

Excel Matematik SPM
Tingkatan 4 Bab 4
Operasi Set
Penyelesaian Lengkap

Praktis Formatif 4.1

1 (a) $\{b, h, k\}$

(b) $\{5, 6\}$

(c) $P = \{2, 3, 5, 7, \dots\}$

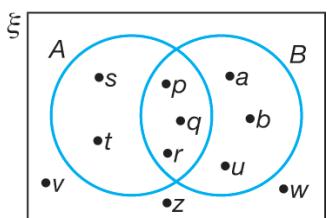
$$Q = \{1, 2, 3, 4, 5, 6\}$$

$$P \cap Q = \{2, 3, 5\}$$

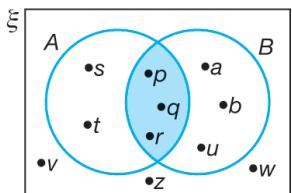
(d) $\{\quad\}$

2 (a) $\{p, q, r\}$

(b) (i)



(ii)



3 (a) $\{2, 4, 5\}$

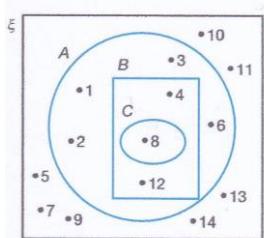
(b) $\{5, 7, 9\}$

4 $A = \{1, 2, 3, 4, 6, 8, 12\}$

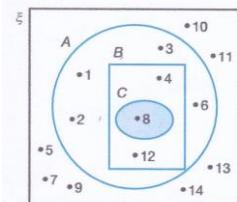
$$B = \{4, 8, 12\}$$

$$C = \{8\}$$

(a)

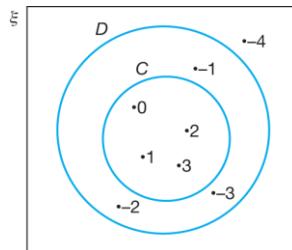


(b)

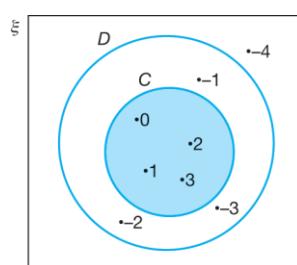


5 (a) $\{0, 1, 2, 3\}$

(b) (i)

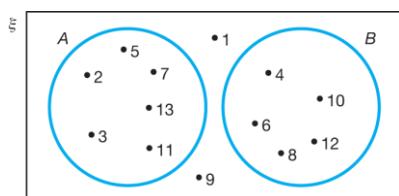


(ii)



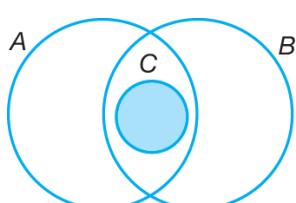
6 (a) $A = \{2, 3, 5, 7, 11, 13\}$

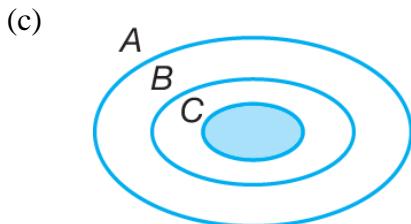
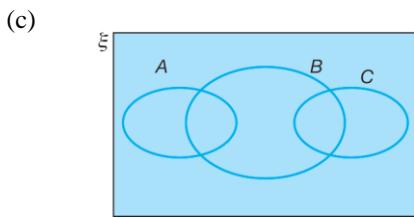
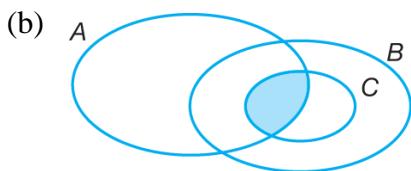
$$B = \{4, 6, 8, 10, 12\}$$



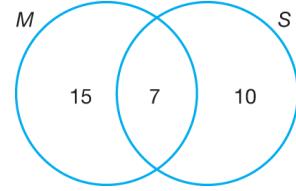
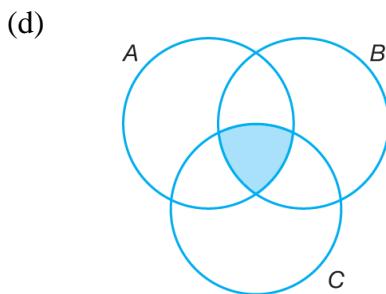
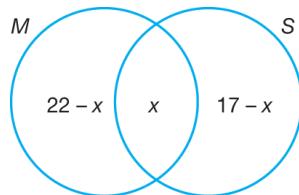
(b) $A \cap B = \{\quad\}$

7 (a)





