

Tingkatan 5 Bab 7
Pengaturcaraan Linear
Penyelesaian Lengkap

Praktis Formatif 7.1

1 (a) $1500x + 900y \leq 45\,000 \Rightarrow 5x + 3y \leq 150$

(b) $y - x \leq 10$

(c) $y \geq \frac{1}{10}x$

2 (a) $x \geq 10$

(b) $y \geq 2x$

(c) $8x + 12y \leq 12 \times 60 \Rightarrow 2x + 3y \leq 180$

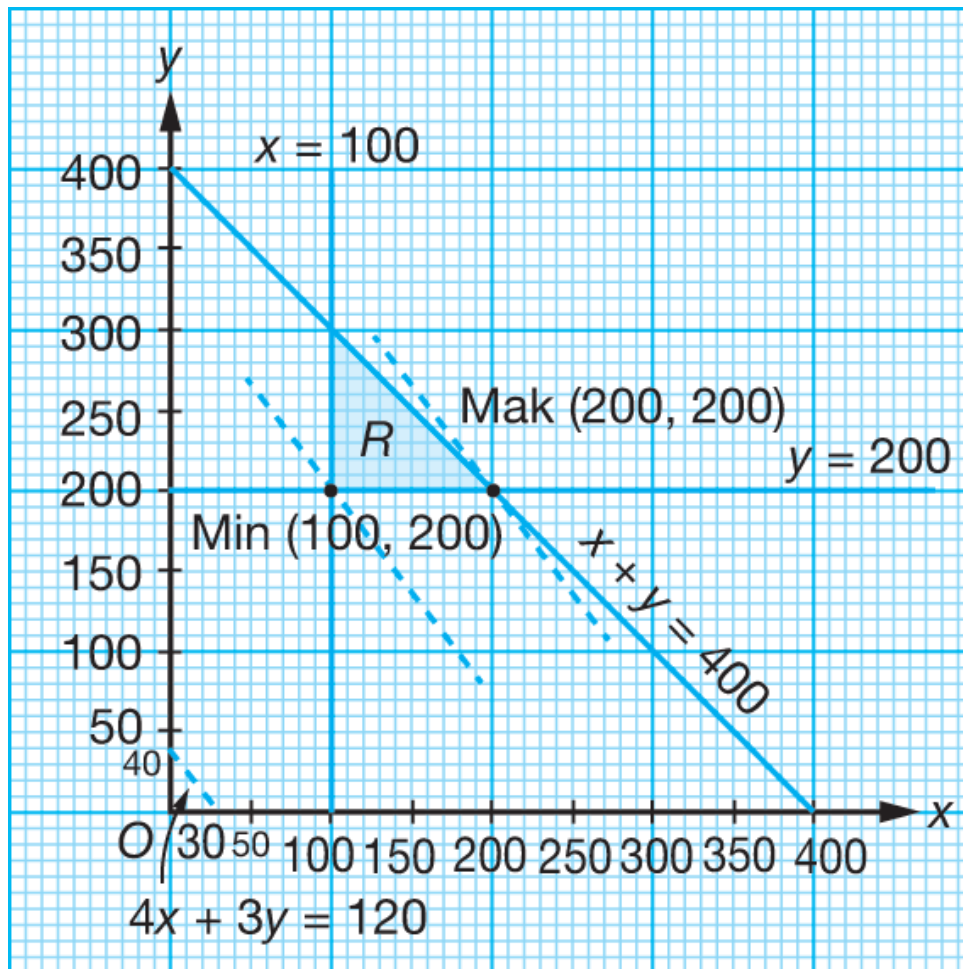
3 (a) $x + y \leq 90$

(b) $x \leq 2y$

(c) $y - x \leq 10$

Praktis Formatif 7.2

- 1 (a) $x \geq 100$, $y \geq 200$, $x + y \leq 400$
 (b)



- (c) Komisyon = $4x + 3y$

Lukis garis lurus $4x + 3y = 120$

Titik optimum (minimum) ialah (100, 200).

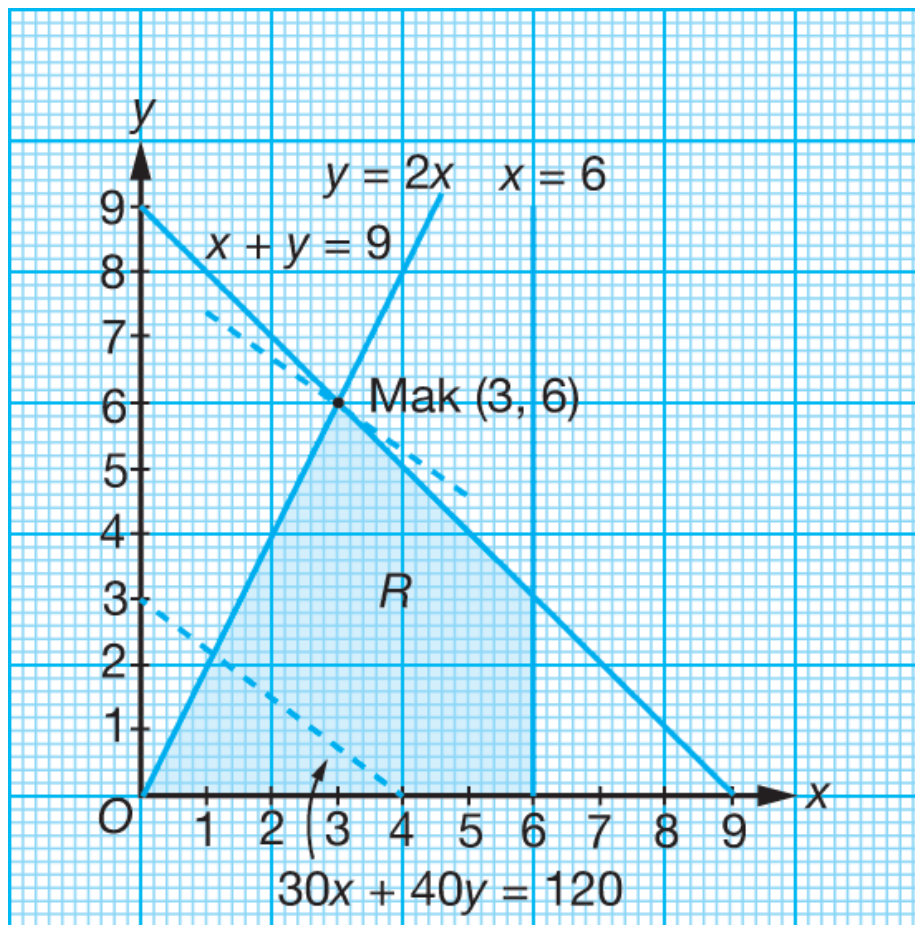
Komisyon minimum = $4(100) + 3(200) = \text{RM}1\ 000$

Titik optimum (maksimum) ialah (200, 200).

Komisyon maksimum = $4(200) + 3(200) = \text{RM}1\ 400$

2 (a) $x \leq 6$, $x + y \leq 9$, $y \leq 2x$

(b)



(c) Yuran bulanan = $30x + 40y$

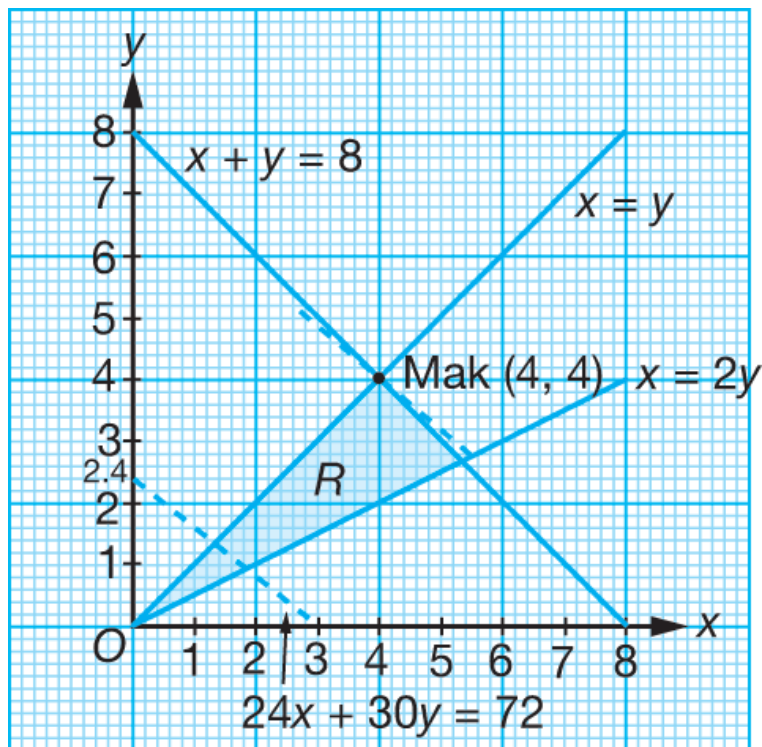
Lukis garis lurus $30x + 40y = 120$

Titik optimum ialah (3, 6).

