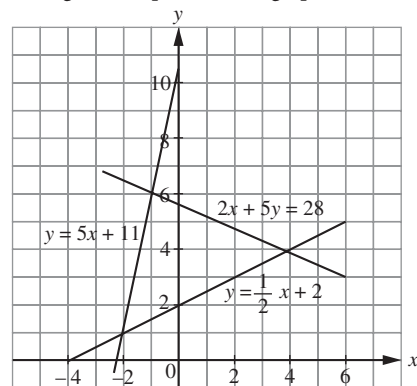
$$2x - y = 2(4) - 14$$

$$= 8 - 14$$

$$= -6$$

$\therefore$  Straight line  $l$  passes through point  $(4, 14).$

9 (a)



The points of intersection of the straight lines are

$(-2, 1), (4, 4)$  and  $(-1, 6).$

(b)  $y = 5x + 11 \dots \textcircled{1}$

$$2x + 5y = 28 \dots \textcircled{2}$$

Substitute  $y = 5x + 11$  into  $\textcircled{2},$

$$2x + 5(5x + 11) = 28$$

$$2x + 25x + 55 = 28$$

$$27x = 28$$

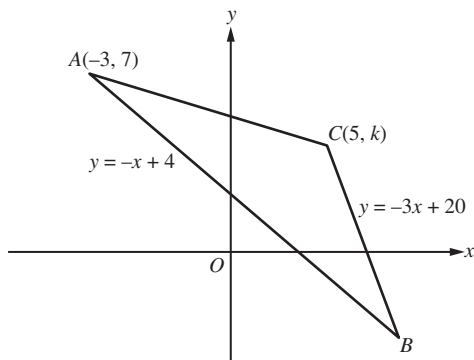
$$x = -1$$

$$\text{From ①, } y = 5(-1) + 11$$

$$= 6$$

The point of intersection  $(-1, 6)$  of the straight lines  $y = 5x + 11$  and  $2x + 5y = 28$  is the same as the graphical method.

10



(a)  $y = -3x + 20$

Substitute  $x = 5, y = k,$

$$k = -3(5) + 20$$

$$= -15 + 20$$

$$= 5$$

(b)  $y = -3x + 20 \dots$  ①

$$x + y = 4 \dots$$
 ②

Substitute ① into ②,

$$x + (-3x + 20) = 4$$

$$-2x + 20 = 4$$

$$-2x = -16$$

$$x = 8$$

$$\text{From ①, } y = -3(8) + 20$$

$$= -24 + 20$$

$$= -4$$

The coordinates of  $B$  are  $(8, -4)$ .

(c) Let the straight line  $AC$  cuts the  $x$ -axis at point

$E(a, 0)$ .

$$\text{Gradient } AE = \text{Gradient } AC$$

$$\frac{7 - 0}{-3 - a} = \frac{7 - 5}{-3 - 5}$$

$$\frac{7}{-3 - a} = \frac{2}{-8}$$

$$-28 = -3 - a$$

$$-25 = -a$$

$$a = 25$$

The  $x$ -intercept of the straight line  $AC$  is 25.

11 (a)  $RS$  is parallel to the  $y$ -axis.

$x$ -coordinate of point  $S = x$ -coordinate of point  $R$

$$a = -4$$

(b) (i) The equation of the straight line  $PQ$  is  $y = -3$ .

(ii) The equation of the straight line  $RS$  is  $x = -4$ .

(c) (i) Gradient  $PS$

$$= \frac{1 + 3}{-4 - 2}$$

$$= -\frac{4}{6}$$

$$= -\frac{2}{3}$$

$$y = -\frac{2}{3}x + c$$

Substitute  $x = 2, y = -3,$

$$-3 = -\frac{2}{3}(2) + c$$

$$-3 = -\frac{4}{3} + c$$

$$c = -3 + \frac{4}{3}$$

$$= -\frac{5}{3}$$

$$y = -\frac{2}{3}x - \frac{5}{3}$$

$$3y = -2x - 5$$

$$2x + 3y = -5$$

The equation of the straight line  $PS$  is  $2x + 3y = -5$ .

(ii) Gradient  $QR$

$$= -\frac{2}{3}$$

$$y = -\frac{2}{3}x + c$$

Substitute  $x = -4, y = 3,$

$$3 = -\frac{2}{3}(-4) + c$$

$$3 = \frac{8}{3} + c$$

$$c = 3 - \frac{8}{3}$$

$$= \frac{1}{3}$$

$$y = -\frac{2}{3}x + \frac{1}{3}$$

$$3y = -2x + 1$$

$$2x + 3y = 1$$

The equation of the straight line

$QR$  is  $2x + 3y = 1$ .

12 (a)  $OQ = 2$  units

$$\therefore Q(0, -2)$$

The equation of the straight line  $QR$  is  $y = -2$ .

(b) Gradient  $PQ$

$$= \frac{3 + 2}{-2 - 0}$$

$$= -\frac{5}{2}$$

$$y = -\frac{5}{2}x - c$$

Substitute  $x = -2, y = 3,$

$$3 = -\frac{5}{2}(-2) + c$$

$$3 = 5 + c$$

$$c = -2$$

The equation of the straight line  $PQ$  is  $y = -\frac{5}{2}x - 2.$

(c)  $QR$  is parallel to the  $x$ -axis.

$QR = 5$  units

$$\therefore R(5, -2)$$

$$y = -\frac{5}{2}x + c$$

Substitute  $x = 5, y = -2,$

$$-2 = -\frac{5}{2}(5) + c$$

$$-2 = -\frac{25}{2} + c$$

$$c = \frac{21}{2}$$

$$y = -\frac{5}{2}x + \frac{21}{2}$$

When  $y = 0,$

$$-\frac{5}{2}x + \frac{21}{2} = 0$$

$$\frac{5}{2}x = \frac{21}{2}$$

$$x = \frac{21}{5}$$

The  $x$ -intercept of the straight line  $RS$  is  $\frac{21}{5}.$

#### Alternative method

Let the straight line  $RS$  cuts the  $x$ -axis at point  $T(a, 0).$

Gradient  $RT =$  Gradient  $RS$

$$\frac{0 + 2}{a - 5} = -\frac{5}{2}$$

$$4 = -5(a - 5)$$

$$4 = -5a + 25$$

$$5a = 21$$

$$a = \frac{21}{5}$$

The  $x$ -intercept of the straight line  $RS$  is  $\frac{21}{5}.$

(d) (i)  $y = \frac{5}{3}x + c$

Substitute  $x = 5, y = -2,$

$$-2 = \frac{5}{3}(5) + c$$

$$-2 = \frac{25}{3} + c$$

$$c = -\frac{31}{3}$$

$$y = \frac{5}{3}x - \frac{31}{3}$$

$$3y = 5x - 31$$

$$5x - 3y = 31$$

The equation of the straight line is  $5x - 3y = 31.$

(ii)  $5x - 3y = 31 \dots \textcircled{1}$

$$y = -\frac{5}{2}x - 2$$

$$2y = -5x - 4$$

$$5x + 2y = -4 \dots \textcircled{2}$$

$$\textcircled{2} - \textcircled{1}, 5y = -35$$

$$y = -7$$

From  $\textcircled{1}, 5x - 3(-7) = 31$

$$5x + 21 = 31$$

$$5x = 10$$

$$x = 2$$

The point of intersection of the two straight lines is  $(2, -7).$