10



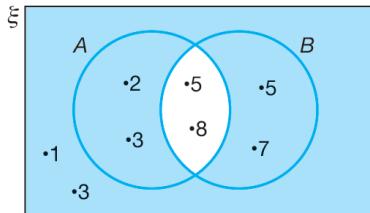
$$22 - x + x + 17 - x = 32$$

$$7 - x = 0$$

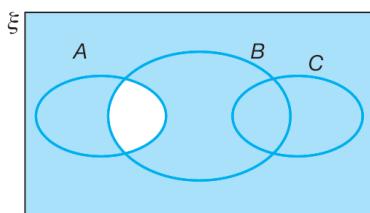
$$x = 7$$

- 8 (a) (i) $A \cap B = \{6, 8\}$
(ii) $(A \cap B)' = \{1, 2, 3, 4, 5, 7\}$

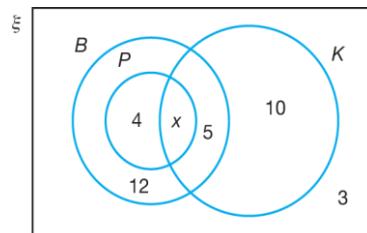
(b)



9 (a)



11

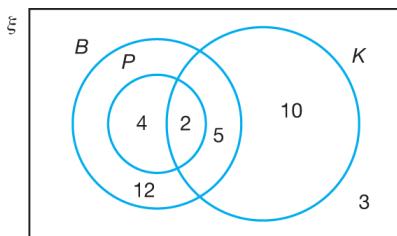
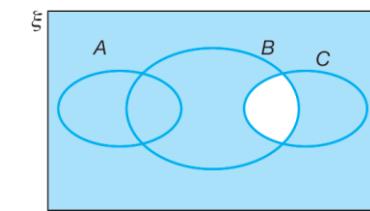


$$n(\xi) = 36$$

$$12 + 4 + x + 5 + 10 + 3 = 36$$

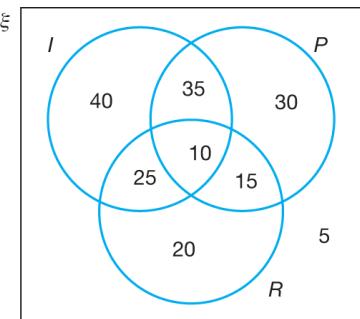
$$x = 2$$

(b)



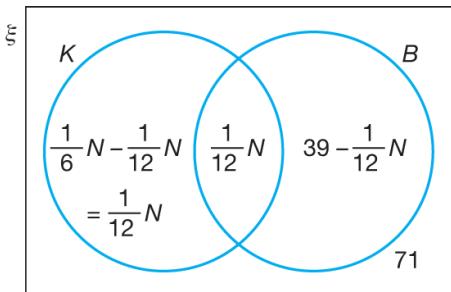
- (a) $n(B \cap P \cap K) = 2$ orang murid
 (b) $n(P' \cap K) = 5 + 10 = 15$ orang murid
 (c) $n(B \cap P') = 5 + 12 = 17$ orang murid
 (d) Bilangan murid yang gemar bermain sejenis permainan sahaja $= 12 + 10 = 22$ orang

12



- (a) $n(\text{internet dan telefon pintar tetapi bukan membaca}) = 35$ orang murid
 (b) $n(\text{dua aktiviti sahaja}) = 35 + 25 + 15 = 75$ orang murid
 (c) $n(\text{satu aktiviti sahaja}) = 40 + 30 + 20 = 90$ orang murid
 (d) $n(\text{tidak menggemari mana-mana aktiviti}) = 5$ orang murid

13



$$(a) \frac{1}{12}N + \frac{1}{12}N + \left(39 - \frac{1}{12}N + 71\right) = N$$

$$\frac{11}{12}N = 110$$

$$N = 120$$

Jumlah bilangan penuntut = 120 orang

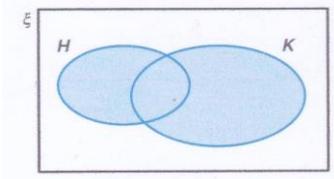
$$(b) \frac{1}{12}N = \frac{1}{12} \times 120 = 10 \text{ orang penuntut}$$

$$(c) 120 - 10 = 110 \text{ orang penuntut}$$

Praktis Formatif 4.2

- 1 (a) $\{5, 7, 15, 20\}$
 (b) $\{a, b, c, d, x, y, z\}$
 (c) $\{p, q, r, s\}$
- 2 $P = \{3, 6, 9, 12\}$
 $Q = \{1, 2, 3, 4, 6, 12\}$
 $P \cup Q = \{1, 2, 3, 4, 6, 9, 12\}$

3 (a)

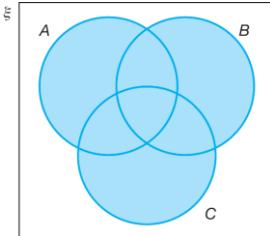


(b)

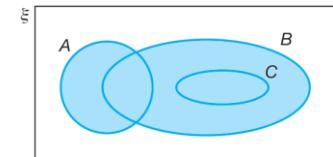
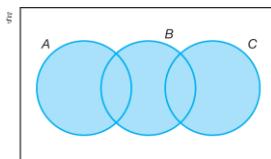


- 4 (a) $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$
 (b) $\{a, b, c, d, e, f, h, j, i, l, o\}$