Yuran maksimum = $30(3) + 40(6) = \text{RM}330$

3 (a) $x + y \leq 8$, $x \geq y$, $x \leq 2y$

(b)



(c) Upah = $24x + 30y$

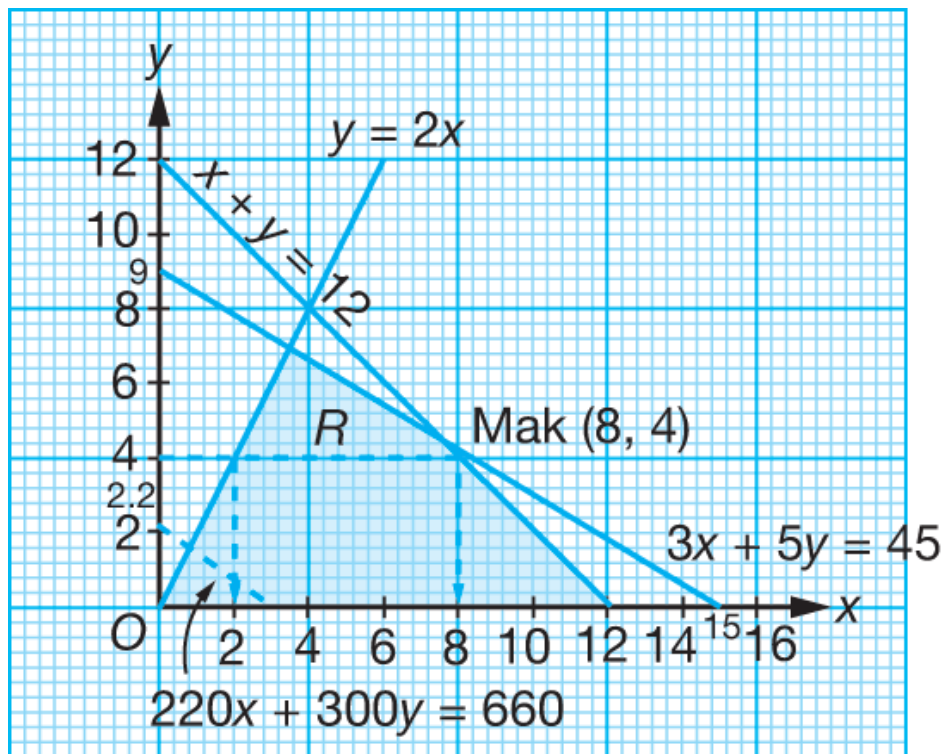
Lukis garis lurus $24x + 30y = 72$

Titik optimum ialah (4, 4).

Upah maksimum = $24(4) + 30(4) = \text{RM}216$

4 (a) $x + y \leq 12$, $y \leq 2x$, $3x + 5y \leq 45$

(b)



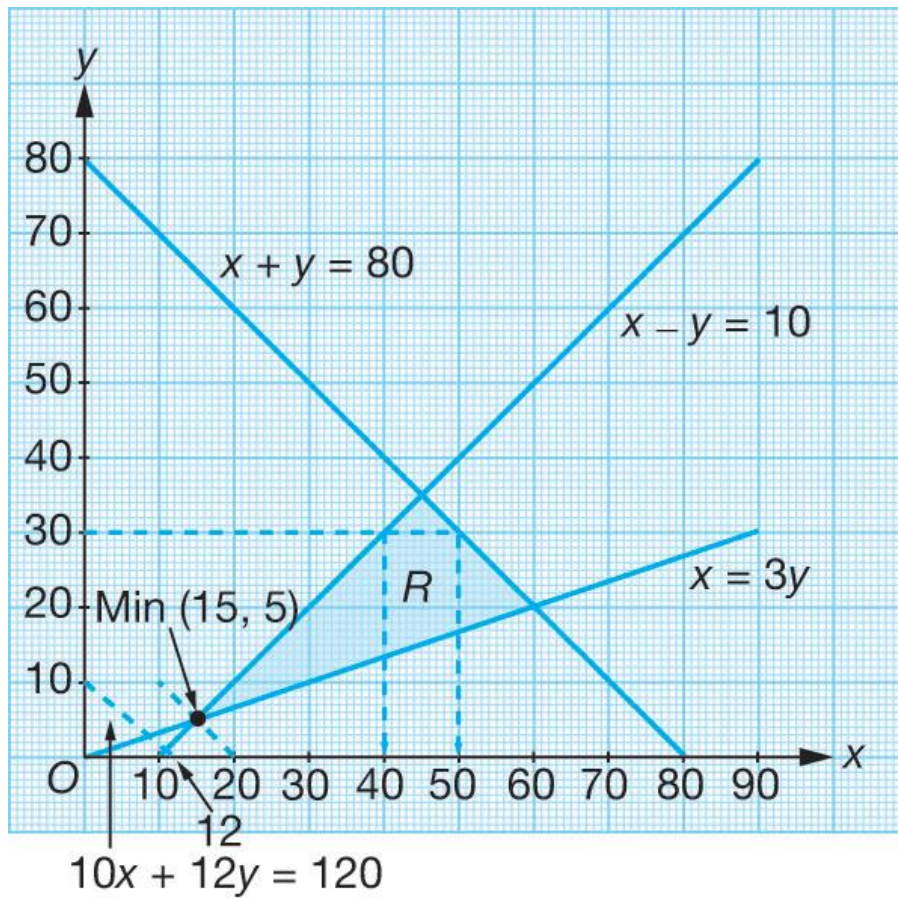
(c) (i) Apabila $y = 4$,
 x (minimum) = 2 buah
 x (maksimum) = 8 buah

(ii) Keuntungan = $220x + 300y$
 Lukis garis lurus $220x + 300y = 660$
 Titik optimum ialah (8, 4).

$$\text{Keuntungan maksimum} = 220(8) + 300(4) = \text{RM2 960}$$

5 (a) $x + y \leq 80$, $x \leq 3y$, $x - y \geq 10$

(b)



(c) (i) Apabila $y = 30$, $40 \leq x \leq 50$.