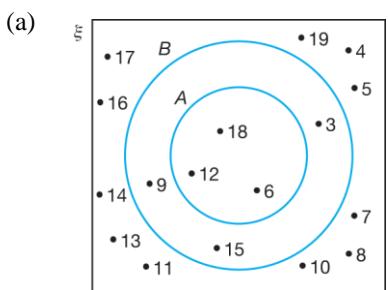
5 (a)



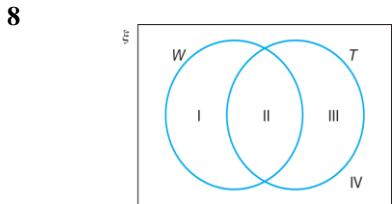
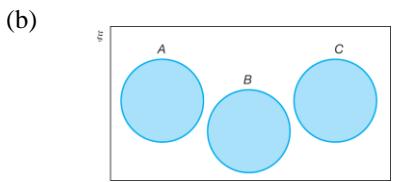
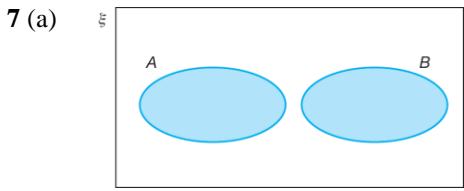
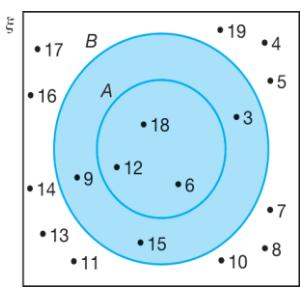
(b)



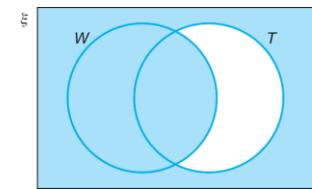
6 $A = \{6, 12, 18\}$
 $B = \{3, 6, 9, 12, 15, 18\}$



(b) (i) $A \cup B = \{3, 6, 9, 12, 15, 18\}$



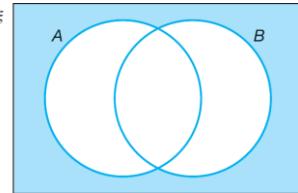
$W = \{\text{I, II}\}$
 $T' = \{\text{I, IV}\}$
 $W \cup T' = \{1, \text{II, IV}\}$



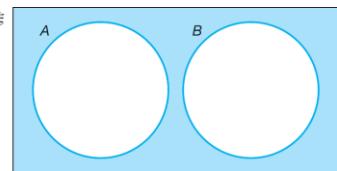
9 (a) $A \cup B = \{1, 3, 5, 6, 7, 9\}$
 $(A \cup B)' = \{2, 4, 8, 10\}$

(b) $P \cup Q = \{a, b, c, d, e, f\}$
 $(P \cup Q)' = \{g, h\}$

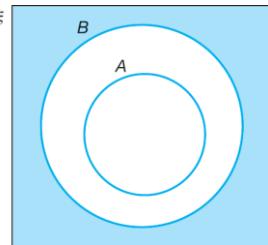
10 (a)



(b)

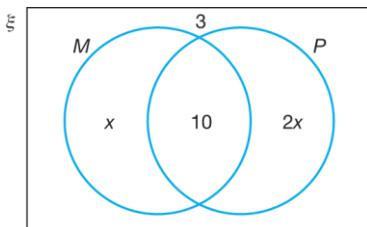


(c)



11 $n(K \cup M)' = n(L \cup M)'$
 $4 + 5 = x + 5$
 $x = 4$

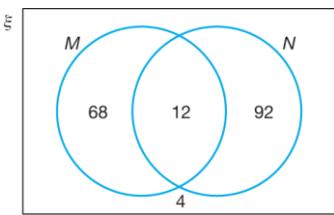
12



$$\begin{aligned} x + 10 + 2x + 3 &= 40 \\ 3x &= 27 \\ x &= 9 \\ n(\text{Pandu Puteri}) &= 10 + 2x \end{aligned}$$

$$= 10 + 2(9) \\ = 28$$

13



$$n(\xi) = 68 + 12 + 92 + 4 = 176 \text{ orang murid}$$

14 (a) $2k + k + 3 = 18$

$$\begin{aligned} 3k &= 15 \\ k &= 5 \end{aligned}$$

(b) $n(\xi) = 4k + 3 = 4(5) + 3 = 23$ orang peserta

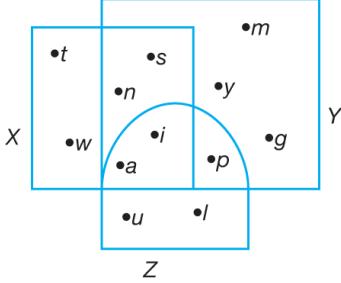
15 (a) $n(E \cap K) = 8$

$$\begin{aligned} 2 + 2h &= 8 \\ h &= 3 \end{aligned}$$

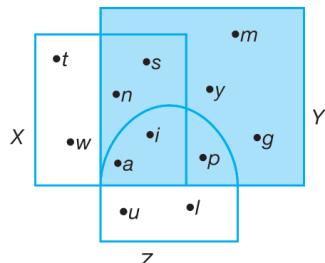
(b) Bilangan murid yang menggemari dua jenis minuman sahaja
 $= 5 + 1 + 2(3)$
 $= 12$

Praktis Formatif 4.3

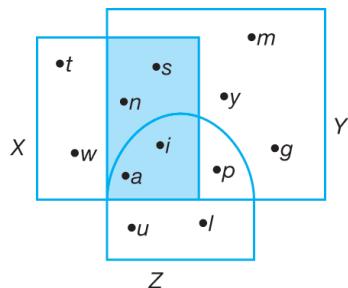
1 (a)



(b) (i)



(ii)



2 (a) (i) $A = \{1, 2, 4, 5, 10\}$

(ii) $B = \{4, 8\}$

(iii) $C = \{2, 4, 6, 8, 10\}$

(b) (i) $B \cap C = \{4, 8\}$

$A \cup (B \cap C) = \{1, 2, 4, 5, 8, 10\}$

(ii) $A \cup B = \{1, 2, 4, 5, 8, 10\}$

$C \cap (A \cup B) = \{2, 4, 8, 10\}$

(iii) $A \cup C = \{1, 2, 4, 5, 6, 8, 10\}$

$B \cap (A \cup C) = \{4, 8\}$

(c) (i) $n[A \cup (B \cap C)] = 6$

(ii) $n[C \cap (A \cup B)] = 4$

(iii) $n[B \cap (A \cup C)] = 2$

3 (a) $(P \cap Q) \cup R$

(b) $(P \cap R) \cup (Q \cap R)$ atau $(P \cup Q) \cap R$

4 $A = \{1, 3, 5, 7, 9\}$

$B = \{2, 4, 6, 8, 10\}$

$C = \{2, 3, 4, 5, 6\}$

(a) $A \cup B = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

$A \cup B \cap C = \{2, 3, 4, 5, 6\}$

$(A \cup B \cap C)' = \{1, 7, 8, 9, 10\}$

(b) $B' = \{1, 3, 5, 7, 9\}$

$B' \cap C = \{3, 5\}$

$A \cup (B' \cap C) = \{1, 3, 5, 7, 9\}$

(c) $A' = \{2, 4, 6, 8, 10\}$

$B \cup C = \{2, 3, 4, 5, 6, 8, 10\}$

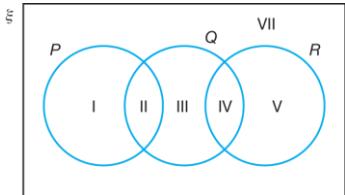
$A' \cap (B \cup C) = \{2, 4, 6, 8, 10\}$

(d) $A \cup B = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

$C' = \{1, 7, 8, 9, 10\}$

$A \cup B \cap C' = \{1, 7, 8, 9, 10\}$

5 (a)



$$C' = \{I, IV, V\}$$

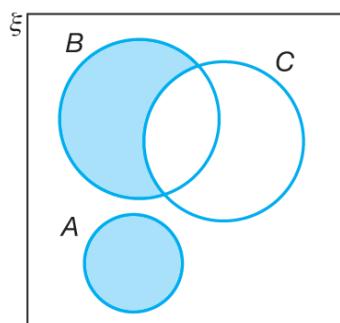
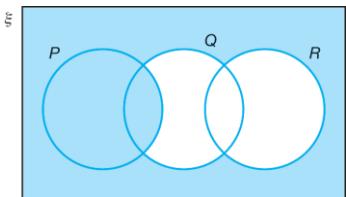
$$B = \{I, II\}$$

$$C' \cap B = \{I\}$$

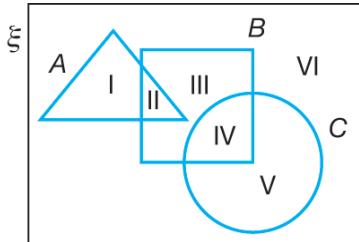
$$A = \{IV\}$$

$$(C' \cap B) \cup A = \{I, IV\}$$

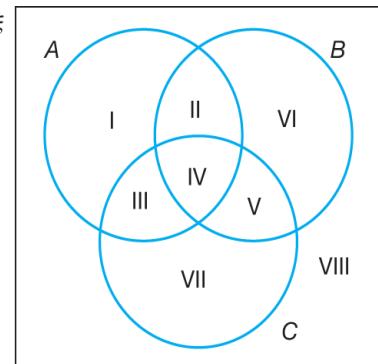
$$\begin{aligned}P &= \{I, II\} \\Q \cup R &= \{II, III, IV, V\} \\(Q \cup R)' &= \{I, VII\} \\P \cup (Q \cup R)' &= \{I, II, VII\}\end{aligned}$$



(b)