(ii) Kos = $10x + 12y$

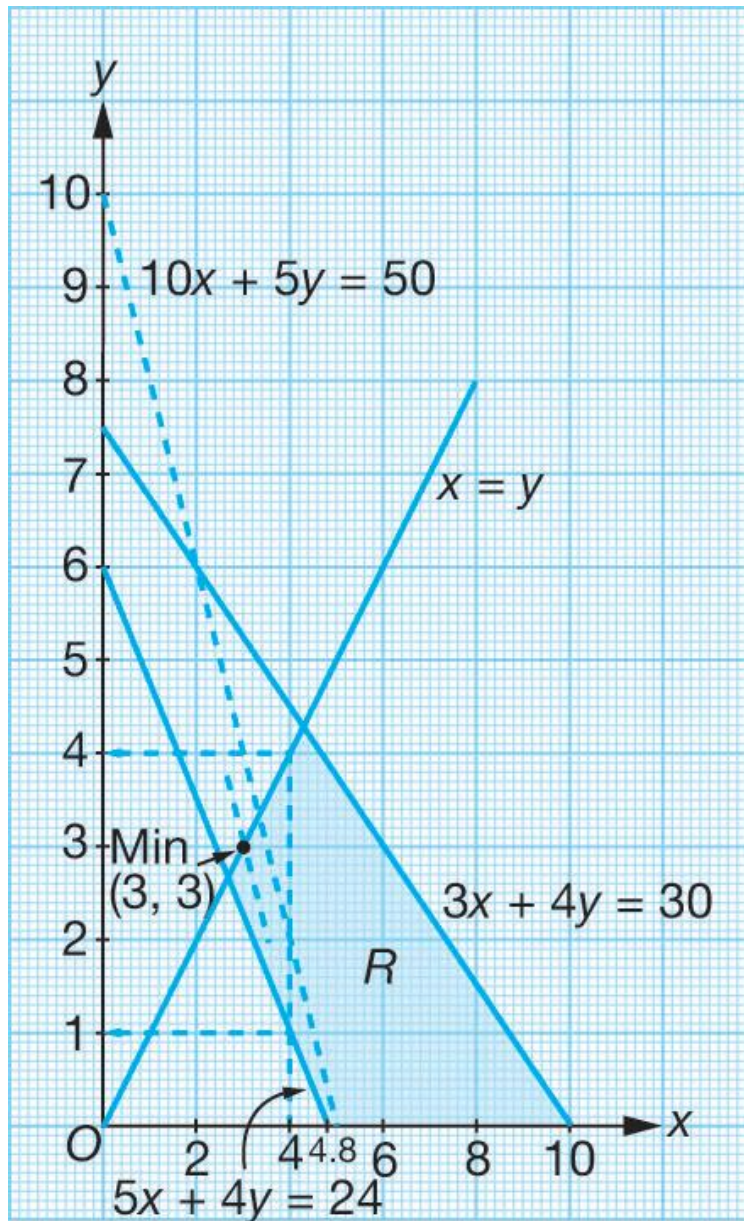
Lukis garis lurus $10x + 12y = 120$

Titik optimum (minimum) ialah (15, 5).

Kos minimum = $10(15) + 12(5) = \text{RM}210$

- 6 (a) $60x + 80y \leq 10 \times 60 \Rightarrow 3x + 4y \leq 30$,
 $75x + 60y \geq 6 \times 60 \Rightarrow 5x + 4y \geq 24$,
 $x \geq y$

(b)



(c) (i) Upah = $10x + 5y$

Lukis garis lurus $5x + 4y = 24$

Titik optimum (minimum) ialah (3, 3).

Upah minimum = $10x + 5y = 10(3) + 5(3) = \text{RM}45$

(ii) Apabila $x = 4$, y (mimimum) = 1

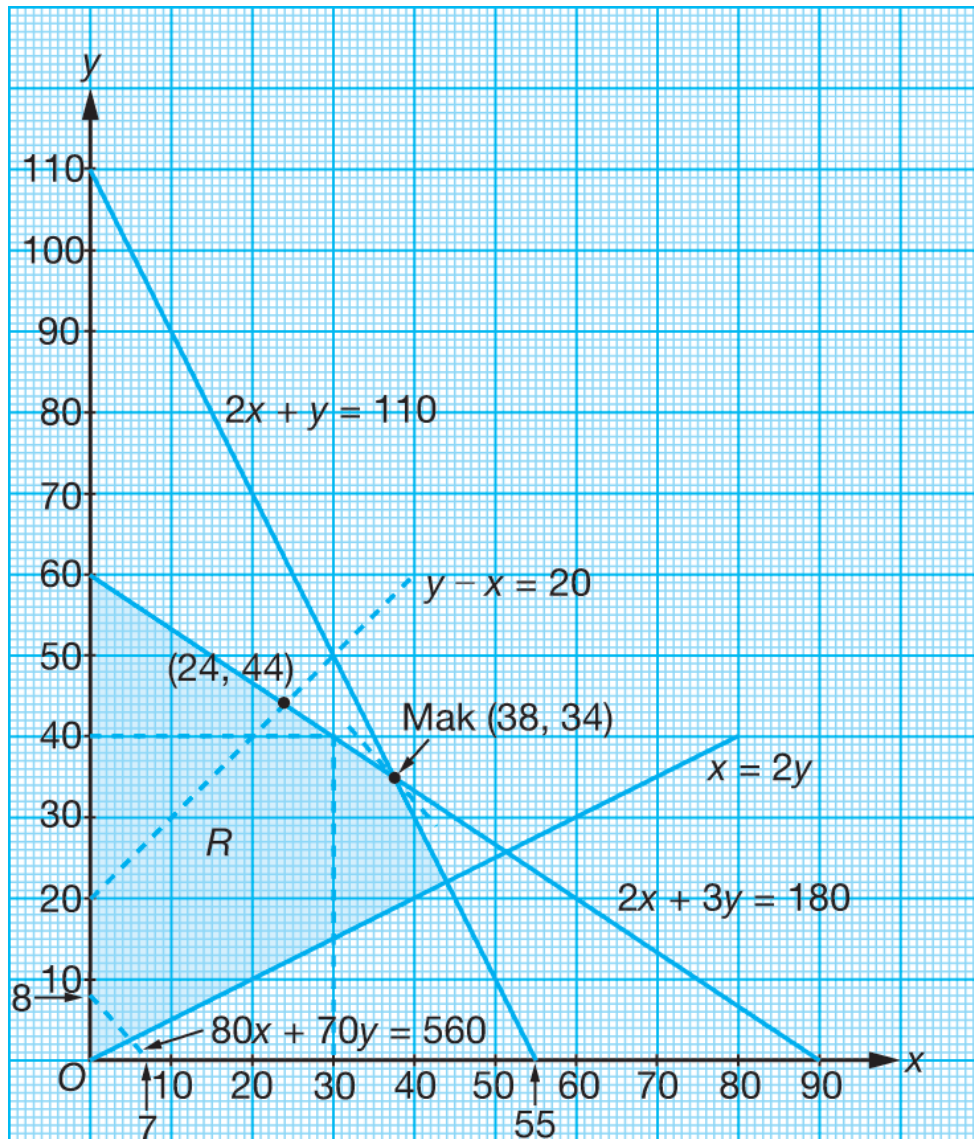
Upah minimum = $10(4) + 5(1) = \text{RM}45$

Apabila $x = 4$, y (maksimum) = 4

Upah maksimum = $10(4) + 5(4) = \text{RM}60$

- 7 (a) $80x + 120y \leq 7\,200 \Rightarrow 2x + 3y \leq 180$,
 $60x + 30y \leq 3\,300 \Rightarrow 2x + y \leq 110$,
 $x \leq 2y$

(b)



(c) (i) Keuntungan = $80x + 70y$

Lukis garis lurus $80x + 70y = 560$

Titik optimum ialah $(38, 34)$.

Keuntungan maksimum = $80(38) + 70(34) = 5\,420$ sen = RM54.20

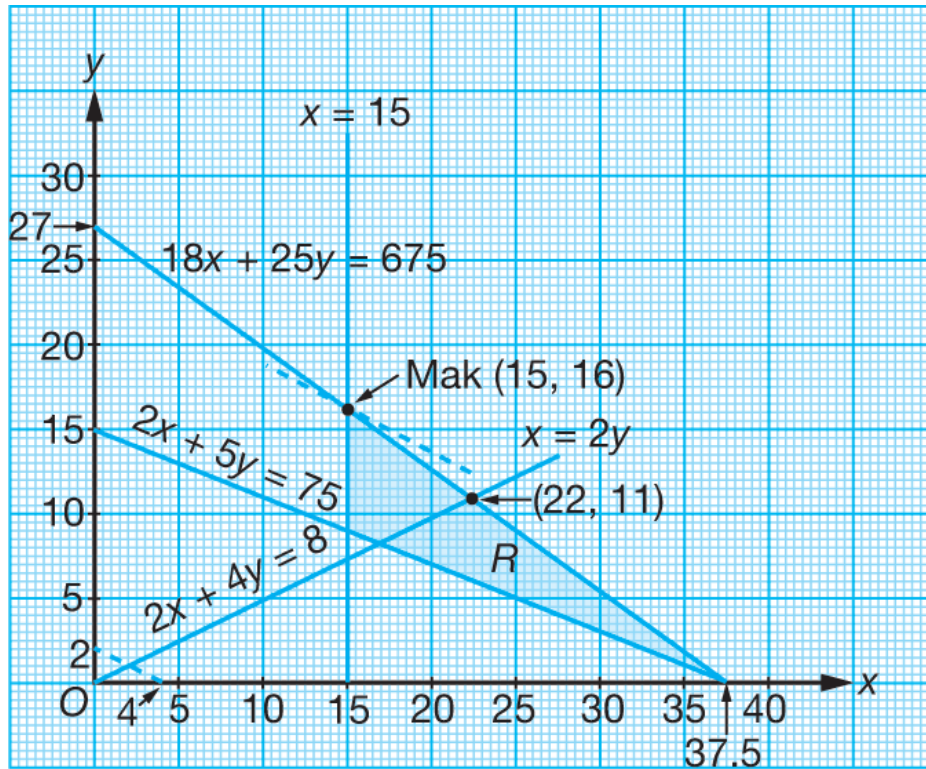
(ii) Lukis garis lurus $y - x = 20$

x (maksimum) = 24 biji kek

y (maksimum) = 44 biji ban

- 8 (a) $180x + 250y \leq 6750 \Rightarrow 18x + 25y \leq 675$,
 $60000x + 150000 \leq 2250000 \Rightarrow 2x + 5y \leq 75$,
 $x \geq 15$