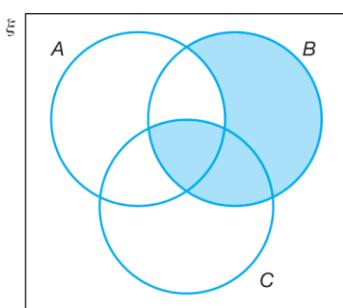
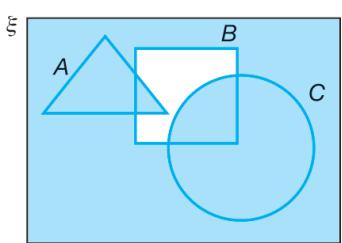


(b)

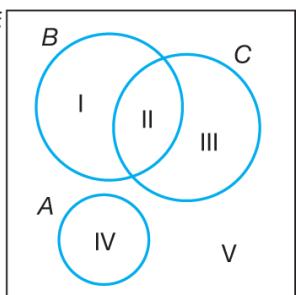


$$\begin{aligned}A &= \{I, II\} \\B' &= \{I, V, VI\} \\C &= \{IV, V\} \\A \cup B' \cup C &= \{I, II, IV, V, VI\}\end{aligned}$$

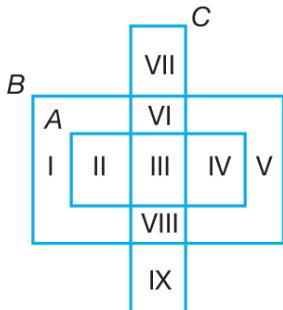
$$\begin{aligned}A' &= \{V, VI, VII, VIII\} \\C &= \{III, IV, V, VII\} \\A' \cup C &= \{III, IV, V, VI, VII, VIII\} \\B &= \{II, IV, V, VI\} \\(A' \cup C) \cap B &= \{IV, V, VI\}\end{aligned}$$



6 (a)



7

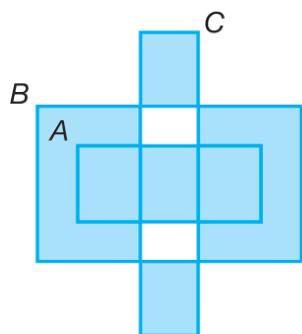


$$B \cap C = \{III, VI, VIII\}$$

$$(B \cap C)' = \{I, II, IV, V, VII, IX\}$$

$$A = \{III, III, IV\}$$

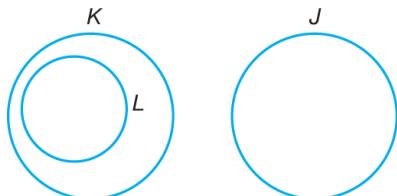
$$(B \cap C)' \cup A = \{I, II, III, IV, V, VII, IX\}$$



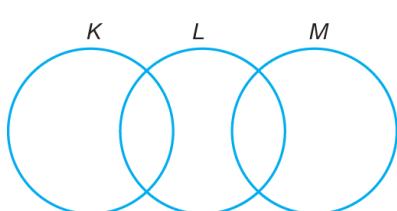
$$8 (Q' \cap P) \cap R$$

$$9 (A \cap B) \cup (B' \cap C)$$

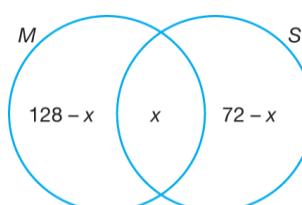
10



11



12



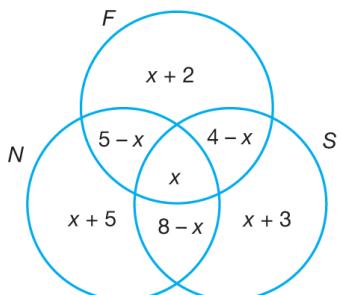
$$n(\xi) = 160$$

$$128 + 72 - x = 160$$

$$x = 40$$

Maka, bilangan murid yang mencapai gred A dalam kedua-dua Matematik dan Sains ialah 40 orang.

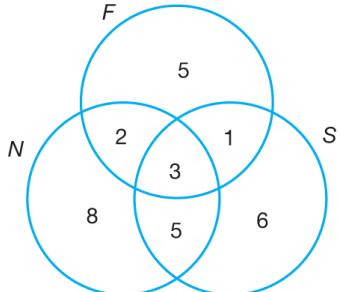
13



$$n(\xi) = x + 27 = 30$$

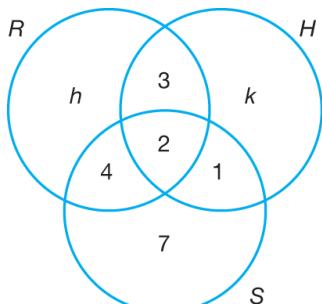
$$x = 3$$

(a)



- (b) (i) Bilangan murid yang gemar membaca ketiga-tiga jenis buku ialah 3 orang.
- (ii) Bilangan murid yang gemar membaca buku bukan fiksyen atau buku sukan tetapi bukan buku cerita fiksyen ialah $8 + 5 + 6 = 19$ orang.
- (iii) Bilangan murid yang gemar membaca buku cerita fiksyen dan buku sukan sahaja = 1 orang.