(b)



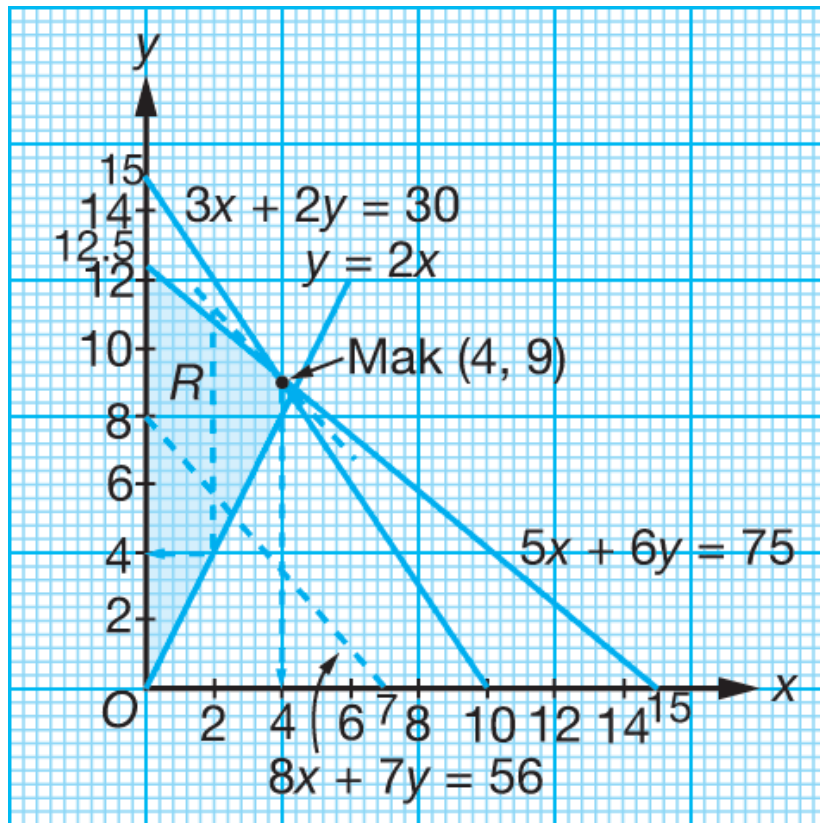
- (c) (i) Keuntungan = $20000x + 40000y$
 Lukis garis lurus $20000x + 40000y = 80000$
 $2x + 4y = 8$
 Titik optimum ialah $(15, 16)$.

$$\text{Keuntungan maksimum} = 20000(15) + 40000(16) = \text{RM}940000$$

- (ii) Lukis garis lurus $x = 2y$.
 x (maksimum) = 22 buah,
 y (maksimum) = 11 buah

- 9 (a) $50x + 60y \leq 750 \Rightarrow 5x + 6y \leq 75$,
 $60x + 40y \leq 10 \times 60 \Rightarrow 3x + 2y \leq 30$,
 $y \geq 2x$

(b)



(c) (i) Keuntungan = $8x + 7y$

Lukis garis lurus $8x + 7y = 56$

Titik optimum ialah (4, 9).

Keuntungan maksimum = $8(4) + 7(9) = \text{RM}95$

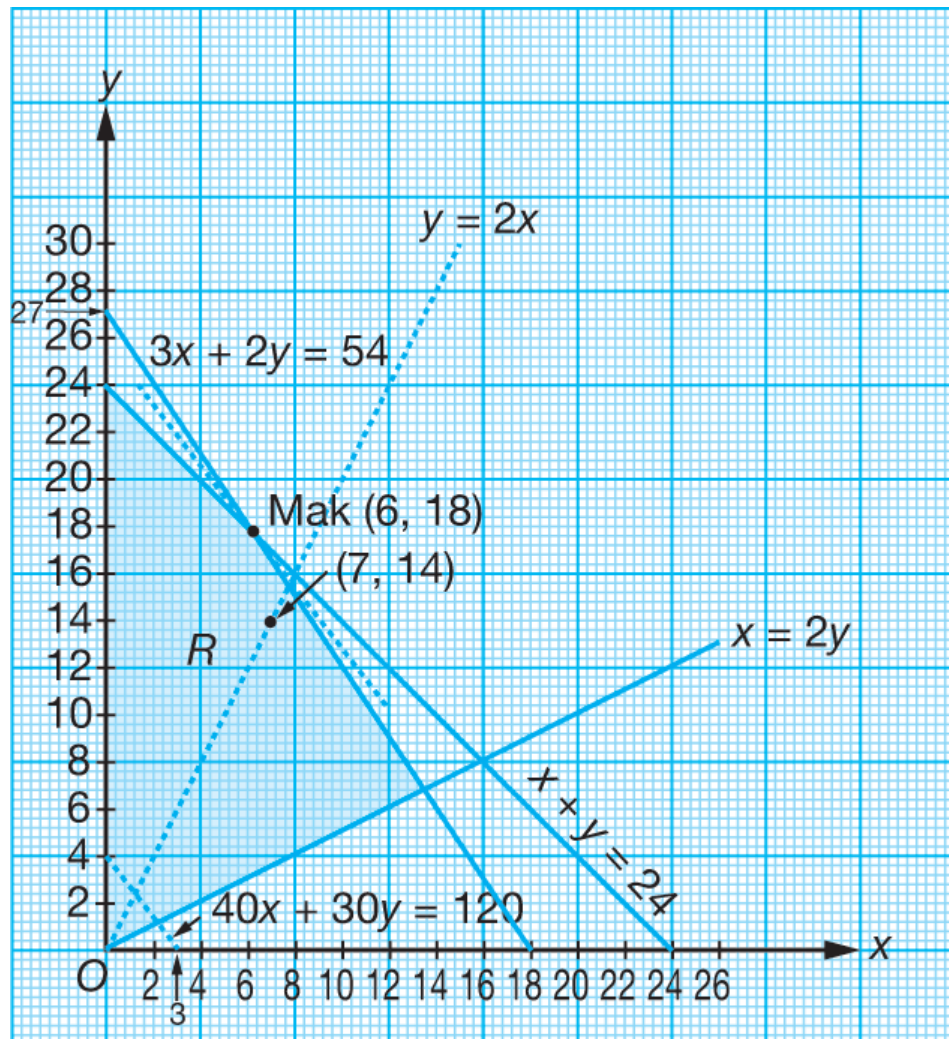
(ii) x (maksimum) = 4 buah bakul

(iii) Apabila $x = 2$, y (minimum) = 4 alas lantai

Praktis Sumatif 7

- 1 (a) $6x + 4y \leq 108 \Rightarrow 3x + 2y \leq 54$,
 $x + y \leq 24$, $y \geq x$

(b)