14 (a)



(b) $n(\xi) = 40$
 $h + k + 17 = 40$
 $h + k = 23 \dots (1)$

$n(R) = n(H)$
 $h + 9 = k + 6$
 $h - k = -3 \dots (2)$

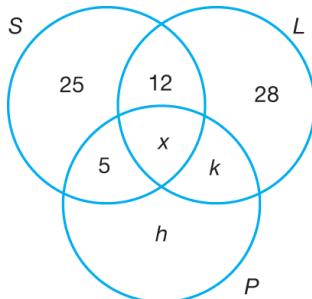
(1) - (2) : $2k = 26$
 $k = 13$

Daripada (1) :

$h + 13 = 23$
 $h = 10$

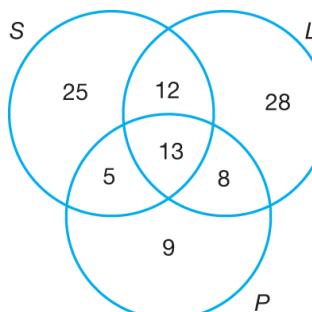
(c) Bilangan murid yang mempunyai dua ciri sahaja $= 3 + 4 + 1 = 8$ orang

15

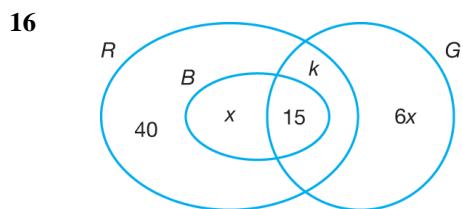


(a) $n(S) = 55$
 $x + 42 = 55$
 $x = 13$
 $n(L) = 61$
 $40 + 13 + k = 91$
 $k = 8$

$n(\xi) = 100$
 $h + 91 = 100$
 $h = 9$

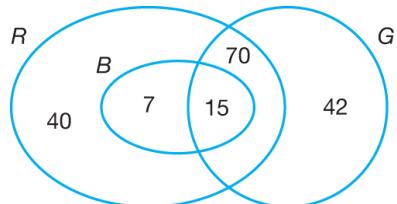


Bilangan penonton yang gemar menonton kisah menakutkan atau lucu dan penyiasatan $= 5 + 13 + 8 = 26$ orang.



(a) $n(B) = \frac{1}{6} \times n(R)$
 $x + 15 = \frac{1}{6}(x + k + 55)$
 $x + 15 = \frac{1}{6}(x + 70 + 55)$
 $6x + 90 = x + 125$
 $5x = 35$
 $x = 7$

(b)



Bilangan ahli yang menyertai tidak lebih daripada dua kelab
 $= 40 + 7 + 70 + 42$
 $= 159$ orang

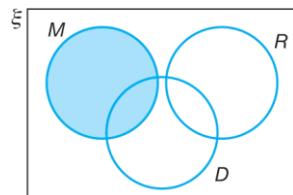
Praktis Sumatif 4

Soalan Objektif

1 Set yang mewakili rantau berlorek ialah $P' \cup Q$.
Jawapan: B

2 Set yang mewakili rantau berlorek ialah $(P \cup R)' \cap Q$.
Jawapan: C

3 Gambar rajah Venn yang mewakili murid yang menggemari nanas tetapi bukan belimbing ialah



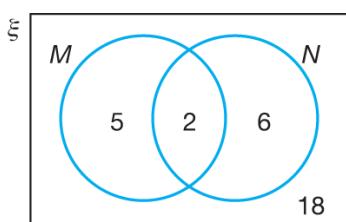
Jawapan: C

4 $M = \{x : x \text{ ialah gandaan } 5\}$
 $M = \{10, 15, 20, 25, 30, 35, 40\}$

$N = \{x : x \text{ ialah gandaan } 4\}$
 $N = \{12, 16, 20, 24, 28, 32, 36, 40\}\}$

$M \cap N = \{20, 40\}$
 $(M \cup N)' = \{11, 13, 14, 17, 18, 19, 21, 22, 23, 26, 27, 29, 31, 33, 34, 37, 38, 39\}$

Gambar rajah Venn yang dikehendaki ialah



Jawapan: D

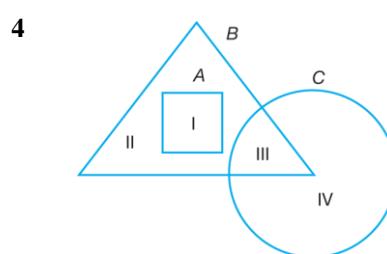
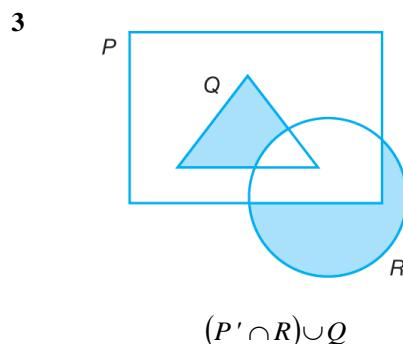
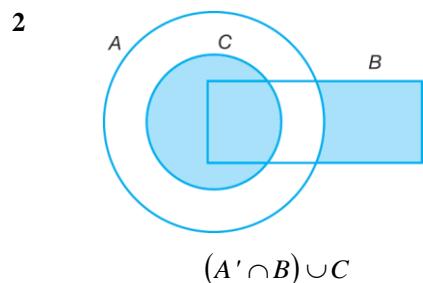
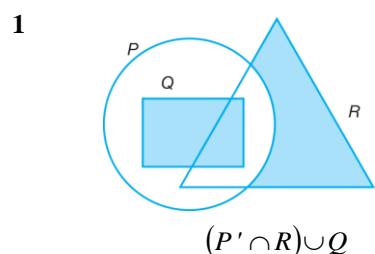
5 $P = \{2, 4, 6, 8, 10\}$
 $Q = \{2, 3, 5, 7\}$
 $R = \{1, 2, 3, 4, 5\}$
 $P' = \{1, 3, 5, 7, 9\}$
 $P' \cup R = \{1, 2, 3, 4, 5, 7, 9\}$
 $Q' = \{1, 4, 6, 8, 9, 10\}$
 $Q' \cap (P' \cup R) = \{1, 4, 9\}$

Jawapan: A

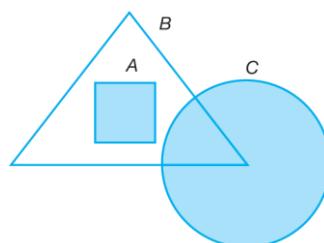
6 Set yang mewakili rantau berlorek ialah $(P \cup R)'$.

Jawapan: C

Soalan Struktur

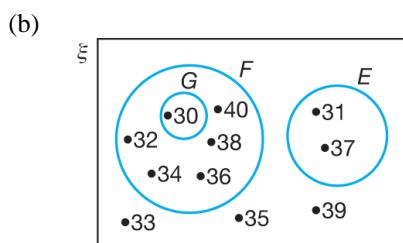


$A = \{I\}$
 $B' = \{IV\}$
 $A \cup B' = \{I, IV\}$
 $C = \{III, IV\}$
 $(A \cup B') \cup C = \{I, III, IV\}$



5 (a) $A \cup (B \cap C)$
(b) $(A \cup B) \cap C'$

6 (a) $\xi = \{30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40\}$
 $E = \{31, 37\}$
 $F = \{30, 32, 34, 36, 38, 40\}$
 $G = \{30\}$

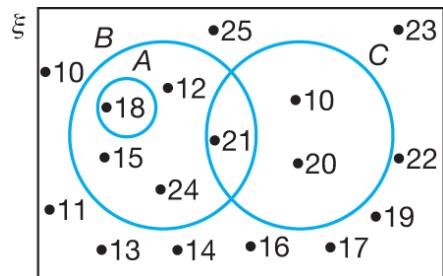


- (c) $F \cap G = \{30\}$
 $E \cup (F \cap G) = \{30, 31, 37\}$
(d) $n[E \cup (F \cap G)] = 3$

7 (a) $\xi = \{10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25\}$

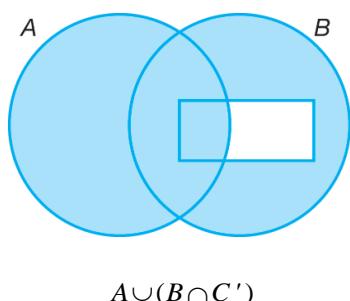
$$\begin{aligned}A &= \{18\} \\B &= \{12, 15, 18, 21, 24\} \\C &= \{10, 20, 21\}\end{aligned}$$

(b)



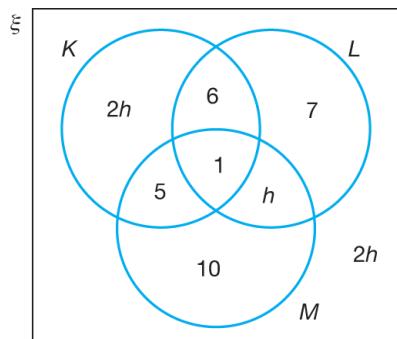
- (c) $(A \cap B) \cup (B \cap C)$
 $= \{18\} \cup \{21\}$
 $= \{18, 21\}$
(d) $n(B \cap C)' = 15 + 1 - 1 = 15$

8



$$A \cup (B \cap C')$$

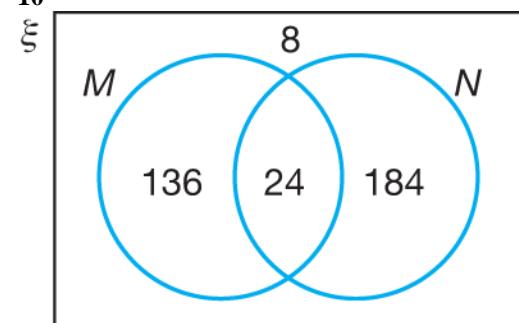
9



- (a) $n(K) = n(L \cup M)'$
 $2h + 12 = 4h$
 $2h = 12$
 $h = 6$

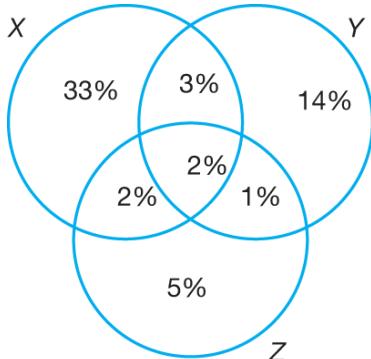
$$\begin{aligned}(b) n[(K \cap L) \cup (L \cap M) \cup (K \cap M)'] &= 2h + 7 + 10 + 2h \\&= 4h + 17 \\&= 4(6) + 17 \\&= 41\end{aligned}$$