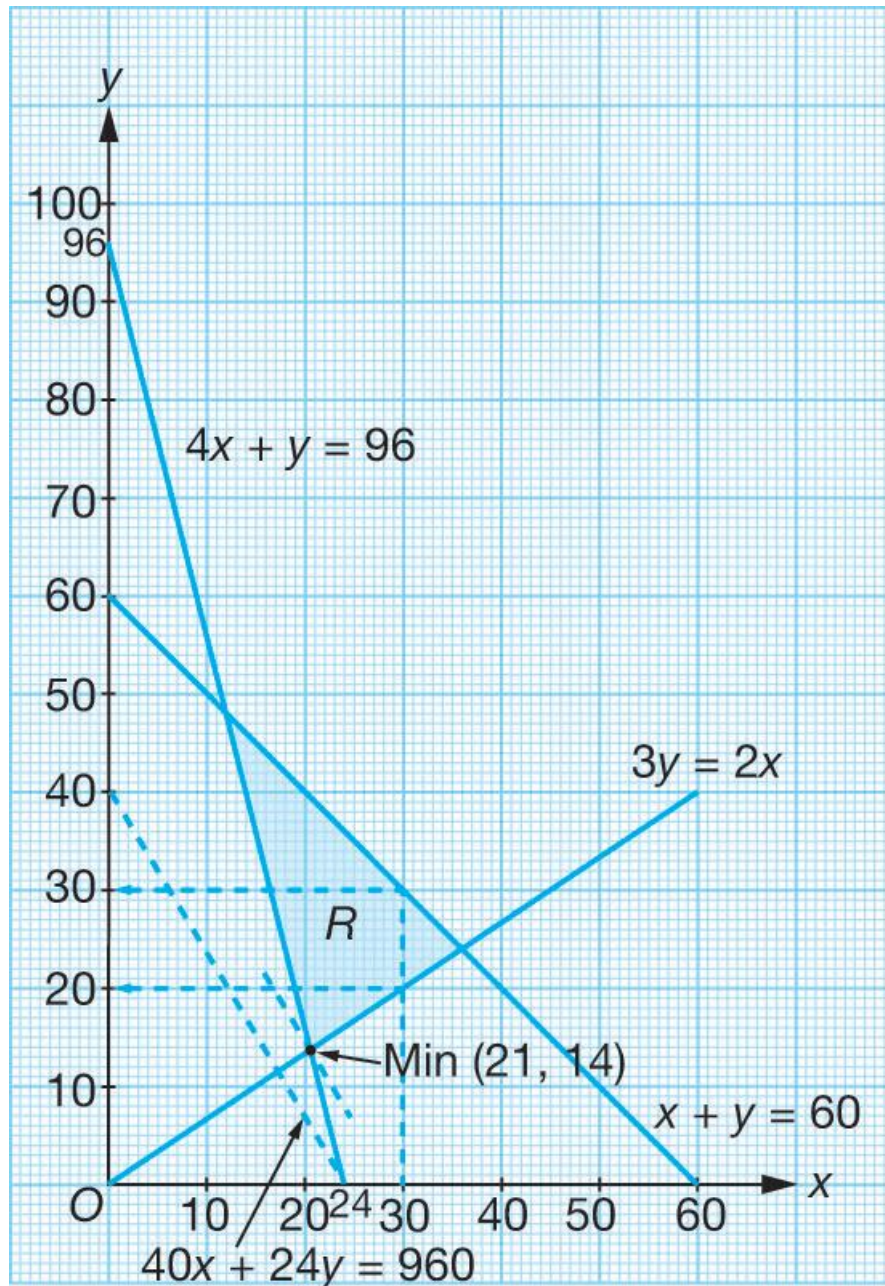
- (c) (i) Keuntungan = $40x + 30y$
 Lukis garis lurus $40x + 30y = 120$
 Titik optimum ialah (6, 18).

Keuntungan maksimum = $40(6) + 30(18) = \text{RM}780$

- (ii) Lukis garis lurus $y = 2x$
 x (maksimum) = 7 batang raket,
 y (maksimum) = 14 batang raket

2 (a) $2x + 2y \leq 120 \Rightarrow x + y \leq 60$,
 $4x + y \geq 96$
 $x \leq \frac{60}{100}(x + y) \Rightarrow x \leq \frac{3}{5}(x + y) \Rightarrow 5x \leq 3x + 3y \Rightarrow 3y \geq 2x$

(b)

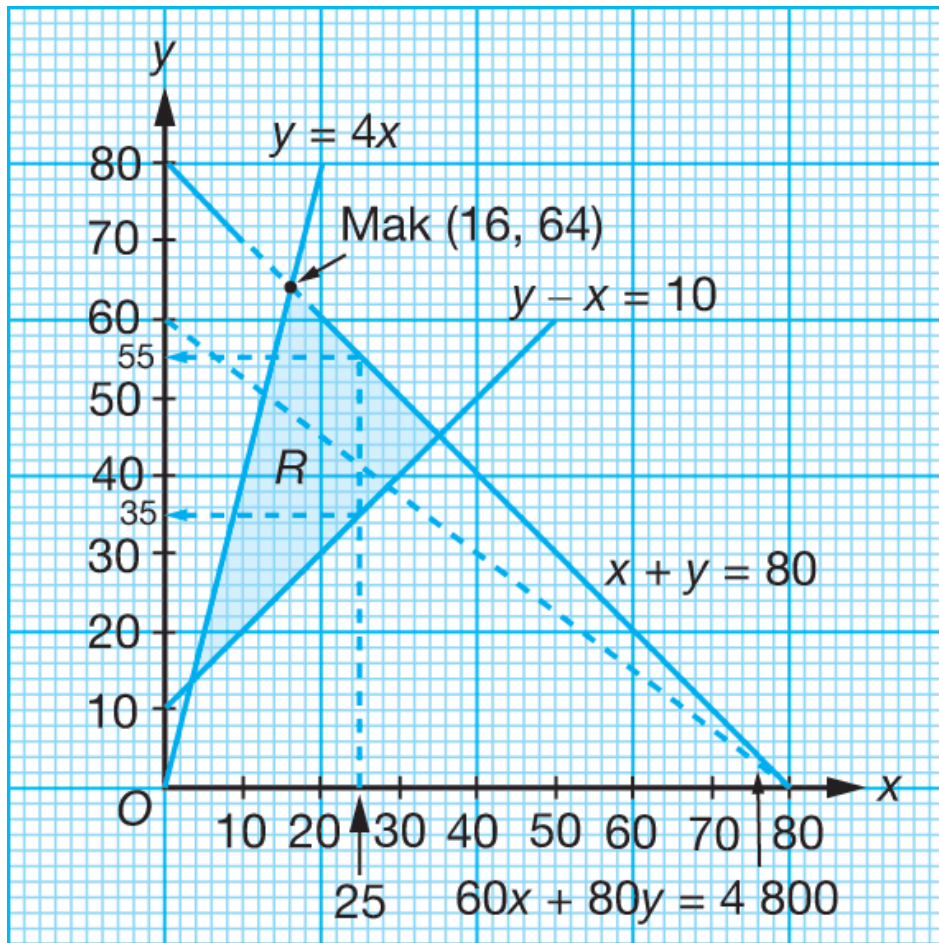


(c) (i) Kos = $40x + 24y$
 Lukis garis lurus $40x + 24y = 960$
 Titik optimum (minimum) ialah (21, 14)
 Kos minimum = $40(21) + 24(14) = \text{RM}1\ 176$

(ii) Apabila $x = 30$, $20 \leq y \leq 30$

3 (a) $x + y \leq 80$, $y \leq 4x$, $y - x \geq 10$

(b)



(c) (i) Apabila $x = 25$, $35 \leq y \leq 55$

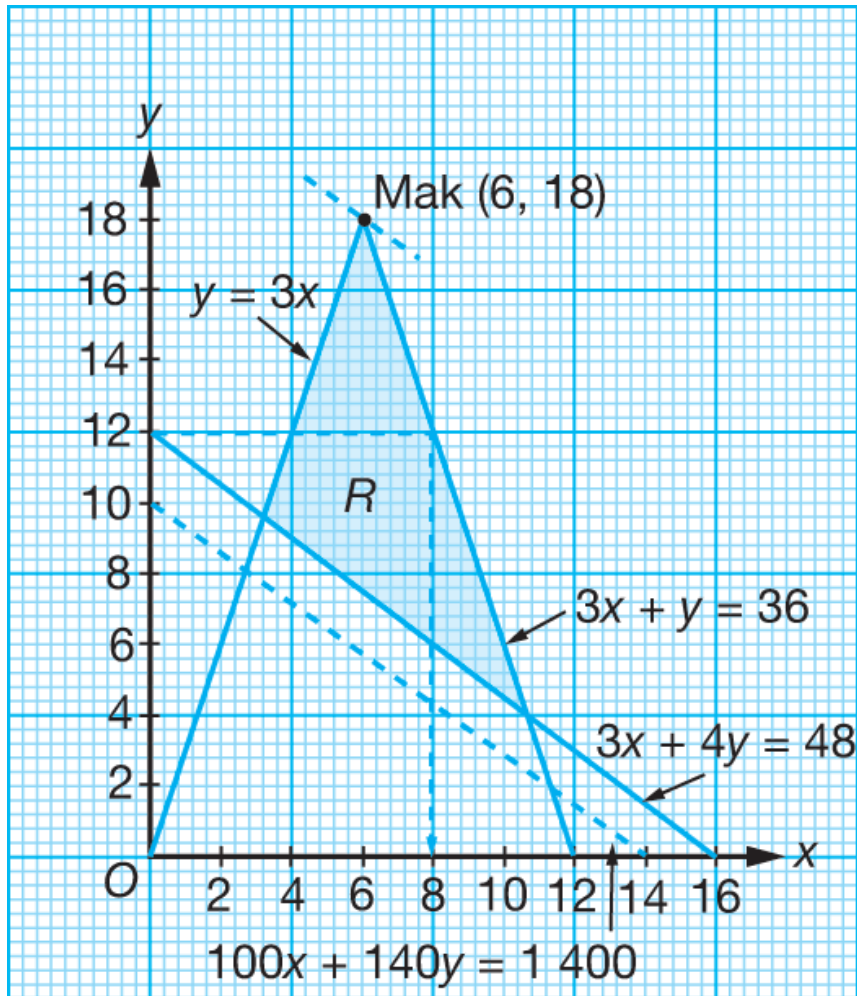
(ii) Peruntukan = $60x + 80y$

Lukis garis lurus $60x + 80y = 4800$

Titik optimum ialah (16, 64).

Peruntukan maksimum = $60x + 80y = 60(16) + 80(64) = \text{RM}6\ 080$

- 4 (a) $60x + 20y \leq 12 \times 60 \Rightarrow 3x + y \leq 36$,
 $30x + 40y \geq 8 \times 60 \Rightarrow 3x + 4y \geq 48$,
 $y \leq 3x$
- (b)



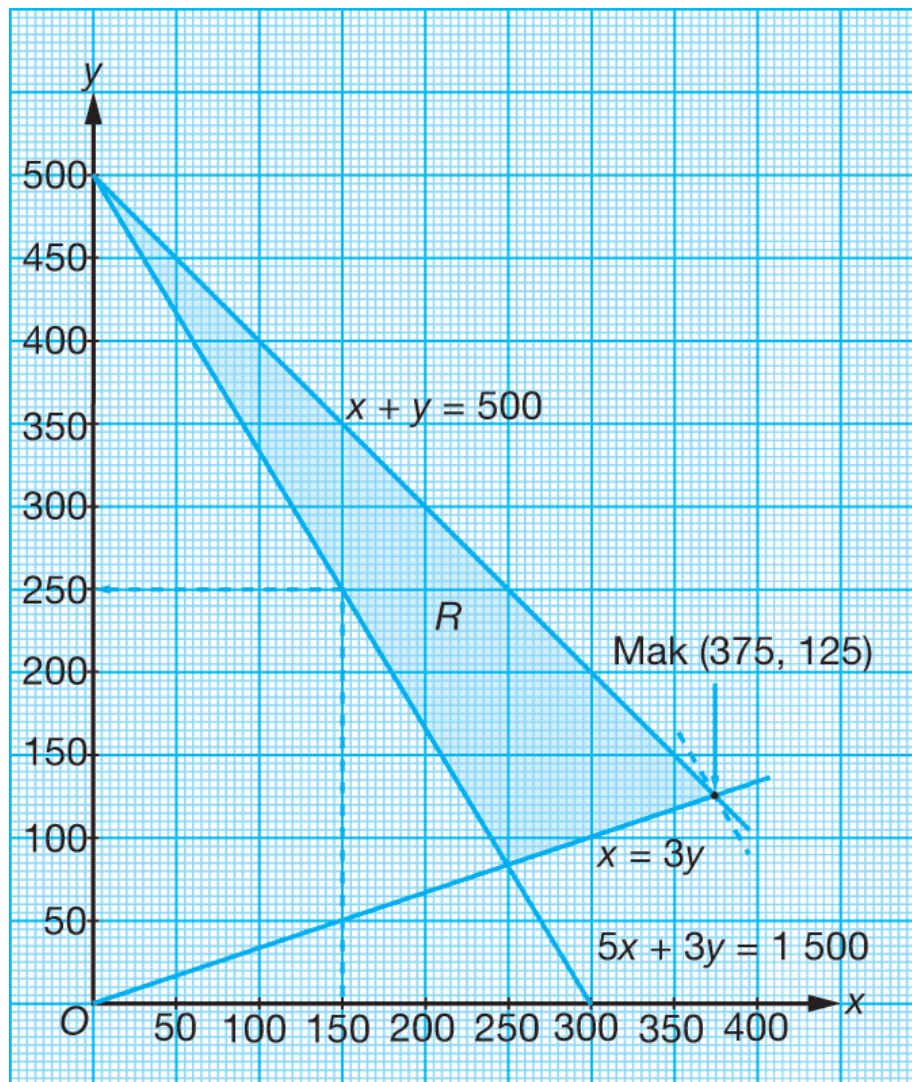
(c) (i) Apabila $y = 12$, x (maksimum) = 8 buah piala

(ii) Keuntungan = $100x + 140y$
 Lukis garis lurus $100x + 140y = 1400$
 Titik optimum ialah (6, 18).

Keuntungan maksimum = $100(6) + 140(18) = \text{RM}3\ 120$

5 (a) $x + y \leq 500$, $x \leq 3y$, $5x + 3y \geq 1500$

(b)



(c) (i) Jika $x = 150$, y (minimum) = 250 kotak fail poket

(ii) Keuntungan = $5x + 3y$

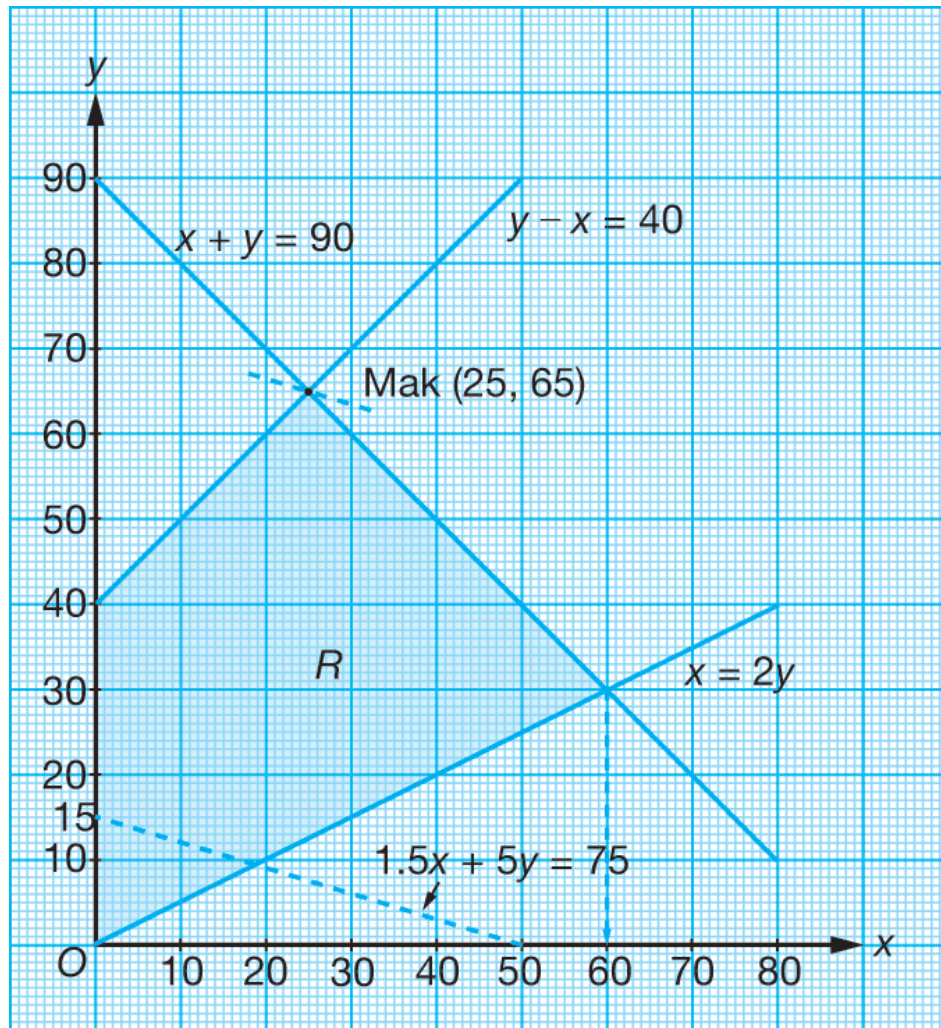
Lukis garis lurus $5x + 3y = 1500$

Titik optimum ialah (375, 125)