10



- (a) Jumlah bilangan murid
 $= 136 + 24 + 184 + 8$
 $= 352$
- (b) Bilangan murid yang gemar membaca sejenis majalah sahaja
 $= 136 + 184$
 $= 320$ orang

11 (a)

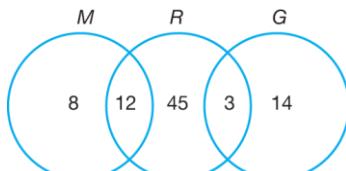


- (b) Peratusan pelanggan yang membeli satu jenama pencuci muka sahaja
 $= 33\% + 14\% + 5\%$
 $= 52\%$

Bilangan pelanggan yang membeli satu jenama pencuci muka sahaja

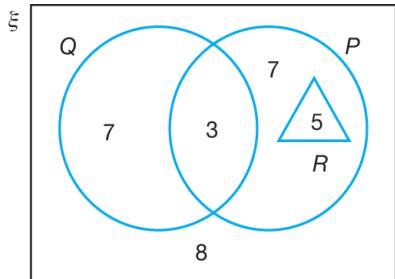
$$\begin{aligned}&= \frac{52}{100} \times 10\ 000 \\&= 5\ 200\text{ orang}\end{aligned}$$

12 (a)



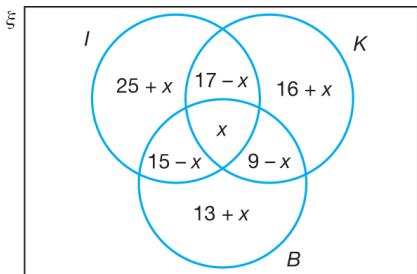
- (b) Bilangan murid yang menggemari dua hobi sahaja
 $= 12 + 3$
 $= 15$ orang

13 (a)

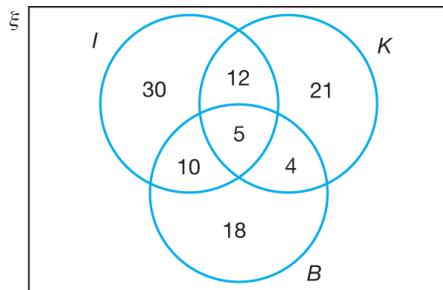


- (a) $h = 7, k = 5, m = 8$
(b) (i) Bilangan pelanggan yang tidak membeli sabun jenama R tetapi membeli sabun jenama P
 $= 7 + 3$
 $= 10$ orang
(ii) Bilangan pelanggan yang tidak membeli sabun jenama Q tetapi membeli sabun jenama P
 $= 7 + 5$
 $= 12$ orang
(c) Bilangan pelanggan yang membeli satu jenama sabun sahaja
 $= 7 + 7$
 $= 14$ orang
(d) $P' \cap R = \{ \}$
 $\therefore n(P' \cap R) = 0$

14

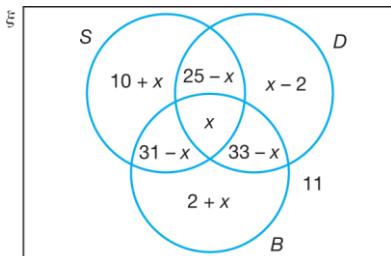


$$25+x+15-x+x+17-x+16+x+9-x+13+x=100$$
 $95+x=100$
 $x=5$

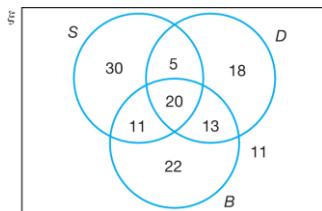


- (a) Bilangan suri rumah yang gemar memasak
(i) ketiga-tiga makanan = 5 orang
(ii) satu jenis makanan sahaja
 $= 30 + 21 + 18$
 $= 69$ orang
(iii) ayam goring atau kari ayam tetapi bukan sayur brokoli
 $= 30 + 12 + 21$
 $= 63$ orang

15



$$10+x+25-x+x+31-x+x-2+33-x+2+x+11=130$$
 $x+110=130$
 $x=20$



- (b) Bilangan pelanggan yang menggemari
(i) ketiga-tiga program
 $= 20$
(ii) satu jenis program sahaja
 $= 30 + 18 + 22$
 $= 70$ orang
(iii) sekurang-kurangnya dua jenis program
 $= 5 + 11 + 13 + 20$
 $= 49$ orang