Keuntungan maksimum = $5(375) + 3(125) = \text{RM}2\,250$

6 (a) $x + y \leq 90$, $x \leq 2y$, $y - x \leq 40$

(b)



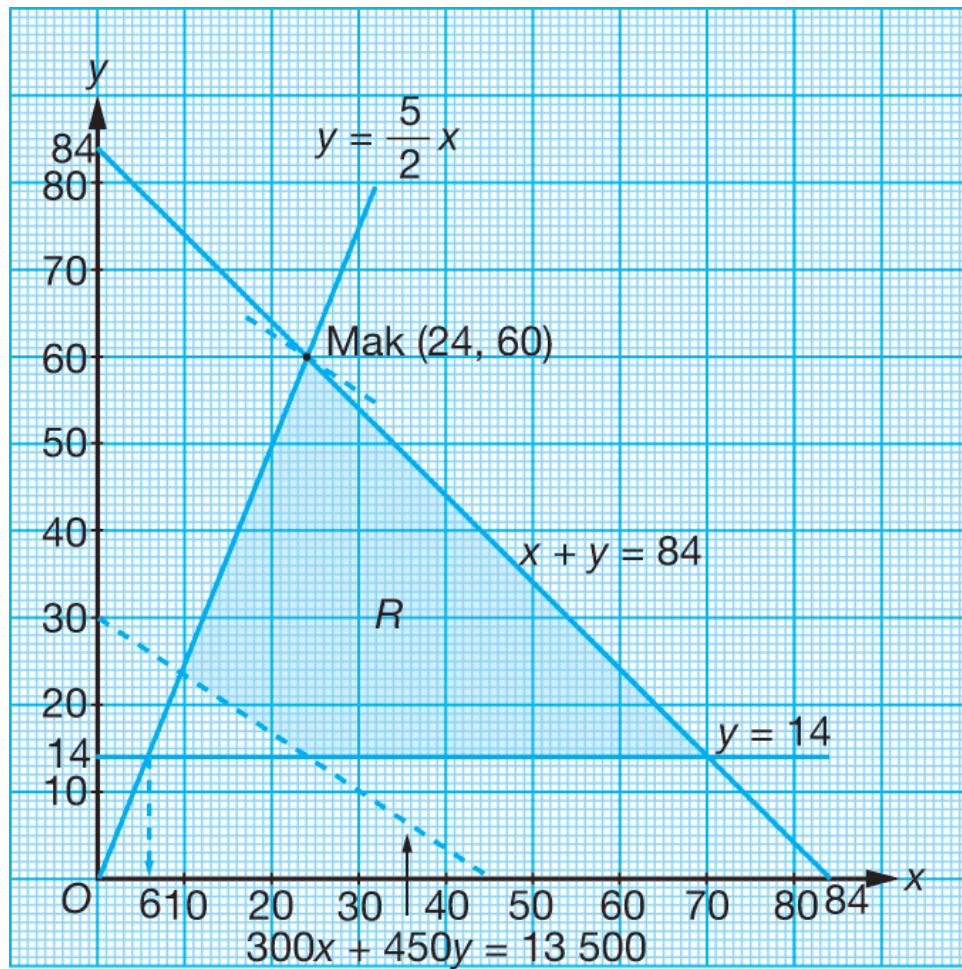
(c) (i) x (maksimum) = 60 batang pen

(ii) Kos = $1.5x + 5y$
 Lukis garis lurus $1.5x + 5y = 75$
 Titik optimum ialah (25, 65).

$$\text{Kos maksimum} = 1.5(25) + 5(65) = \text{RM}362.50$$

7 (a) $x + y \leq 84$, $y \geq 14$, $y \leq \frac{5}{2}x$

(b)

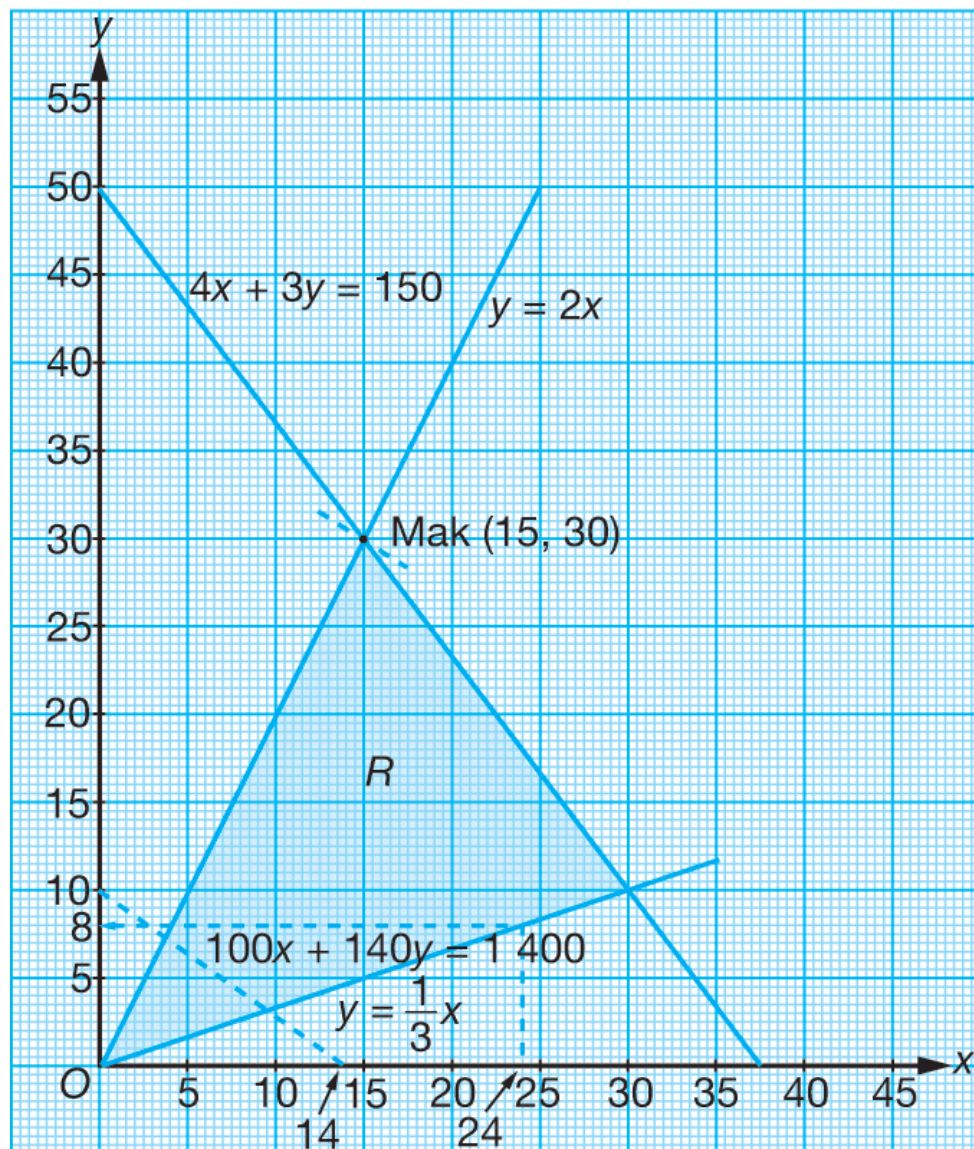


(c) (i) x (minimum) = 6 orang peserta

(ii) Yuran = $300x + 450y$
 Lukis garis lurus $300x + 450y = 13500$
 Titik optimum ialah (24, 60).

Yuran maksimum = $300(24) + 450(60) = \text{RM}34\,200$

- 8 (a) $y \leq 2x$, $y \geq \frac{1}{3}x$, $4x + 3y \leq 150$
 (b)

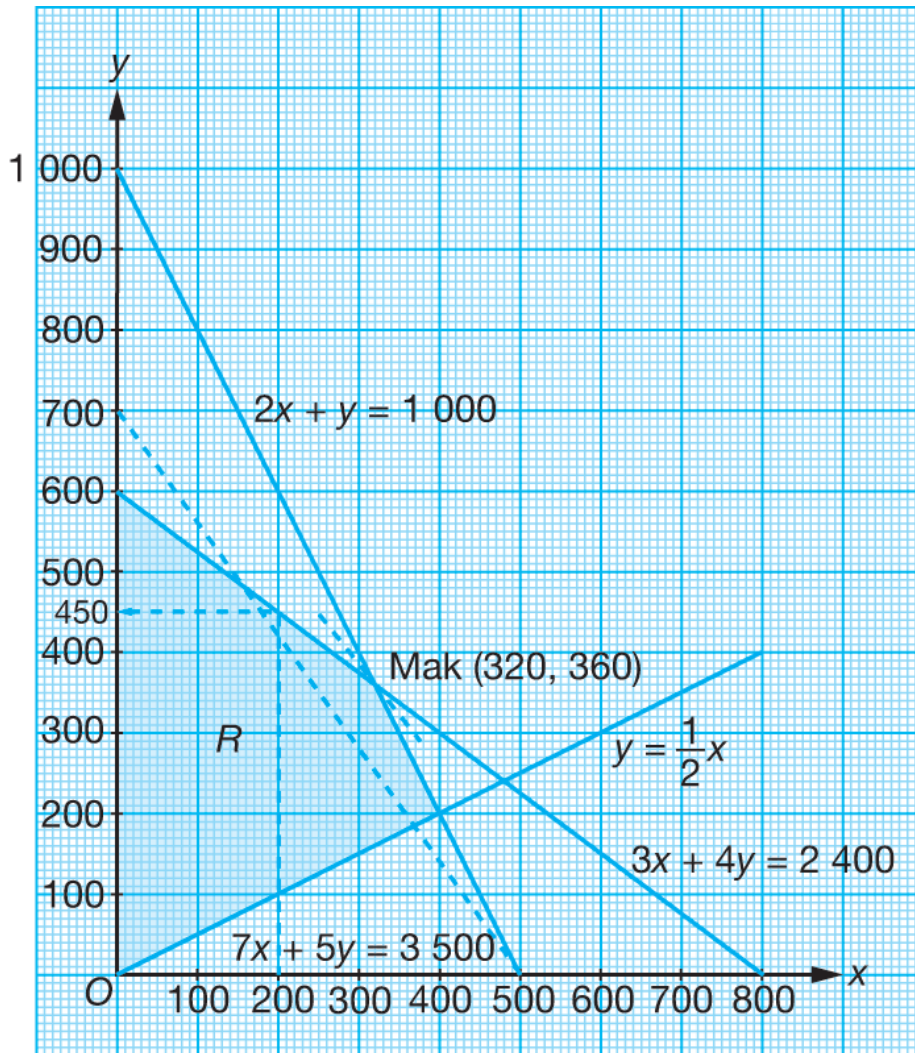


- (c) (i) Jika $x = 24$, y (minimum) = 8 tin cat
 (ii) Perbelanjaan = $100x + 140y$
 Lukis garis lurus $100x + 140y = 1400$
 Titik optimum ialah (15, 30).

Perbelanjaan maksimum = $100(15) + 140(30) = \text{RM}5\ 700$

9 (a) $3x + 4y \leq 2\,400$, $2x + y \leq 1\,000$, $y \geq \frac{1}{2}x$

(b)



(c) (i) Jika $x = 200$, y (maksimum) = 450 buah kerusi

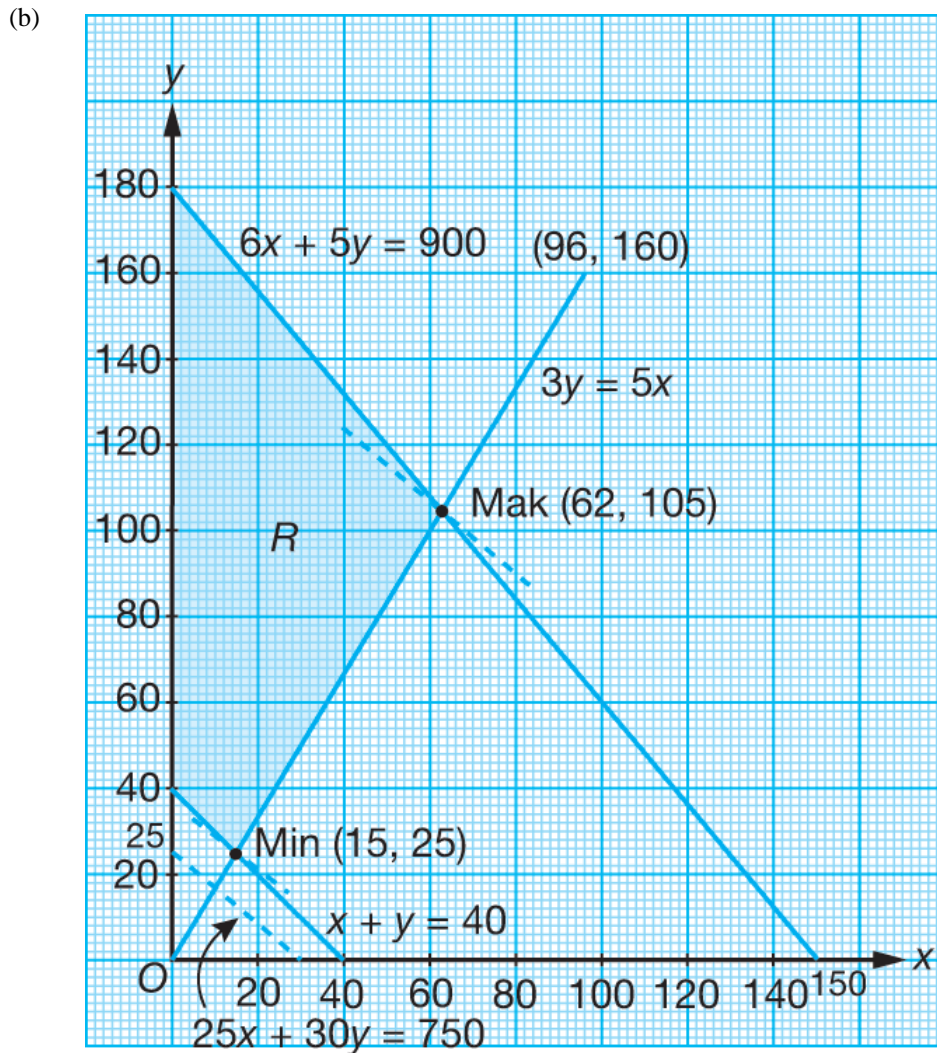
(ii) Keuntungan = $7x + 5y$

Lukis garis lurus $7x + 5y = 3\,500$

Titik optimum ialah $(320, 360)$.

$$\text{Keuntungan maksimum} = 7(320) + 5(360) = \text{RM}4\,040$$

10 (a) $x + y \geq 40$,
 $96x + 80y \leq 240 \times 60 \Rightarrow 6x + 5y \leq 900$,
 $\frac{x}{y} \leq \frac{3}{5} \Rightarrow 3y \geq 5x$



(c) Jumlah jualan = $25x + 30y$
 Lukis garis lurus $25x + 30y = 750$

Titik optimum (minimum) ialah (15, 25).
 Jumlah jualan minimum = $25(15) + 30(25) = \text{RM}1\ 150$

Titik optimum (maksimum) ialah (62, 105).
 Jumlah jualan maksimum = $25(62) + 30(105) = \text{RM}4\ 700$

Maka, $\text{RM}1\ 125 \leq \text{Jumlah jualan} \leq \text{RM}4\ 700$